CARNEGIE MELLON UNIVERSITY COMPUTER SCIENCE DEPARTMENT 15-445/645 – DATABASE SYSTEMS (FALL 2024) PROF. ANDY PAVLO

Homework #3 (by William) Due: Sunday October 6th, 2024 @ 11:59pm

IMPORTANT:

- Enter all of your answers into Gradescope by 11:59pm on Sunday October 6th, 2024.
- **Plagiarism**: Homework may be discussed with other students, but all homework is to be completed **individually**.

For your information:

- Graded out of 100 points; 5 questions total
- Rough time estimate: \approx 4-6 hours (1-1.5 hours for each question)

Revision : 2024/09/26 21:43

Question	Points	Score
Linear Hashing and Cuckoo Hashing	18	
Extendible Hashing	20	
B+Tree	27	
Bloom Filter	20	
Alternate Index Structures	15	
Total:	100	

For warmup, consider the following Linear Probe Hashing schema:

- 1. The table have a size of 4 slots, each slot can only contain one key value pair.
- 2. The hashing function is $h_1(\mathbf{x}) = \mathbf{x} \ \% \ 4.$
- 3. When there is conflict, it finds the next free slot to insert key value pairs.
- 4. The original table is empty.
- 5. Uses a tombstone when deleting a key.
- (a) **[2 points]** Insert key/value pair (1,A) and (7,B). For (1,A), "1" is the key and "A" is the value. Select the value in each entry of the resulting table.
 - i. Entry 0 (key % 4 = 0) $\Box A$ $\Box B$ \Box Emptyii. Entry 1 (key % 4 = 1) $\Box A$ $\Box B$ \Box Emptyiii. Entry 2 (key % 4 = 2) $\Box A$ $\Box B$ \Box Emptyiv. Entry 3 (key % 4 = 3) $\Box A$ $\Box B$ \Box Empty
- (b) [2 points] After the changes from part (a), delete (1, A), insert key value (5, D), and lastly insert (9, C). Select the value in each entry of the resulting table.

i. Entry 0 (key % $4 = 0$) \Box Tombstone	\Box A	$\square B$	\Box C	\Box D	□ Empty
ii. Entry 1 (key % $4 = 1$) \Box Tombstone	\Box A	$\square B$	\Box C	\Box D	□ Empty
iii. Entry 2 (key % $4 = 2$) \Box Tombstone	\Box A	$\square B$	\Box C	\Box D	□ Empty
iv. Entry 3 (key % $4 = 3$) \Box Tombstone	\Box A	$\square B$	\Box C	\Box D	□ Empty

Consider the following *Cuckoo Hashing* schema:

- 1. Both tables have a size of 4.
- 2. The hashing function of the first table returns the fourth and third least significant bits: $h_1(x) = (x \ge 2) \& 0b11.$
- 3. The hashing function of the second table returns the least significant two bits: $h_2(\mathbf{x}) = \mathbf{x} \& 0b11$.
- 4. When inserting, try table 1 first.
- 5. When replacement is necessary, first select an element in the second table.
- 6. The original entries in the table are shown in the figure below.

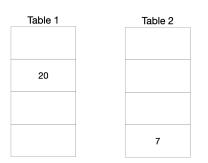


Figure 1: Initial contents of the hash tables.

(a) [2 points] Select the sequence of insert operations that results in the initial state. □ Insert 20, Insert 7 □ Insert 7, Insert 20 □ None of the above

- (b) Starting from the initial contents, insert key 22 and then insert 38. Select the values in the resulting two tables.
 - i. Table 1

α) [1 point]	Entry 0 (0b00)	□ 20	□ 7	□ 22	□ 38	□ Empty
β) [1 point]	Entry 1 (0b01)	□ 20	□ 7	□ 22		□ Empty
γ) [1 point]	Entry 2 (0b10)	□ 20	□ 7	□ 22		□ Empty
δ) [1 point]	Entry 3 (0b11)	□ 20	□ 7	□ 22		□ Empty
:: Table 2						
ii. Table 2						
<i>α</i>) [1 point]	Entry 0 (0b00)	\Box 20	□ 7	□ 22	□ 38	□ Empty
β) [1 point]	Entry 1 (0b01)	□ 20	□ 7	□ 22	□ 38	□ Empty
γ) [1 point]	Entry 2 (0b10)	□ 20	□ 7	□ 22	□ 38	□ Empty
δ) [1 point]	Entry 3 (0b11)	□ 20	□ 7	□ 22	□ 38	□ Empty

- (c) **[4 points]** Consider completely empty tables using the same two hash functions. Select which sequence of insertions below will cause an infinite loop.
 - □ [0, 4, 17, 20]
 - □ [0, 4, 16, 20]
 - □ [1, 4, 16, 20]
 - □ [1, 5, 17, 22]
 - \Box None of the above

Consider an extendible hashing structure such that:

- Each bucket can hold up to two records.
- The hashing function uses the lowest g bits, where g is the global depth.
- A new extendible hashing structure is initialized with q = 0 and one empty bucket
- If multiple keys are provided in a question, assume they are inserted one after the other from left to right.
- (a) Starting from an empty table, insert keys 1, 2.
 - i. **[1 point]** What is the global depth of the resulting table?
 - $\Box 0 \Box 1 \Box 2 \Box 3 \Box 4 \Box$ None of the above
 - ii. **[1 point]** What is the local depth of the bucket containing 2? $\Box \ 0 \ \Box \ 1 \ \Box \ 2 \ \Box \ 3 \ \Box \ 4 \ \Box$ None of the above
- (b) Starting from the result in (a), you insert keys 9, 11.
 - i. **[2 points]** What is the global depth of the resulting table? $\Box \ 0 \ \Box \ 1 \ \Box \ 2 \ \Box \ 3 \ \Box \ 4 \ \Box$ None of the above
 - ii. [2 points] What are the local depths of the buckets for each key?
 - □ 1 (Depth 1), 2 (Depth 1), 9 (Depth 1), 11 (Depth 1)
 - □ 1 (Depth 3), 2 (Depth 1), 9 (Depth 3), 11 (Depth 3)
 - □ 1 (Depth 2), 2 (Depth 1), 9 (Depth 2), 11 (Depth 2)
 - □ 1 (Depth 3), 2 (Depth 1), 9 (Depth 3), 11 (Depth 2)
 - □ 1 (Depth 2), 2 (Depth 2), 9 (Depth 2), 11 (Depth 2)
 - \Box None of the above
- (c) Starting from the result in (b), you insert keys 13, 27.
 - i. **[2 points]** What is the global depth of the resulting table? $\Box \ 0 \ \Box \ 1 \ \Box \ 2 \ \Box \ 3 \ \Box \ 4 \ \Box$ None of the above
 - $\Box 0 \Box 1 \Box 2 \Box 3 \Box 4 \Box$ None of the above
 - ii. [2 points] What are the local depths of the buckets for each new key?
 - □ 13 (Depth 1), 27 (Depth 1)
 - □ 13 (Depth 1), 27 (Depth 2)
 - \Box 13 (Depth 2), 27 (Depth 2)
 - □ 13 (Depth 3), 27 (Depth 2)
 - □ 13 (Depth 3), 27 (Depth 3)
 - \Box None of the above
- (d) [3 points] Starting from (c)'s result, which key(s), if inserted next, will not cause a split? \Box 5 \Box 17 \Box 43 \Box 8 \Box None of the above
- (e) **[3 points]** Starting from the result in (c), which **key**(s), if inserted next, will cause a split and increase the table's global depth?
 - \Box 0 \Box 3 \Box 5 \Box 17 \Box None of the above
- (f) **[4 points]** Starting from an empty table, insert keys 32, 64, 128, 512. What is the global depth of the resulting table?

 $\Box 4 \quad \Box 5 \quad \Box 6 \quad \Box 7 \quad \Box 8 \quad \Box \ge 9$

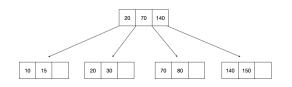


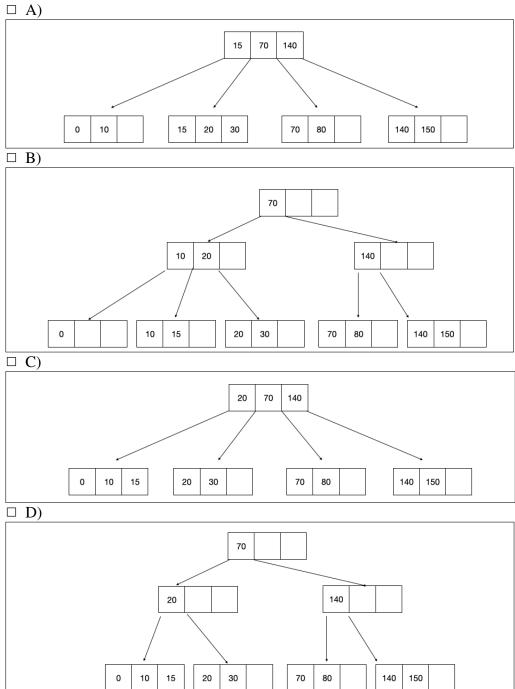
Figure 2: B+ Tree of order d = 4 and height h = 2.

When answering the following questions, be sure to follow the procedures described in class and in your textbook. You can make the following assumptions:

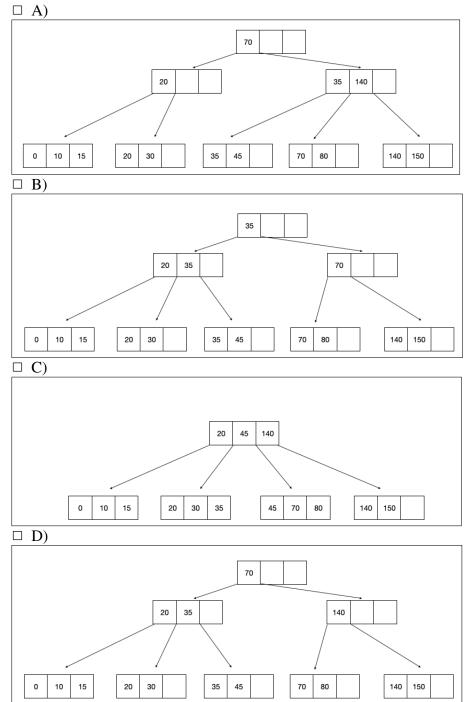
- A left pointer in an internal node guides towards keys < than its corresponding key, while a right pointer guides towards keys ≥.
- A leaf node underflows when the number of **keys** goes below $\lceil \frac{d-1}{2} \rceil$.
- An internal node underflows when the number of **pointers** goes below $\left\lceil \frac{d}{2} \right\rceil$.

Note that B+ tree diagrams for this problem omit leaf pointers for convenience. The leaves of actual B+ trees are linked together via pointers, forming a singly linked list allowing for quick traversal through all keys.

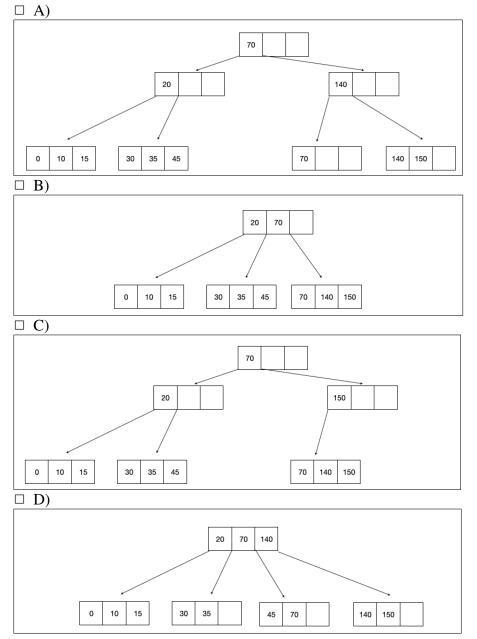
(a) [4 points] Insert 0^* into the B+tree. Select the resulting tree.



(b) **[5 points]** Starting with the tree that results from (a), insert 35^{*} and then 45^{*}. Select the resulting tree.



(c) [8 points] Starting with the tree that results from (b), deletes 80^{*} and then 20^{*}. Select the resulting tree.



- (d) i. [2 points] Under optimistic latch crabbing, read-only thread can drop its latch on the current page before acquiring the latch on the next page (e.g., child, sibling).
 □ True □ False
 - ii. **[2 points]** Under optimistic latch coupling, write threads never take the write latch on the root to avoid contention.
 - \Box True \Box False
 - iii. [2 points] Threads can release their latches in any order.
 - \Box True \Box False
 - iv. **[2 points]** "No-Wait" mode for acquiring sibling latches prevents deadlock by allowing a read thread to inspect what another thread is doing.
 - \Box True \Box False
 - v. **[2 points]** For OLTP-style queries, a DBMS will not benefit from using two separate buffer pools for inner node and leaf pages.
 - \Box True \Box False

functions h_1 and h_2 which hash the following strings to the following values:

input	h_1	h_2
"DataBootX"	1749	8327
"QueryOptimizeR"	4123	9681
"FilterStream"	5076	2310
"ProtoBloom"	6598	9842

(a) **[6 points]** Suppose the filter has 8 bits initially set to 0:

bit 0	bit 1	bit 2	bit 3	bit 4	bit 5	bit 6	bit 7
0	0	0	0	0	0	0	0

Which bits will be set to 1 after "DataBootX" and "ProtoBloom" have been inserted? \Box 0 \Box 1 \Box 2 \Box 3 \Box 4 \Box 5 \Box 6 \Box 7

(b) Suppose the filter has 8 bits set to the following values:

bit 0	bit 1	bit 2	bit 3	bit 4	bit 5	bit 6	bit 7
0	1	0	1	1	1	0	0

- i. **[4 points]** What will we learn using the above filter if we lookup "FilterStream"? □ FilterStream has been inserted
 - □ FilterStream has not been inserted
 - □ FilterStream may have been inserted
 - \Box Not possible to know
- ii. [4 points] What will we learn if we lookup "QueryOptimizeR"?
 - □ QueryOptimizeR has been inserted
 - □ QueryOptimizeR has not been inserted
 - □ QueryOptimizeR may have been inserted
 - \Box Not possible to know
- (c) **[6 points]** A colleague is interviewing a candidate and would like to first test your knowledge of bloom filters. The colleague has a list of prepared statements and would like you to identify which of them are true. Select all true statements.
 - □ Bloom filters can eliminate unnecessary disk I/Os.
 - \Box We can lower a bloom filter's false positive rate by using more hash functions.
 - \Box Bloom filters are effective for exact-match (or lookup) queries.
 - $\hfill\square$ Add and lookup operations on bloom filters are parallelizable.
 - \Box All of the above.

- (a) [5 points] Your manager is thinking of utilizing a skip list index. They asked a large language model for some factual statements about skip lists but are uncertain about the model's response. They would like you to identify all factually correct statements.
 □ Multiple threads can scan, insert, and delete from skip-lists without latches.
 - □ Skip Lists require re-balancing.
 - \Box Single-Linked Skip Lists support finding (keys \leq X) and (keys \geq X).
 - \Box When inserting a key into a skip list, the number of towers is a function of the key.
 - \Box Each level (i) of a skip list *must* have half the nodes as the level below (i+1).
 - \Box None of the above
- (b) [5 points] You are interviewing for a company. The team lead is asking you to compare B+Trees, Skip Lists, Radix Trees, and Inverted Indexes. Select all the true statements.
 - □ Both Skip Lists and B+Tree guarantee logarithmic complexity for lookups.
 - $\hfill\square$ Radix Trees and Inverted Indexes are both efficient at substring predicates.
 - $\hfill\square$ B+Tree performs better than Radix Trees for prefix queries.
 - $\hfill\square$ Update overhead is generally Inverted Index > Skip Lists > B+Tree.
 - \Box None of the above.
- (c) **[5 points]** Suppose you are trying to run the following query:

SELECT * FROM PEOPLE WHERE name NOT LIKE '%WuTang%';

Assume that there is a non-clustering B+Tree index on name. Your query takes too long. Which of the following choices (if any) would make this query go faster?

- □ Replace non-clustering B+Tree with a *clustering* B+Tree index on name.
- \Box Replace the index with a *hash index* on name.
- \Box Drop the index and build a *bloom filter* on name.
- □ Replace the index with a *trie or radix tree* on name.
- \Box None of the above.