CARNEGIE MELLON UNIVERSITY COMPUTER SCIENCE DEPARTMENT 15-445/645 – DATABASE SYSTEMS (FALL 2019) PROF. ANDY PAVLO

Homework #3 (by Erik Sargent) – Solutions Due: Wednesday Oct 9, 2019 @ 11:59pm

IMPORTANT:

- Upload this PDF with your answers to Gradescope by 11:59pm on Wednesday Oct 9, 2019.
- **Plagiarism**: Homework may be discussed with other students, but all homework is to be completed **individually**.
- You have to use this PDF for all of your answers.

For your information:

- Graded out of 100 points; 2 questions total
- Rough time estimate: $\approx 1 2$ hours (0.5 1 hours for each question)

Revision : 2019/10/13 12:16

Question	Points	Score
Sorting Algorithms	40	
Join Algorithms	60	
Total:	100	

Number of Days this Assignment is Late:

Number of Late Day You Have Left:

We have a database file with six million pages (N = 6,000,000 pages), and we want to sort it using external merge sort. Assume that the DBMS is not using double buffering or blocked I/O, and that it uses quicksort for in-memory sorting. Let *B* denote the number of buffers.

(a) **[10 points]** Assume that the DBMS has <u>five</u> buffers. How many passes does the DBMS need to perform in order to sort the file?

 $\square 8 \square 10 \blacksquare 12 \square 14 \square 15$

Solution:

$$1 + \left\lceil \log_{B-1} \left(\left\lceil \frac{N}{B} \right\rceil \right) \right\rceil = 1 + \left\lceil \log_4 \left(\left\lceil 6, 000, 000/5 \right\rceil \right) \right\rceil$$
$$= 1 + \left\lceil \log_4 \left(\left\lceil 1, 200, 000 \right\rceil \right) \right\rceil$$
$$= 1 + 11 = 12$$

(b) **[5 points]** Again, assuming that the DBMS has <u>five</u> buffers. What is the total I/O cost to sort the file?

 \Box 72,000,000 \Box 120,000,000 \Box 132,000,000 \blacksquare 144,000,000 \Box 168,000,000

Solution: $Cost = 2N \times \# passes = 2 \times 6,000,000 \times 12$

(c) **[10 points]** What is the smallest number of buffers *B* that the DBMS can sort the target file using only <u>two</u> passes?

 $\square 50 \square 51 \square 52 \square 53 \square 172 \square 173 \square 174 \blacksquare$ **2,450** $\square 2,451 \\ \square 2,452 \square 3,000,000 \square 3,000,001$

Solution: We want *B* where $N \le B \times (B - 1)$. If B = 2450, then 6,000,000 $\le 2450 \times 2449 = 6,000,050$; any smaller value for *B* would fail.

- (d) [10 points] What is the smallest number of buffers B that the DBMS can sort the target file using only <u>four</u> passes?
 □ 50 51 □ 52 □ 53 □ 172 □ 173 □ 174 □ 2,450 □ 2,451 □ 2,452 □ 3,000,000 □ 3,000,001
 Solution: B × (B 1)³ = 51 × 50 × 50 × 50 = 6,375,000. Any smaller value of B would fail.
- (e) **[5 points]** Suppose the DBMS has <u>ten</u> buffers. What is the largest database file (expressed in terms of N, the number of pages) that can be sorted with external merge sort using <u>five</u> passes?

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□ 89 □ 9 □ 590,489	90 □ 91 □ 590,490	■ 65,610	□ 65,611	□ 65,612	□ 590,488
Solution: Waitself, which it	e want N such th is $10 \times 9^4 = 656$	at $N \le B \times (B)$	$(3-1)^4$. The large	gest such value	is $B \times (B-1)^4$

Consider relations R(a, b) and S(a, c, d) to be joined on the common attribute a. Assume that there are no indexes available on the tables to speed up the join algorithms.

- There are B = 36 pages in the buffer
- Table R spans M = 1800 pages with 100 tuples per page
- Table S spans N = 600 pages with 60 tuples per page

Answer the following questions on computing the I/O costs for the joins. You can assume the simplest cost model where pages are read and written one at a time. You can also assume that you will need <u>one</u> buffer block to hold the evolving output block and <u>one</u> input block to hold the current input block of the inner relation. You may ignore the cost of the writing of the final results.

- (a) Hash join with S as the outer relation and R as the inner relation. You may ignore recursive partitioning and partially filled blocks.
 - i. [5 points] What is the cost of the partition phase?
 □ 1,800 □ 2,400 □ 3,600 4,800 □ 7,200
 Solution: 2 × (M + N) = 2 × (1800 + 600) = 2 × 2400 = 4800
 ii. [5 points] What is the cost of the probe phase?
 □ 1,800 2,400 □ 3,600 □ 4,800 □ 7,200

Solution: (M + N) = (1800 + 600) = 2400

(b) **[10 points]** Block nested loop join with R as the outer relation and S as the inner relation: \Box 31,200 \Box 31,800 \Box 32,400 \Box 33,000 \blacksquare 33,600

Solution: $M + \left\lceil \frac{M}{B-2} \right\rceil \times N = 1800 + \left\lceil \frac{1800}{34} \right\rceil \times 600 = 1800 + 31800 = 33600$

(c) [5 points] Block nested loop join with S as the outer relation and R as the inner relation: \Box 31,200 \Box 31,800 \Box 32,400 \blacksquare 33,000 \Box 33,600

Solution: $N + \lceil \frac{N}{B-2} \rceil \times M = 600 + \lceil \frac{600}{34} \rceil \times 1800 = 600 + 32400 = 33000$

- (d) Sort-merge join with S as the outer relation and R as the inner relation:
 - i. **[10 points]** What is the cost of sorting the tuples in R on attribute a? □ 3,600 □ 5,400 □ 7,200 □ 9,000 ■ **10,800**

Solution: $passes = 1 + \lceil \log_{B-1}(\lceil \frac{M}{B} \rceil) \rceil = 3$ $2M \times passes = 2 * 1800 * 3 = 10800$ ii. [5 points] What is the cost of sorting the tuples in S on attribute a? **2,400** \square 3,000 \square 3,600 \square 4,200 \square 4,800

Solution: $passes = 1 + \lceil \log_{B-1}(\lceil \frac{N}{B} \rceil) \rceil = 2$ $2N \times passes = 2 * 600 * 2 = 2400$

iii. **[10 points]** What is the cost of the merge phase assuming there are no duplicates in the join attribute?

□ 1,200 □ 1,800 **■ 2,400** □ 3,600 □ 4,800 Solution: M + N = 1800 + 600 = 2400

iv. [10 points] What is the cost of the merge phase in the worst case scenario? \Box 2,400 \Box 4,800 \Box 600,000 \blacksquare 1,080,000 \Box 1,200,000 \Box 1,200,000

Solution: $M \times N = 1800 \times 600 = 1080000$