CARNEGIE MELLON UNIVERSITY COMPUTER SCIENCE DEPARTMENT 15-445/645 – DATABASE SYSTEMS (FALL 2020) PROF. ANDY PAVLO

Homework #3 (by Kunal Jobanputra) – Solutions Due: **Sunday Oct 18, 2020** @ **11:59pm**

IMPORTANT:

- Upload this PDF with your answers to Gradescope by 11:59pm on Sunday Oct 18, 2020.
- **Plagiarism**: Homework may be discussed with other students, but all homework is to be completed **individually**.
- You have to use this PDF for all of your answers.

For your information:

• Graded out of 100 points; 2 questions total

• Rough time estimate: $\approx 1 - 2$ hours (0.5 - 1 hours for each question)

Revision: 2020/10/25 11:35

Question	Points	Score
Sorting Algorithms	40	
Join Algorithms	60	
Total:	100	

Question 1: Sorting Algorithms	[40 points]
Graded by:	

We have a database file with eight million pages (N = 8,000,000 pages), and we want to sort it using external merge sort. Assume that the DBMS is not using double buffering or blocked I/O, and that it uses quicksort for in-memory sorting. Let B denote the number of buffers.

(a) [10 points] Assume that the DBMS has <u>four</u> buffers. How many passes does the DBMS need to perform in order to sort the file?

 \square 8 \square 10 \square 12 \square 14 \blacksquare 15

Solution:

$$1 + \left\lceil \log_{B-1} \left(\left\lceil \frac{N}{B} \right\rceil \right) \right\rceil = 1 + \left\lceil \log_3 \left(\left\lceil 8, 000, 000/4 \right\rceil \right) \right\rceil$$
$$= 1 + \left\lceil \log_3 \left(\left\lceil 2, 000, 000 \right\rceil \right) \right\rceil$$
$$= 1 + 14 = 15$$

(b) **[5 points]** Again, assuming that the DBMS has <u>four</u> buffers. What is the total I/O cost to sort the file?

 \square 60,000,000 \square 120,000,000 \square 144,000,000 \blacksquare **240,000,000** \square 480,000,000

Solution: $Cost = 2N \times \#passes = 2 \times 8,000,000 \times 15$

(c) [10 points] What is the smallest number of buffers B that the DBMS can sort the target file using only two passes?

 \square 172 \square 173 \square 174 \square 2,450 \square 2,451 \square 2,452 \square 2,827 \square 2,828 \blacksquare 2.829 \square 3,999,999 \square 4,000,000 \square 4,000,001

Solution: We want B where $N \le B \times (B-1)$. If B=2829, then $8,000,000 \le 2829 \times 2828 = 8,000,412$; any smaller value for B would fail.

(d) [10 points] What is the smallest number of buffers B that the DBMS can sort the target file using only five passes?

 \square 24 **■ 25** \square 26 \square 50 \square 51 \square 52 \square 53 \square 2,450 \square 2,451 \square 2,452 \square 3,999,999 \square 4,000,000 \square 4,000,001

Solution: $B \times (B-1)^4 = 25 \times 24 \times 24 \times 24 \times 24 = 8,294,400$. Any smaller value of B would fail.

(e) [5 points] Suppose the DBMS has $\underline{\text{twenty}}$ buffers. What is the largest database file (expressed in terms of N, the number of pages) that can be sorted with external merge sort using $\underline{6}$ passes?

□ 89	□ 98	□ 65,610	□ 65,601	□ 590,490	□ 590,940	49,521,980
□ 49,2	251,980	□ 56,980,2	$34 \Box \ 65,98$	80,234		

Solution: We want N such that $N \leq B \times (B-1)^5$. The largest such value is $B \times (B-1)^5$ itself, which is $20 \times 19^5 = 49,521,980$.

Question 2: Join Algorithms [60 points] Graded by:

Homework #3

Consider relations R(a, b) and S(a, c, d) to be joined on the common attribute a. Assume that there are no indexes available on the tables to speed up the join algorithms.

- There are B = 75 pages in the buffer
- Table R spans M = 2,400 pages with 80 tuples per page
- Table S spans N = 1,200 pages with 100 tuples per page

Answer the following questions on computing the I/O costs for the joins. You can assume the simplest cost model where pages are read and written one at a time. You can also assume that you will need <u>one</u> buffer block to hold the evolving output block and <u>one</u> input block to hold the current input block of the inner relation. You may ignore the cost of the writing of the final results.

(a)	Hash join with S as the outer relation and R as the inner relation.	You may ignore recursive
	partitioning and partially filled blocks.	

i.	[5 points]	What is the cost of the partition phase?
	□ 1,800	$\square \ 2,400 \ \square \ 3,600 \ \square \ 4,800 \ \blacksquare \ 7,200$
	Solution:	$2 \times (M+N) = 2 \times (2,400+1,200) = 2 \times 3,600 = 7,200$
ii.	[5 points]	What is the cost of the probe phase?
	\Box 1,800	$\Box 2,400 \blacksquare 3,600 \Box 4,800 \Box 7,200$

Solution: $(M+N) = (2,400+1,200) = 3,600$
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- (b) [10 points] Assume that the tables do not fit in main memory and that a high cardinality of distinct values hash to the same bucket using your hash function h_1 . Which of the following approaches works the best?
 - Create hashtables for the innner and outer relation using h_1 and rehash into an embedded hash table using $h_2 != h_1$ for large buckets

	Create	hashtables	for the	innner	and	outer	relation	using	h_1	and	rehash	into	an	em-
be	dded ha	ish table us		or large	bucl	kets								

 \Box Use linear probing for collisions and page in and out parts of the hashtable needed at a given time

 \Box Create 2 hashtables half the size of the original one, run the same hash join algorithm on the tables, and then merge the hashtables together

		ution: ion desc		sn join with re	cursive pa	rtitioning, which i	s what the correct
(c)	_			loop join with F □ 33,600		ter relation and S as	s the inner relation
	Sol	ution:	$M + \lceil \frac{M}{B-2} \rceil \times$	N = 2,400 +	$\left\lceil \frac{2,400}{73} \right\rceil \times$	1,200 = 2,400 + 3	39,600 = 42,000
(d)		_		loop join with S □ 33,600		ter relation and R as □ 42,600	s the inner relation
	Sol	ution:	$N + \left\lceil \frac{N}{B-2} \right\rceil \times$	M = 1,200 +	$\left\lceil \frac{1,200}{73} \right\rceil \times$	2,400 = 1,200 + 4	40,800 = 42,000
(e)		[5 poir	its] What is t		ng the tupl	s the inner relation es in R on attribute 10,800	
				$1 + \lceil \log_{B-1}(\lceil 2, 400 * 2 = 9, \rceil)$			
	ii.	_		he cost of sorting \Box 3,600	-	es in S on attribute 4,800	a?
				$1 + \lceil \log_{B-1}(\lceil 1, 200 * 2 = 4, \rceil)$			
	iii.	the join	attribute?	the cost of the \Box 2,400		se assuming there a \Box 4,800	are no duplicates in
		Soluti	on: $M + N =$	=2,400+1,20	00 = 3,600		
	iv.	_				se in the worst case \Box 4, 750,000	

Solution: $M \times N = 2,400 \times 1,200 = 2,880,000$