# Selection Interview Interview Interview Intro to Database Systems (15-445/645) **08 B+Tree Indexes**



#### **ADMINISTRIVIA**

Homework 2 due February 17<sup>th</sup>.

Project 1 due February 19<sup>th</sup>. → Saturday office hours: February 18<sup>th</sup> 3-5 p.m.

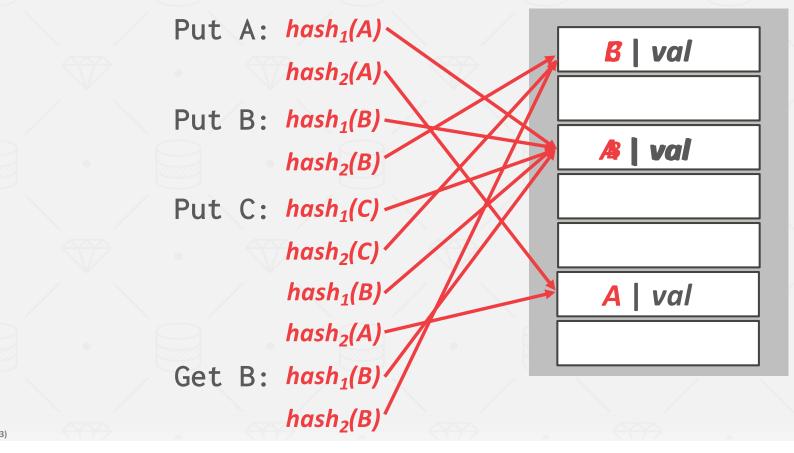
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# LAST TIME

Hash tables

- $\rightarrow$  Hash Functions
- $\rightarrow$  Static Hashing Schemes
- $\rightarrow$  Dynamic Hashing Schemes

#### **CUCKOO HASHING**



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# **CUCKOO HASHING PARAMETERS**

- 1. # of buckets
- 2. # of hash functions
- 3. # of slots per bucket

# **DATA STRUCTURES**

Internal Meta-data Core Data Storage Temporary Data Structures Table Indexes

#### **TABLE INDEXES**

A <u>table index</u> is a replica of a subset of a table's attributes that are organized and/or sorted for efficient access using those attributes.

The DBMS ensures that the contents of the table and the index are logically synchronized.

#### **TABLE INDEXES**

It is the DBMS's job to figure out the best index(es) to use to execute each query.

There is a trade-off regarding the number of indexes to create per database.

- $\rightarrow$  Storage Overhead
- $\rightarrow$  Maintenance Overhead

# **TODAY'S AGENDA**

Q

B+Tree Overview Use in a DBMS Design Choices Optimizations

# **B-TREE FAMIL**

There is a specific data structure ca

People also use the term to genera class of balanced tree data structu  $\rightarrow$  **B-Tree** (1971)  $\rightarrow$  **B+Tree** (1973)  $\rightarrow$  **B\*Tree** (1977?)

 $\rightarrow$  **B**<sup>link</sup>-Tree (1981

#### The Ubiquitous B-Tree

DOUGLAS COMER

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B-trees have become, de facto, a standard for file organization. File indexes of users dedicated database systems, and general-purpose access methods have all been proposed and implemented using B-trees This paper reviews B-trees and shows why they have been so successful It discusses the major variations of the B-tree, especially the B<sup>+</sup>-tree, contrasting the relative merits and costs of each implementation. It illustrates a general purpose access method which uses a B-tree.

Keywords and Phrases: B-tree, B\*-tree, B\*-tree, file organization, index CR Categories: 3.73 3.74 4.33 4 34

#### INTRODUCTION

The secondary storage facilities available on large computer systems allow users to store, update, and recall data from large collections of information called files. A computer must retrieve an item and place it in main memory before it can be processed. In order to make good use of the computer resources, one must organize files intelligently, making the retrieval process efficient.

The choice of a good file organization depends on the kinds of retrieval to be performed. There are two broad classes of retrieval commands which can be illustrated by the following examples: Sequential: "From our employee file, pre-

pare a list of all employees' names and addresses," and Random: "From our employee file, ex-

tract the information about employee J. Smith".

We can imagine a filing cabinet with three drawers of folders, one folder for each employee. The drawers might be labeled "A- by considering last names as index entries,

might be labeled with the employees' last names. A sequential request requires the searcher to examine the entire file, one folder at a time. On the other hand, a random request implies that the searcher, guided by the labels on the drawers and folders, need only extract one folder.

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Associated with a large, randomly accessed file in a computer system is an *index* which, like the labels on the drawers and folders of the file cabinet, speeds retrieval by directing the searcher to the small part of the file containing the desired item. Figure 1 depicts a file and its index. An index may be physically integrated with the file, like the labels on employee folders, or physically separate, like the labels on the drawers. Usually the index itself is a file. If the index file is large, another index may be built on top of it to speed retrieval further, and so on. The resulting hierarchy is similar to the employee file, where the topmost index consists of labels on drawers, and the next level of index consists of labels on folders.

G," "H-R," and "S-Z," while the folders do not always produce the best perform-

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Computing Surveys, Vol 11, No 2, June 1979

# **B+TREE**

A **B+Tree** is a self-balancing, ordered tree data structure that allows searches, sequential access, insertions, and deletions in **O(log n)**.

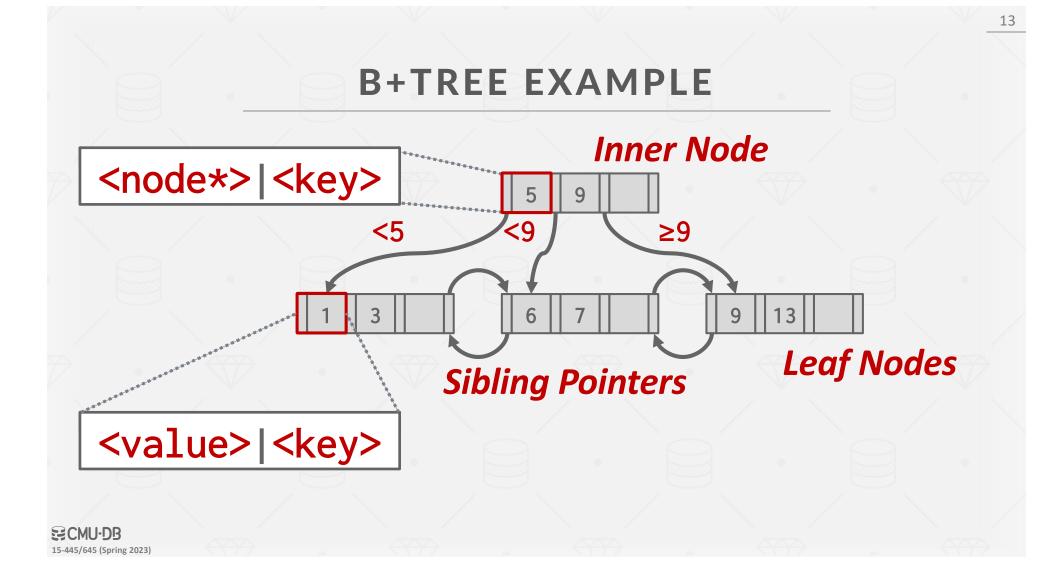
- → Generalization of a binary search tree, since a node can have more than two children.
- → Optimized for systems that read and write large blocks of data.

#### **B+TREE PROPERTIES**

A B+Tree is an *M*-way search tree with the following properties:

- → It is perfectly balanced (i.e., every leaf node is at the same depth in the tree)
- → Every node other than the root is at least half-full M/2-1 ≤ #keys ≤ M-1

 $\rightarrow$  Every inner node with **k** keys has **k+1** non-null children



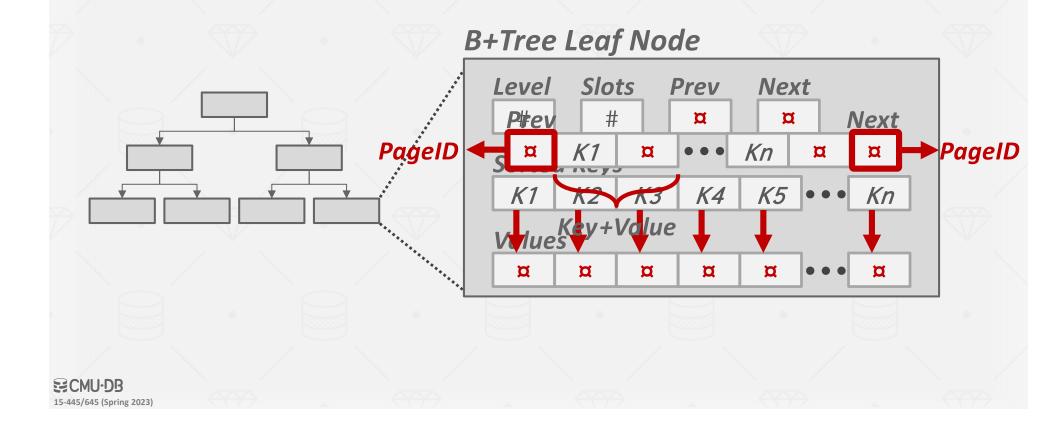
# NODES

Every B+Tree node is comprised of an array of key/value pairs.

- → The keys are derived from the attribute(s) that the index is based on.
- → The values will differ based on whether the node is classified as an <u>inner node</u> or a <u>leaf node</u>.

The arrays are (usually) kept in sorted key order.

#### **B+TREE LEAF NODES**



# **LEAF NODE VALUES**

#### Approach #1: Record IDs

 $\rightarrow$  A pointer to the location of the tuple to which the index entry corresponds.

#### Approach #2: Tuple Data

- $\rightarrow$  The leaf nodes store the actual contents of the tuple.
- $\rightarrow$  Secondary indexes must store the Record ID as their values.



DB2

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#### **B-TREE VS. B+TREE**

The original **B-Tree** from 1972 stored keys and values in all nodes in the tree.

→ More space-efficient, since each key only appears once in the tree.

A **B+Tree** only stores values in leaf nodes. Inner nodes only guide the search process.

# **B+TREE – INSERT**

Find correct leaf node L. Insert data entry into L in sorted order.

If L has enough space, done!

Otherwise, split L keys into L and a new node L2

 $\rightarrow$  Redistribute entries evenly, copy up middle key.

 $\rightarrow$  Insert index entry pointing to L2 into parent of L.

To split inner node, redistribute entries evenly, but push up middle key.

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#### **B+TREE VISUALIZATION**

# https://cmudb.io/btree

Source: David Gales (Univ. of San Francisco)

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# **B+TREE - DELETE**

Start at root, find leaf L where entry belongs. Remove the entry.

If L is at least half-full, done!

- If L has only M/2-1 entries,
- $\rightarrow$  Try to re-distribute, borrowing from sibling (adjacent node with same parent as L).
- $\rightarrow$  If re-distribution fails, merge L and sibling.

If merge occurred, must delete entry (pointing to L or sibling) from parent of L.

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#### **SELECTION CONDITIONS**

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The DBMS can use a B+Tree index if the query provides any of the attributes of the search key.

Example: Index on <a,b,c>

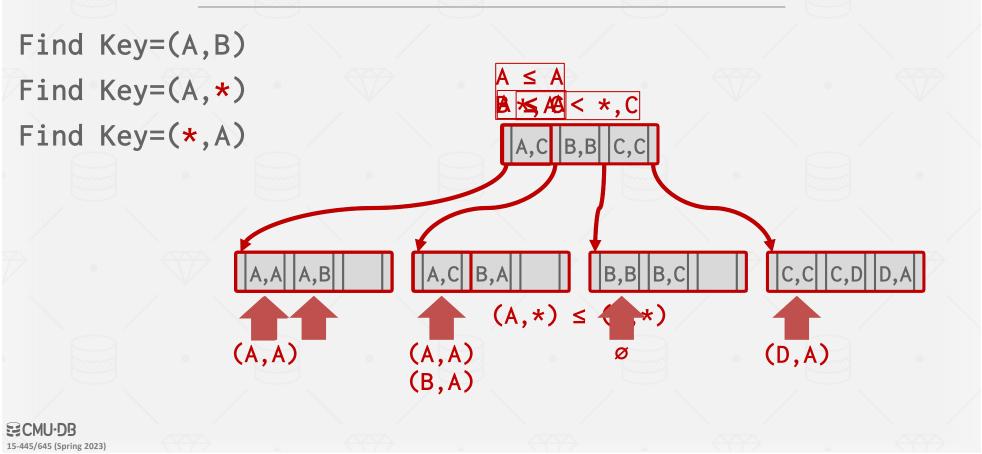
- $\rightarrow$  Supported (a=1 AND b=2 AND c=3)
- $\rightarrow$  Supported: (a=1 AND b=2)
- $\rightarrow$  Supported: (b=2), (c=3)

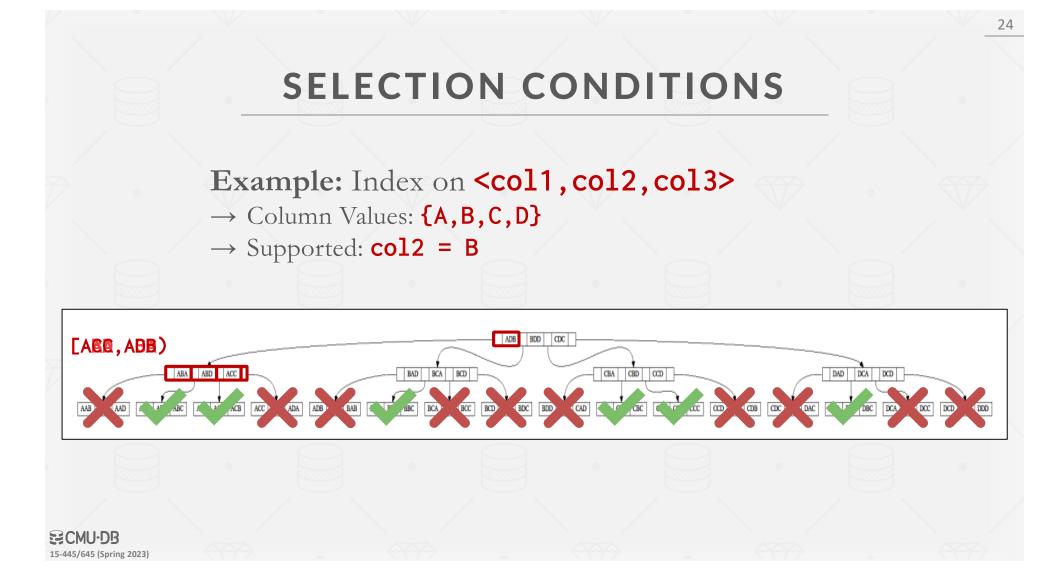
Not all DBMSs support this. For a hash index, we must have all attributes in search key.

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#### **SELECTION CONDITIONS**

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# **B+TREE - DUPLICATE KEYS**

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#### Approach #1: Append Record ID

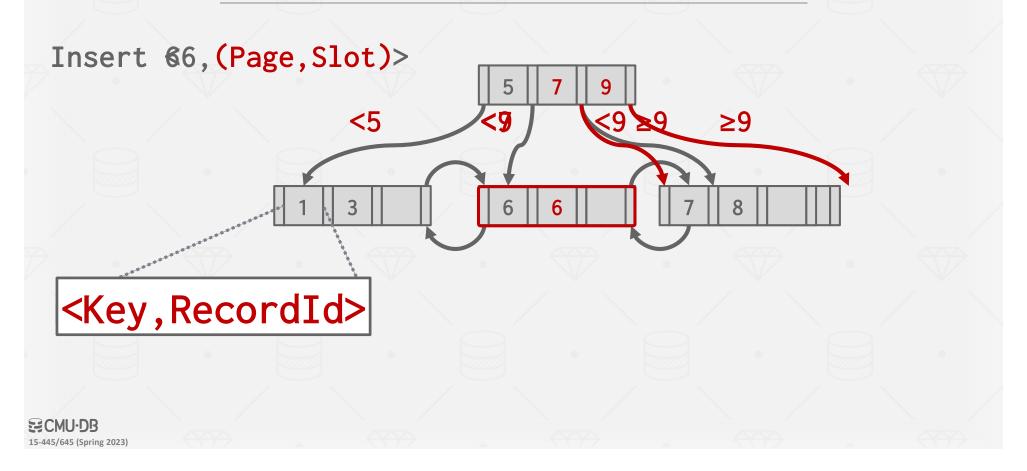
- $\rightarrow$  Add the tuple's unique Record ID as part of the key to ensure that all keys are unique.
- $\rightarrow$  The DBMS can still use partial keys to find tuples.

#### Approach #2: Overflow Leaf Nodes

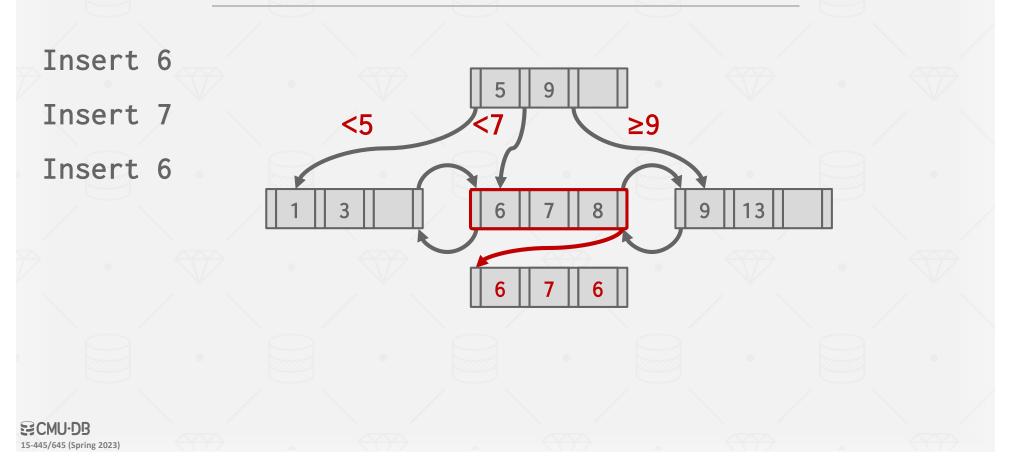
- → Allow leaf nodes to spill into overflow nodes that contain the duplicate keys.
- $\rightarrow$  This is more complex to maintain and modify.

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#### **B+TREE - APPEND RECORD ID**



#### **B+TREE – OVERFLOW LEAF NODES**



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#### **CLUSTERED INDEXES**

The table is stored in the sort order specified by the primary key.

 $\rightarrow$  Can be either heap- or index-organized storage.

Some DBMSs always use a clustered index.
→ If a table does not contain a primary key, the DBMS will automatically make a hidden primary key.

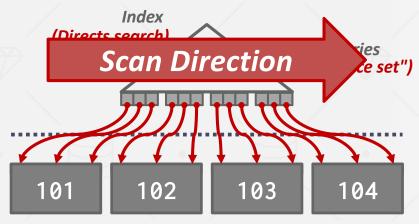
Other DBMSs cannot use them at all.

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#### **CLUSTERED B+TREE**

Traverse to the left-most leaf page and then retrieve tuples from all leaf pages.

This will always be better than sorting data for each query.



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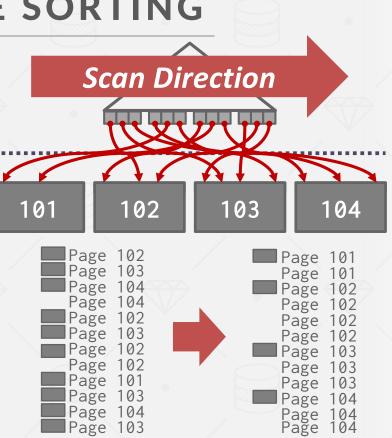
Table Pages

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#### **INDEX SCAN PAGE SORTING**

Retrieving tuples in the order they appear in a non-clustered index is inefficient due to redundant reads.

The DBMS can first figure out all the tuples that it needs and then sort them based on their Page ID.



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#### **B+TREE DESIGN CHOICES**

Node Size Merge Threshold Variable-Length Keys Intra-Node Search Foundations and Trends<sup>®</sup> In Databases 3:4

#### **Modern B-Tree Techniques**

Goelz Graefe

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#### NODE SIZE

The slower the storage device, the larger the optimal node size for a B+Tree.

- $\rightarrow$  HDD: ~1MB
- $\rightarrow$  SSD: ~10KB
- $\rightarrow$  In-Memory: ~512B

Optimal sizes can vary depending on the workload  $\rightarrow$  Leaf Node Scans vs. Root-to-Leaf Traversals

#### **MERGE THRESHOLD**

Some DBMSs do not always merge nodes when they are half full.

Delaying a merge operation may reduce the amount of reorganization.

It may also be better to just let smaller nodes exist and then periodically rebuild entire tree.

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# VARIABLE-LENGTH KEYS

#### **Approach #1: Pointers**

 $\rightarrow$  Store the keys as pointers to the tuple's attribute.

#### Approach #2: Variable-Length Nodes

- $\rightarrow$  The size of each node in the index can vary.
- $\rightarrow$  Requires careful memory management.

#### Approach #3: Padding

 $\rightarrow$  Always pad the key to be max length of the key type.

#### Approach #4: Key Map / Indirection

→ Embed an array of pointers that map to the key + value list within the node.

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# **INTRA-NODE SEARCH**

#### Approach #1: Linear

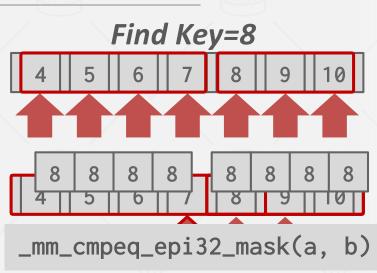
→ Scan node keys from beginning to end.
→ Use SIMD to vectorize comparisons.

#### Approach #2: Binary

→ Jump to middle key, pivot left/right depending on comparison.

#### **Approach #3: Interpolation**

→ Approximate location of desired key based on known distribution of keys.



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# NEXT TIME

#### B+Tree Optimizations Index Concurrency Control