

CARNEGIE MELLON UNIVERSITY
COMPUTER SCIENCE DEPARTMENT
15-445/645 – DATABASE SYSTEMS (FALL 2019)
PROF. ANDY PAVLO

Homework #2 (by Amadou Ngom) – Solutions
Due: **Monday Sept 30, 2019 @ 11:59pm**

IMPORTANT:

- **Upload this PDF** with your answers to **Gradescope by 11:59pm on Monday Sept 30, 2019.**
- **Plagiarism:** Homework may be discussed with other students, but all homework is to be completed **individually.**
- **You have to use this PDF for all of your answers.**

For your information:

- Graded out of **100** points; **4** questions total
- Rough time estimate: \approx 1-4 hours (0.5-1 hours for each question)

Revision : 2019/10/10 13:09

Question	Points	Score
Cuckoo Hashing	20	
B+Tree	45	
Extendible Hashing	25	
Suffix Trees	10	
Total:	100	

Number of Days this Assignment is Late:

Number of Late Day You Have Left:

Question 1: Cuckoo Hashing.....[20 points]

Graded by:

Consider the following cuckoo hashing schema:

1. Both tables have a size of 4.
2. The hashing function of the first table returns the lowest two bits: $h_1(x) = x \ \& \ 0b11$.
3. The hashing function of the second table returns the next two bits: $h_2(x) = (x \gg 2) \ \& \ 0b11$
4. When replacement is necessary, first select an element in the second table.
5. The original content is shown in Figure 1.

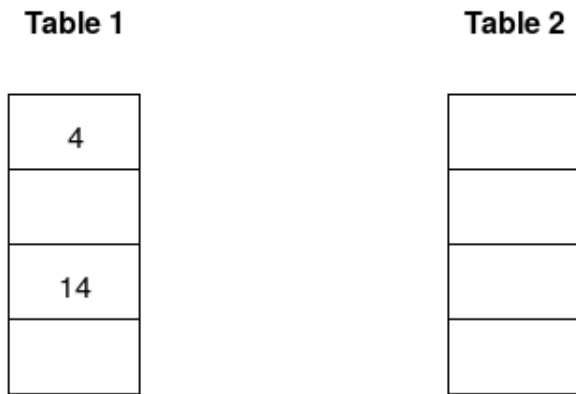


Figure 1: Initial contents of the hash tables.

Use the following template to answer the questions: <https://cmudb.io/fall2019-hw1>.

- (a) **[4 points]** Insert keys 12 and 10. Draw the resulting two tables.
- (b) **[4 points]** Then delete 14, and insert 8. Draw the resulting two tables.
- (c) **[6 points]** Finally, insert 28. Draw the resulting two tables.
- (d) **[6 points]** What is the smallest key that potentially causes an infinite loop given the tables in (c)
 0 2 5 6 7 9 None of the above

Solution: a)

Table 1	Table 2
4	
14	10
	12

b)

Table 1

4
10

Table 2

8
12

c)

Table 1

12
10

Table 2

4
8
28

Question 2: B+Tree.....[45 points]

Graded by:

Consider the following B+tree.

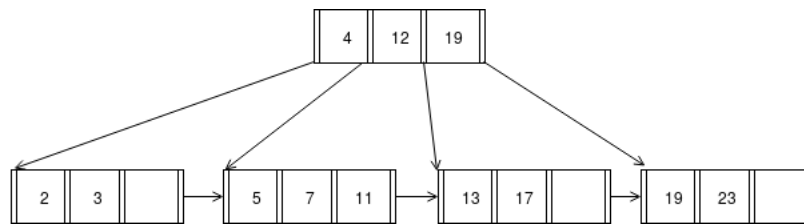


Figure 2: B+ Tree of order $d = 4$ and height $h = 2$.

When answering the following questions, be sure to follow the procedures described in class and in your textbook. You can make the following assumptions:

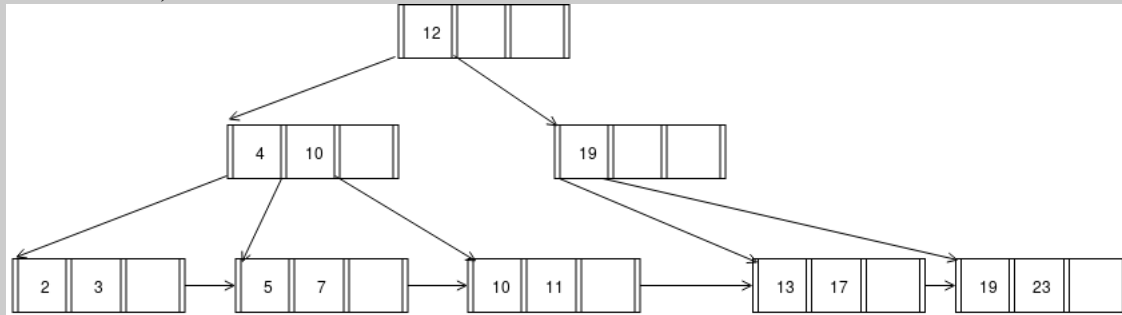
- A left pointer in an internal node guides towards keys $<$ than its corresponding key, while a right pointer guides towards keys \geq .
- A leaf node underflows when the number of **keys** goes below $\lceil \frac{d-1}{2} \rceil$.
- An internal node underflows when the number of **pointers** goes below $\lceil \frac{d}{2} \rceil$.

Use the following draw.io template for your answers:

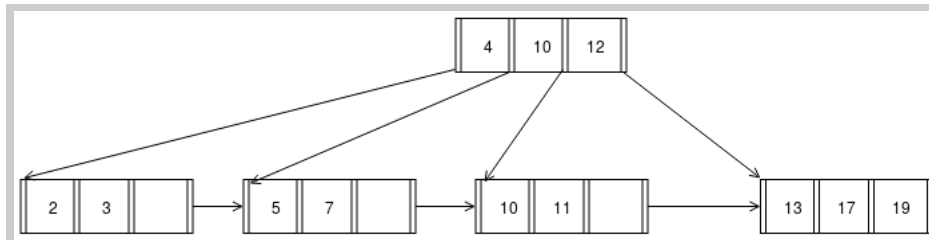
<https://cmudb.io/fall12019-hw2>

- (a) [15 points] Insert 10^* into the B+tree. Draw the resulting tree.
- (b) [5 points] How many pointers (parent-to-child and sibling-to-sibling) do you chase to find all keys between 5 and 15?
 2 3 4 5 6 7
- (c) [15 points] Then delete 23^* . Draw the resulting tree.
- (d) [10 points] Finally insert 4^* and delete 11^* . Draw the resulting tree.

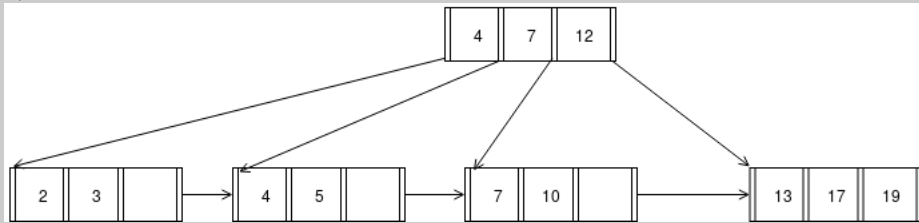
Solution: a)



b)



c)



Question 3: Extendible Hashing.....[25 points]**Graded by:**

Consider an extendible hashing structure such that:

- Each bucket can hold up to two records.
- The hashing function uses the lowest g bits, where g is the global depth.

(a) Starting from an empty table, insert keys 15, 3, 7, 14.

i. [3 points] What is the global depth of the resulting table?

- 0 1 2 3 4 None of the above

ii. [3 points] What is the local depth the bucket containing 14?

- 0 1 2 3 4 None of the above

iii. [3 points] What is the local depth of the bucket containing 3?

- 0 1 2 3 4 None of the above

(b) Starting from the result in (a), you insert keys 1, 9, 23, 11, 17.

i. [4 points] Which key will first cause a split (without doubling the size of the table)?

- 1 9 23 11 17 None of the above

ii. [4 points] Which key will first make the table double in size?

- 1 9 23 11 17 None of the above

(c) Now consider the table below, along with the following deletion rules:

1. If two buckets have the same local depth d , and share the first $d - 1$ bits of their indexes (e.g. 010 and 110 share the first 2 bits), then they can be merged if the total capacity fits in a single bucket. The resulting local depth is $d - 1$.
2. If the global depth g becomes strictly greater than all local depths, then the table can be halved in size. The resulting global depth is $g - 1$.

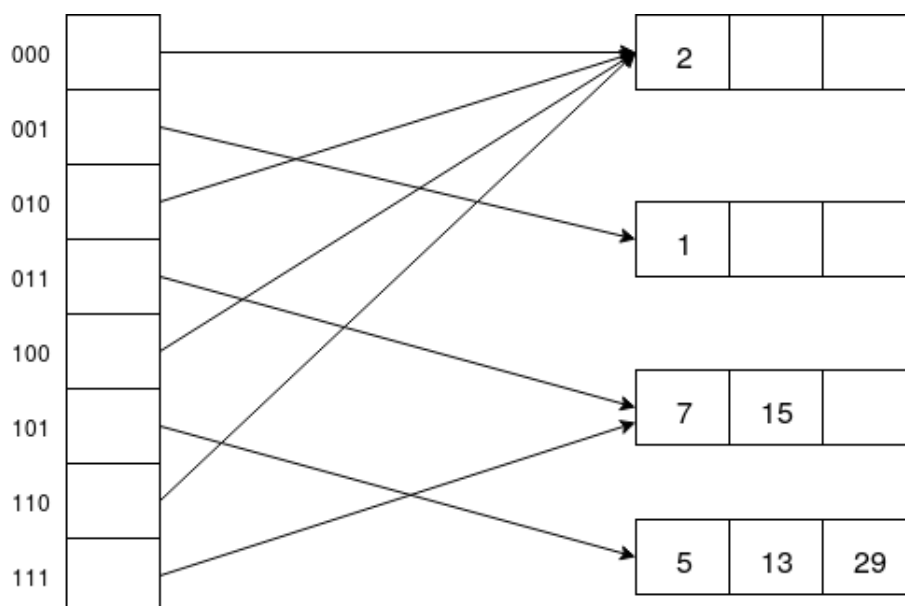


Figure 3: Extendible Hash Table along with the indexes of each bucket

Starting from the table above, delete keys 2, 7, 13, 15, 29.

- i. **[4 points]** Which deletion first causes a reduction in a local depth.
 2 7 **13** 15 29 None of the above
- ii. **[4 points]** Which deletion first causes a reduction in global depth.
 2 7 **13** 15 29 None of the above

Question 4: Suffix Trees [10 points]

Graded by:

Consider the following suffix tree for **unsigned 32-bit integers**.

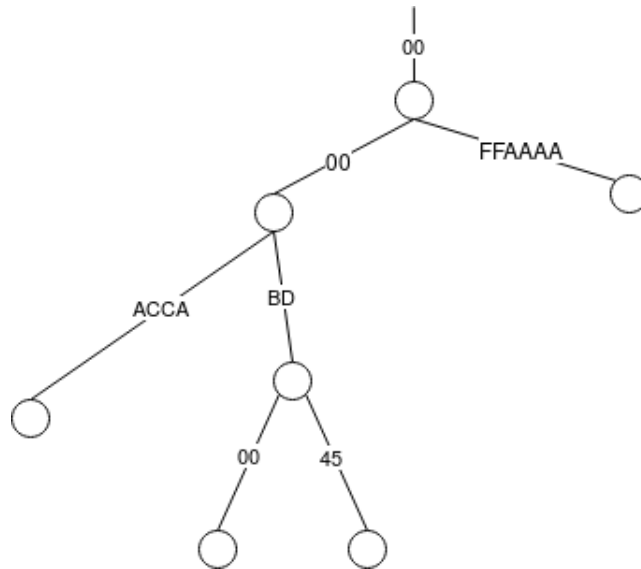


Figure 4: Suffix Tree

(a) [3 points] Which of the following elements belong to the suffix tree. Select all that apply.

- 0x45BD0000
- 0x0000CAAC
- 0xFFAAAA00
- 0xACCA0000
- 0xBD000000

None of the above

(b) [7 points] Insert the key 0x00FFAABB. Draw the resulting tree using this template: <https://cmudb.io/fall12019-hw4>.

Solution: b)