Carnegie Mellon University Database Systems Bloom Filters, Tries, Skip Lists, Inverted Indexes, Vector Indexes

15-445/645 SPRING 2025 » PROF. JIGNESH PATEL

ADMINISTRIVIA

Project #2 out; due Sunday March 2nd @ 11:59pm

- \rightarrow Don't forget to do a GitHub "pull" before starting
- \rightarrow Recitation on Wednesday Feb. 19 4:00-5:00 pm, GHC 5117

Homework #3 (indices and filters) due Sunday Feb 23th @11:59pm

Mid-term Exam on Wednesday Feb 26^{th} \rightarrow In-class in this room



INDEXES VS. FILTERS

An <u>index</u> data structure of a subset of a table's attributes that are organized and/or sorted to the location of specific tuples using those attributes. \rightarrow Example: B+Tree

A <u>filter</u> is a data structure that answers set membership queries; it tells you whether a key (likely) exists in a set but <u>not</u> where it is located. \rightarrow Example: Bloom Filter

TODAY'S AGENDA

Bloom Filters Skip Lists Tries / Radix Trees Inverted Indexes Vector Indexes **DB Flash Talk: <u>Weaviate</u>**



Probabilistic data structure (bitmap) that answers set membership queries.

- \rightarrow False negatives will never occur.
- \rightarrow False positives can sometimes occur.
- \rightarrow See <u>Bloom Filter Calculator</u>.

Insert(x):

 \rightarrow Use *k* hash functions to set bits in the filter to 1.

Lookup(x):

 \rightarrow Check whether the bits are 1 for each hash function.

Insert 'RZA'

0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0



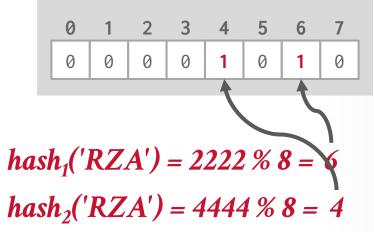
Insert 'RZA'

Bloom Filter

0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0

 $hash_1('RZA') = 2222 \% 8 = 6$ $hash_2('RZA') = 4444 \% 8 = 4$

Insert 'RZA'





Insert 'RZA'

Insert 'GZA'

Bloom Filter

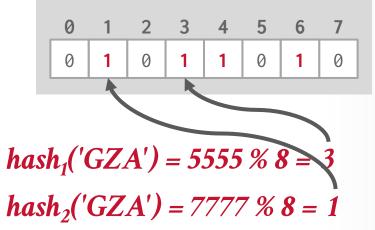
0	1	2	3	4	5	6	7
0	0	0	0	1	0	1	0

hash₁('GZA') = 5555 % 8 = 3 hash₂('GZA') = 7777 % 8 = 1



Insert 'RZA'

Insert 'GZA'

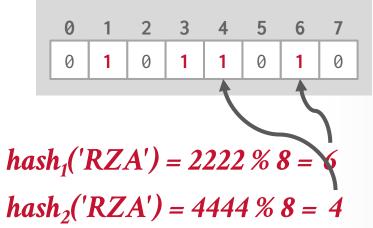




Insert 'RZA'

Insert 'GZA'

Lookup 'RZA'

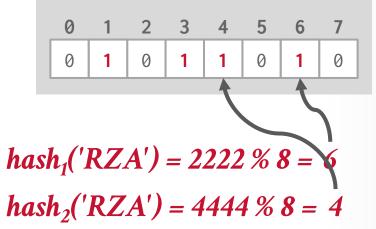




Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' \rightarrow *TRUE*



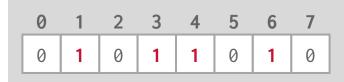


Insert 'RZA'

Insert 'GZA'

Lookup 'RZA'→*TRUE*

Lookup 'Raekwon'





Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' \rightarrow *TRUE*

Lookup 'Raekwon'

Bloom Filter



hash₁('Raekwon') = 3333 % 8 = 5 hash₂('Raekwon') = 8899 % 8 = 3

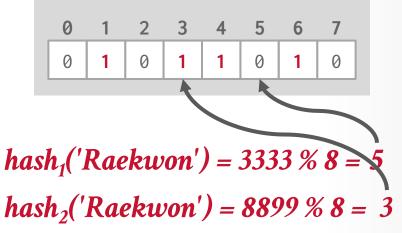


Insert 'RZA'

Insert 'GZA'

Lookup 'RZA'→*TRUE*

Lookup 'Raekwon'



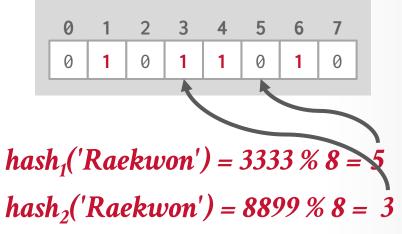


Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' → *TRUE*

Lookup 'Raekwon' \rightarrow FALSE



Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' \rightarrow *TRUE*

Lookup 'Raekwon'→ *FALSE*



Insert 'RZA'

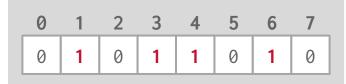
Insert 'GZA'

Lookup 'RZA' → *TRUE*

Lookup 'Raekwon' \rightarrow FALSE

Lookup 'ODB'

Bloom Filter



 $hash_1('ODB') = 6699 \% 8 = 3$ $hash_2('ODB') = 9966 \% 8 = 6$



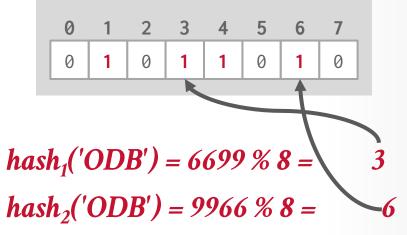
Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' → *TRUE*

Lookup 'Raekwon'→ FALSE

Lookup 'ODB'





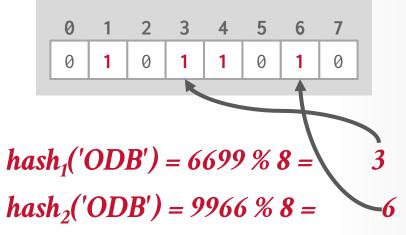
Insert 'RZA'

Insert 'GZA'

Lookup 'RZA' \rightarrow *TRUE*

Lookup 'Raekwon' \rightarrow FALSE

Lookup 'ODB' $\rightarrow TRUE$





Insert 'RZA'

Insert 'GZA'

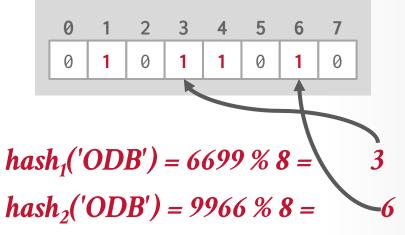
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Lookup 'RZA' → *TRUE*

Lookup 'Raekwon' \rightarrow FALSE

Lookup 'ODB' $\rightarrow TRUE$

Bloom Filter



Bloomfilter calculator: <u>https://hur.st/bloomfilter/</u>

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OTHER FILTERS

Counting Bloom Filter

- \rightarrow Supports dynamically adding and removing keys.
- \rightarrow Uses integers instead of bits to count the number of occurrences of a key in a set.

Cuckoo Filter

- \rightarrow Also supports dynamically adding and removing keys.
- \rightarrow Uses a Cuckoo Hash Table but stores <u>fingerprints</u> instead of full keys.

Succinct Range Filter (SuRF)

 \rightarrow Immutable compact trie that supports approximate exact matches and range filtering.

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Carnegie Mellon

University

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S2CMU-DB 15-445/645 (Spring 2025) Succinct Range Filter (S

 \rightarrow Immutable compact trie tha matches and range filtering

Develop with Redis	Docs → Develop w
Quick starts	Cuck
Connect	CUCK
Understand data types	Cuckoo filters are
Strings	
JSON	A Cuckoo filter, ju enables you to ch
Lists	while also allowing
Sets	scenarios.
Hashes	While the Bloom fi
Sorted sets	Cuckoo filter is an
Streams	positions decided possible buckets for
Geospatial	cuckoo filter's finge
Bitmaps	
Bitfields	
Probabilistic	Use cases
HyperLogLog	
Bloom filter	Targeted ad campa
Cuckoo filter	This application ans
t-digest	Use a Cuckoo filter f
Тор-К	user id is checked ag
Count-min sketch	
Configuration	 If yes, the user h If the user clicks
Time series	 If no, the user has
Interact with data	Discount code/coup
libraries and tools	
	This application answ
ledis products	Use a Cuckoo filter po is checked against the
ommands	 If no, the coupon is If yes, the coupon filter as used

rith Redis → Understand Redis data types → Probabilistic → Cuckoo filter

00 filter

a probabilistic data structure that checks for presence of an element in a set

ust like a Bloom filter, is a probabilistic data structure in Redis Stack that teck if an element is present in a set in a very fast and space efficient way, ig for deletions and showing better performance than Bloom in some

ïlter is a bit array with flipped bits at positions decided by the hash function, a array of buckets, storing fingerprints of the values in one of the buckets at by the two hash functions. A membership query for item x searches the or the fingerprint of x, and returns true if an identical fingerprint is found. A erprint size will directly determine the false positive rate

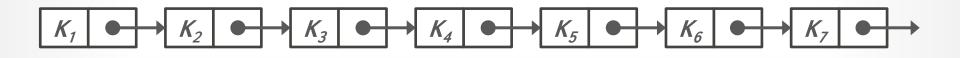
igns (advertising, retail)

wers this question: Has the user signed up for this campaign yet? for every campaign, populated with targeted users' ids. On every visit, the gainst one of the Cuckoo filters. has not signed up for campaign. Show the ad ad and signs up, remove the user id from that Cuckoo filter. as signed up for that campaign. Try the next ad/Cuckoo filter. on validation (retail, online shops) ers this question: Has this discount code/coupon been used yet?

opulated with all discount codes/coupons. On every try, the entered code

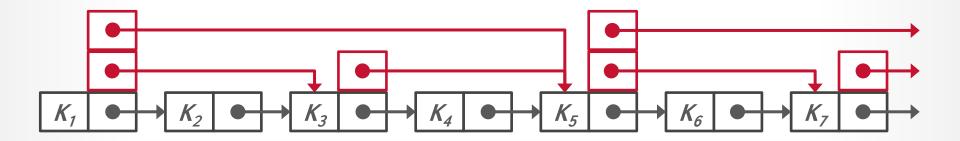
s not valid

can be valid. Check the main database. If valid, remove from Cuckoo









SKIP LISTS

Multiple levels of linked lists with extra pointers to <u>skip</u> over entries.

- \rightarrow 1st level is a sorted list of all keys.
- \rightarrow 2nd level links every other key
- \rightarrow 3rd level links every fourth key
- \rightarrow Each level has $\frac{1}{2}$ the keys of one below it

Maintains keys in sorted order without requiring global rebalancing. \rightarrow Approximate O(log n) search times.

Mostly for in-memory data structures.

 \rightarrow Example: LSM MemTable

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Skip Lists: A Probabilistic Alternative to Balanced Trees

Skip liss are a data structure that can be used in place of balanced trees. Skip liss use probabilistic balancing rather than strictly enforced balancing and as a result the algorithms for insertion and deletion in skip liss are much simpler and significantly faster than equivalent algorithms for balanced trees.

William Pugh

Binary trees can be used for representing abstract data types such a dictionation and ordered lines. They waive will when the elements are intered in a random order. Some sequences of operations, such as intering the elements in order, produce a second strategies and the second strategies and the it waves possible to randomly permute the list of items to be in a randomly permute will with high photohylify for any input sequence. In most cases queries must be answered on-line, a randomly permute ble pingt is impractical. Notice of the maintain term balance conclusions and assume popularity matter.

Skip fairs are a probabilistic alternative to balanced trees. Skip fais are alterative by cosmiling a random moder generator. Allowing halp lists have bad worse case performance the strength of the strength of the strength of the strength term randomly. It is very unlikely as key list data strength with the primerary timelish lists and the strength of the randomly. It is very unlikely as key list data strength with the strength of the strength strength of the strength of the strength of the strength strength of the strength of the strength of the strength strength of the strength of the strength of the strength strength of the strength

Balancing a data structure probabilistically is easier than explicitly maintaining the balance. For many applications, skip latis are a more natural representation than trees, also leading to simple apportnm. The simplicity of skip lat algorithms makes them easier to implement and provides significant content latest producing more thanking the prorate of the simple structure of the simple significant scatter of the simple significant simple significant simple space efficient. They can easily be configured to require an average of 11 yr, jointer per element (or were less) and do and require balance or priority information to be stored with each node.

SKIP LISTS

We might need to examine every node of the list when searching a linked list (Figure 1a). If the list is stored in sorted order and every other node of the list also has a pointer to the node two shead it in the list (Figure 1b), we have to examine no more than $|n^2|$ + 1 nodes (where n is the length of the list). Also giving every fourth node a pointer four shead (Figure 1c) requires that no more famf n/4) + 2 nodes be examined. If every (2^{10} node has a pointer 2^{10} nodes shead (Figure 1d), the number of nodes that must be examined can be reduced to $\log_2 n$ I while only doubling the number of pointers. This data structure could be used for fast searching, but insertion and deletion would be imparcial.

A note that has a ferevater pointern is called a level a node in the recycl $L^{(2)}$ mode in a pointer $L^{(2)}$ scale has due to the level (1) and the recycl (1) and the recycl (1) and the recycl (1) and the recycle (1) and

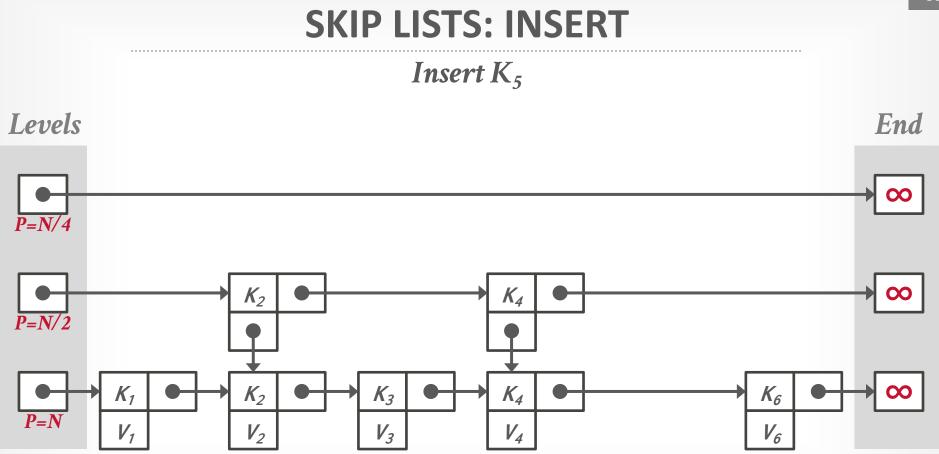
SKIP LIST ALGORITHMS

This section gives algorithms to search for, insert and delete elements in a dictionary or symbol table. The Search operation returns the contents of the value associated with the de sired key or failure if the key is not present. The Insert opera tion associates a specified key with a new value (inserting the key if it had not already been present). The Delete operation deletes the specified key. It is easy to support additional one ations such as "find the minimum key" or "find the next key" Each element is represented by a node, the level of which osen randomly when the node is inserted without regard for the number of elements in the data structure. A level i node has i forward pointers, indexed 1 through i. We do not need to store the level of a node in the node. Levels are capped at some appropriate constant MaxLevel. The level of a list is the maximum level currently in the list (or 1 if the list is empty). The header of a list has forward pointers at levels one through MaxLevel. The forward pointers of the header at levels higher than the current maximum level of the list point

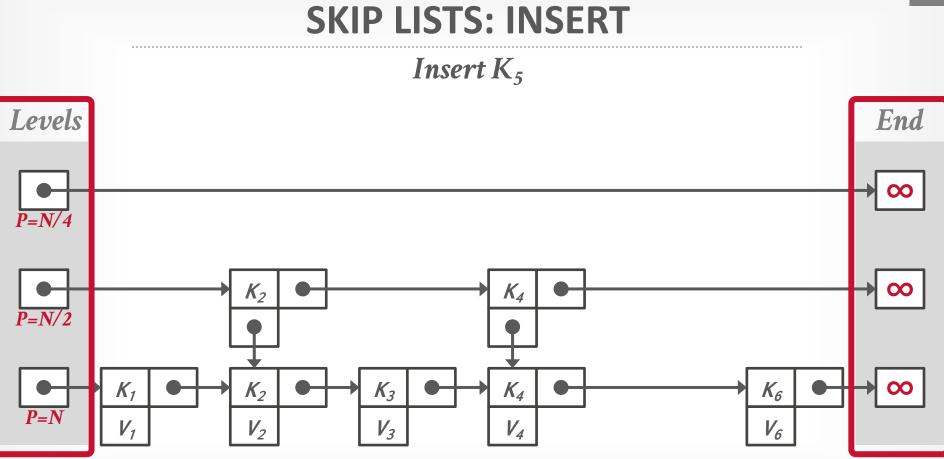


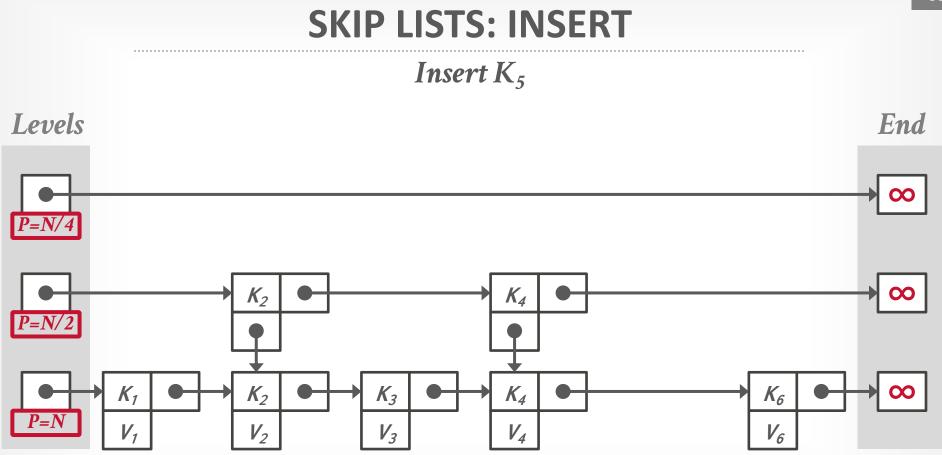


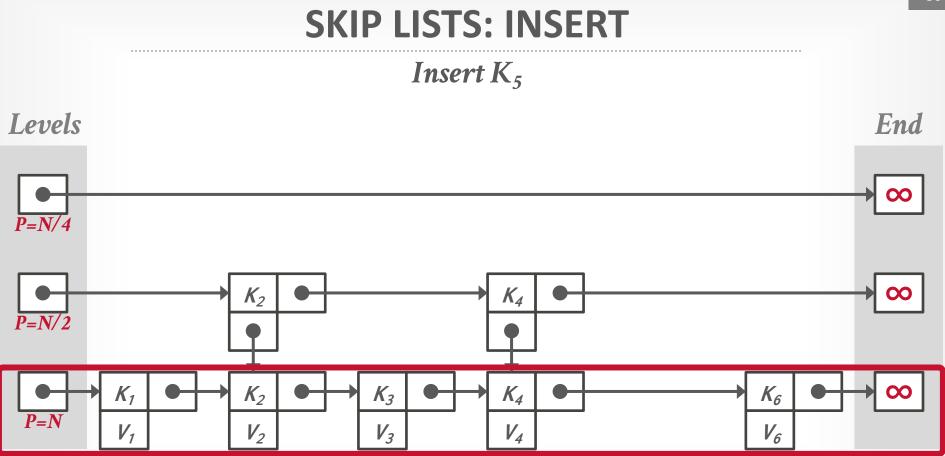
Couchbase

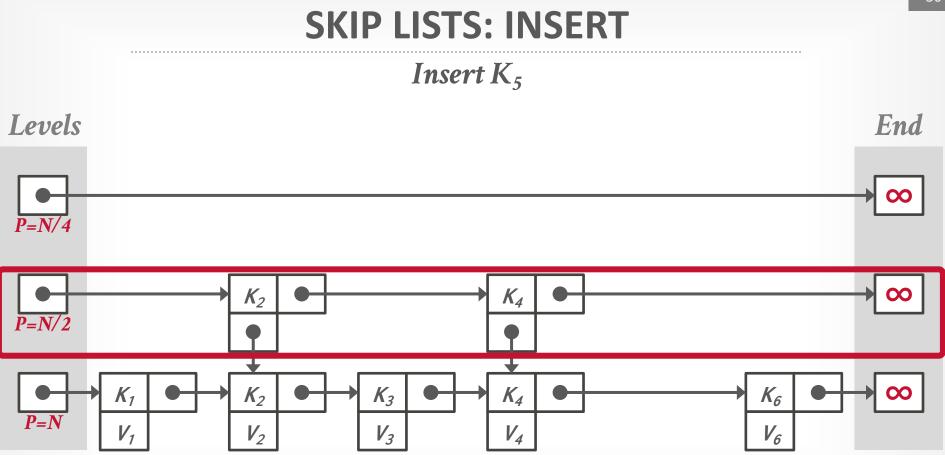


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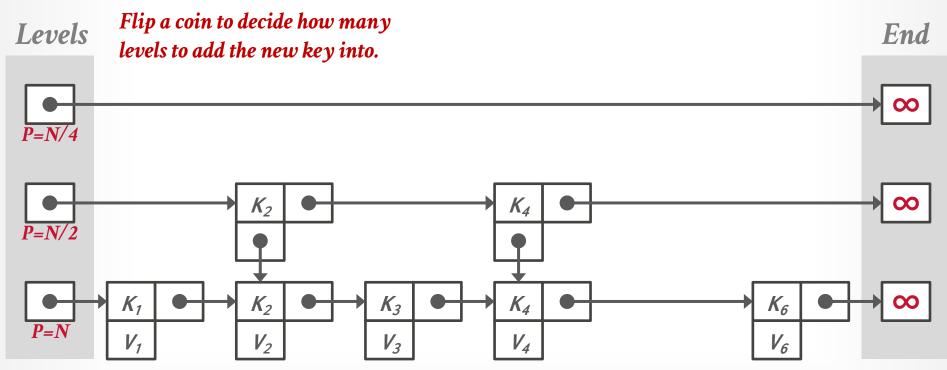


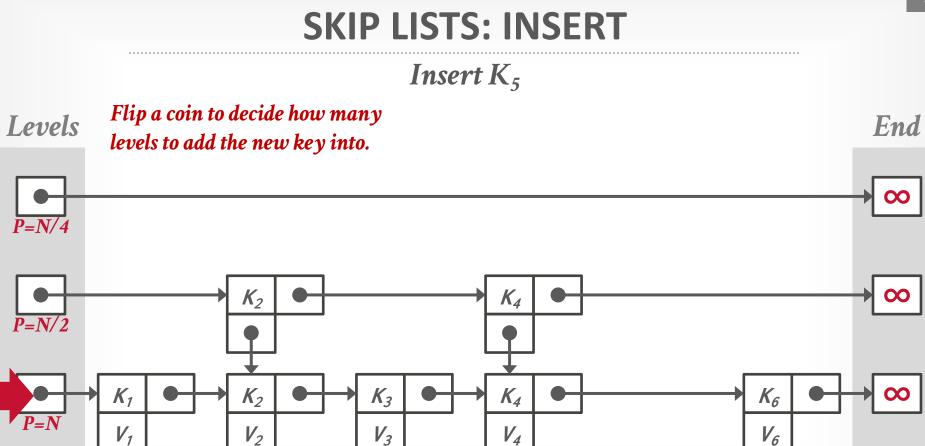


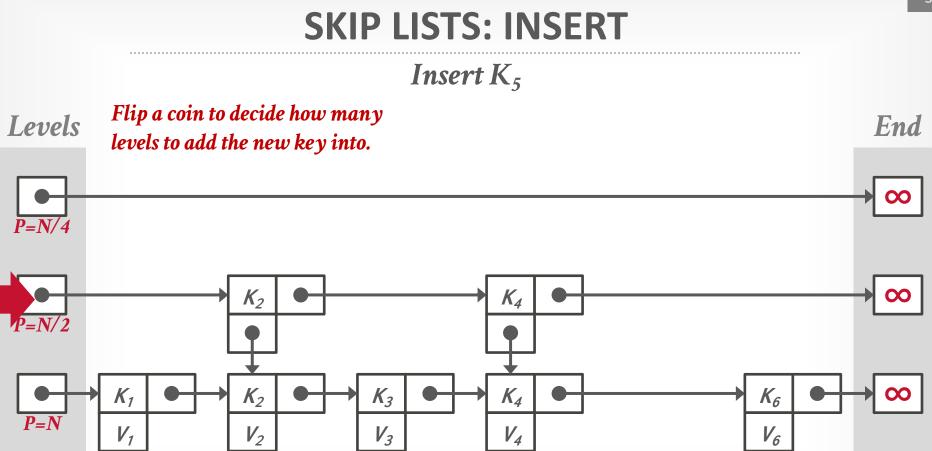


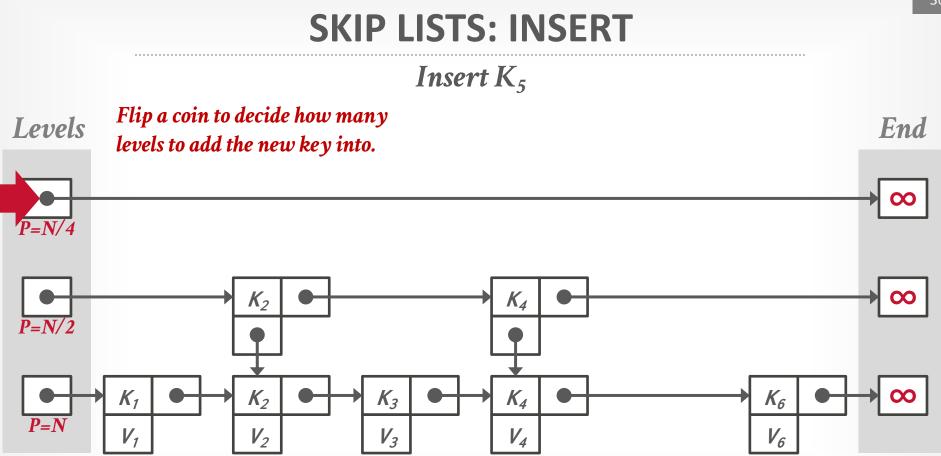
SKIP LISTS: INSERT

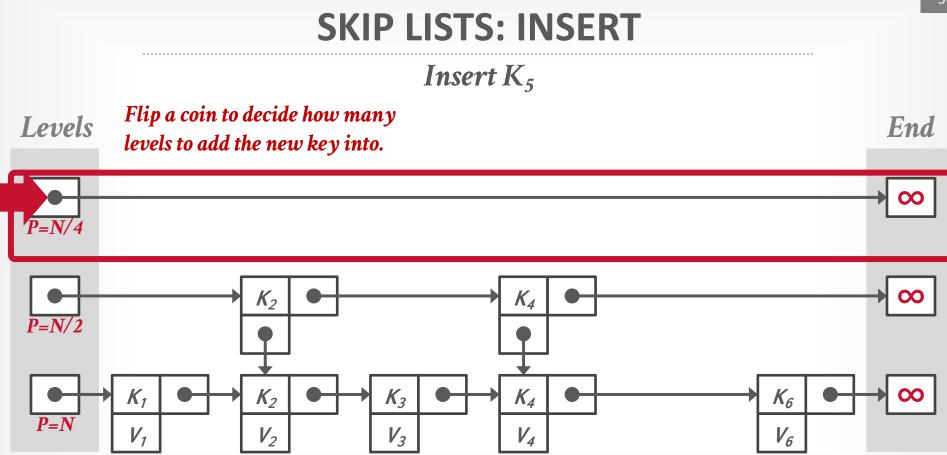
Insert K₅

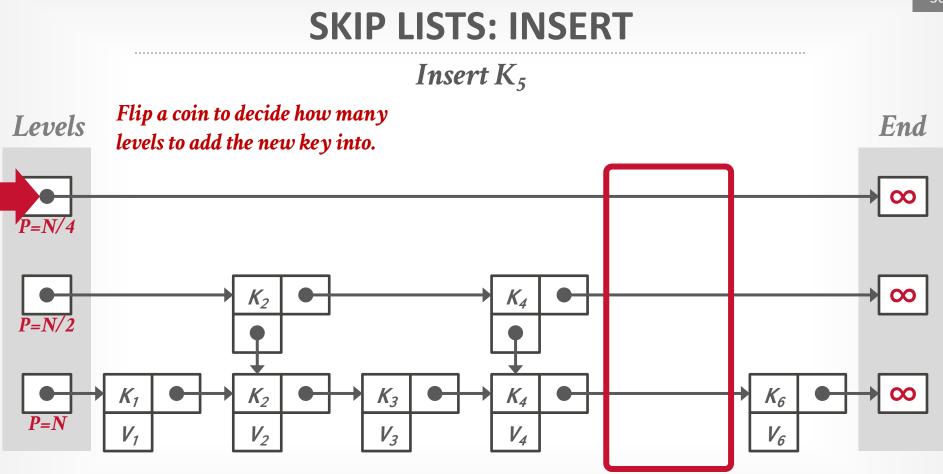


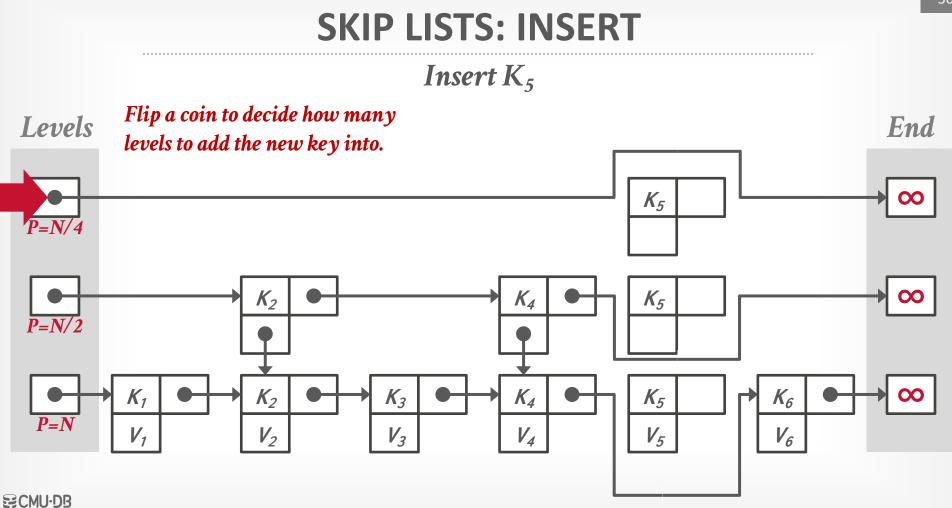


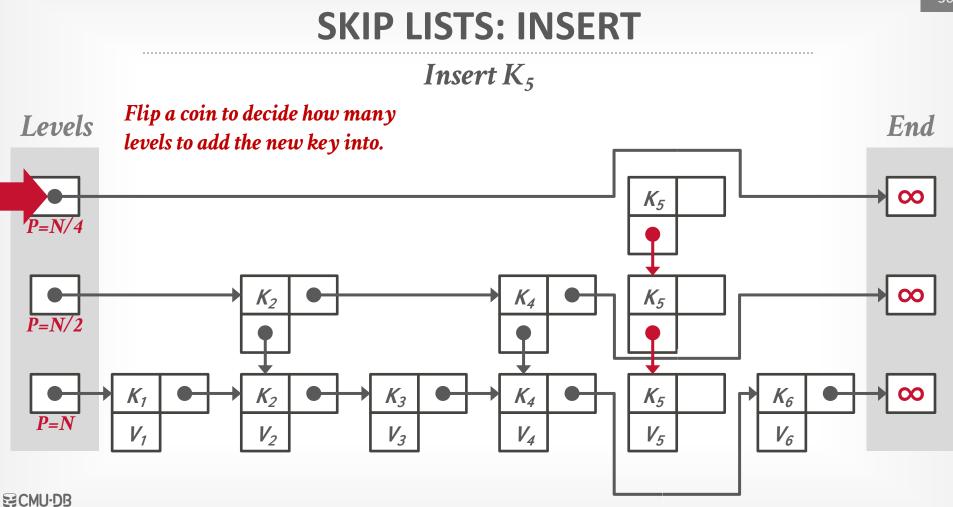


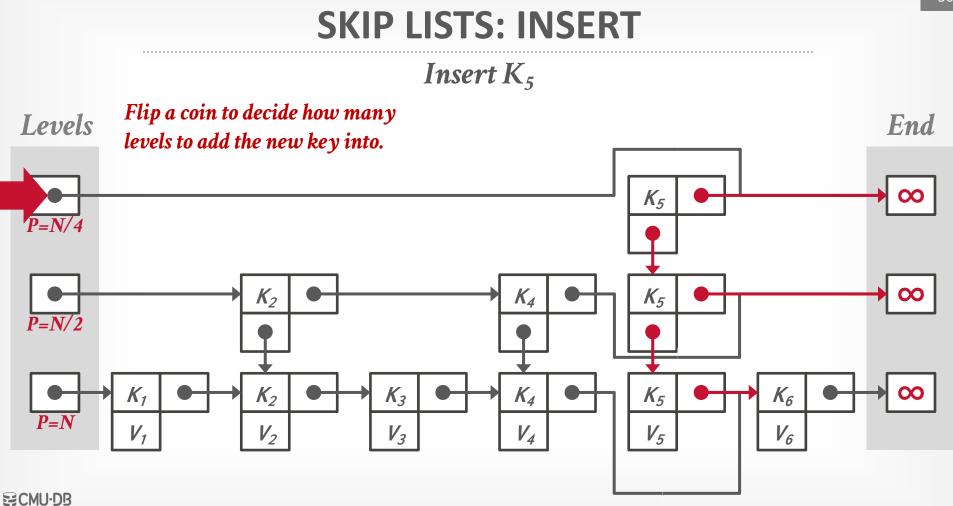


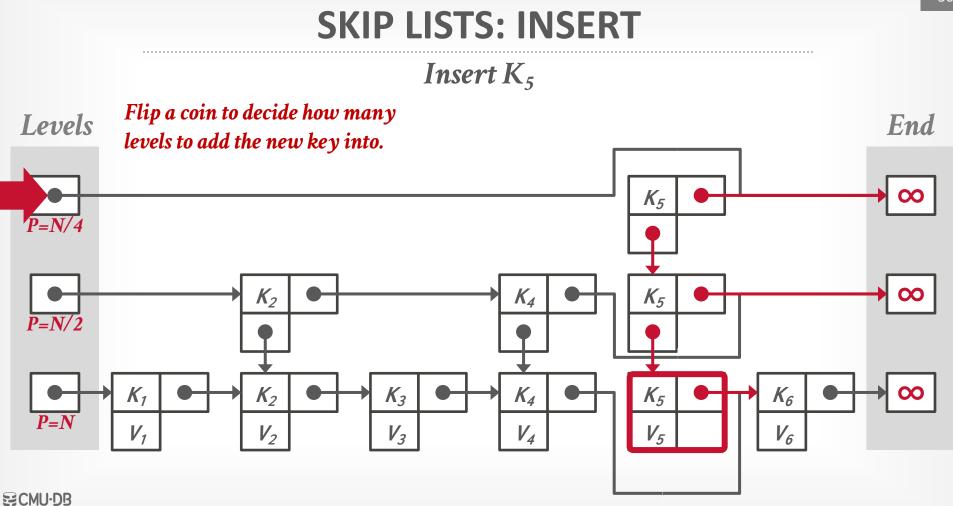


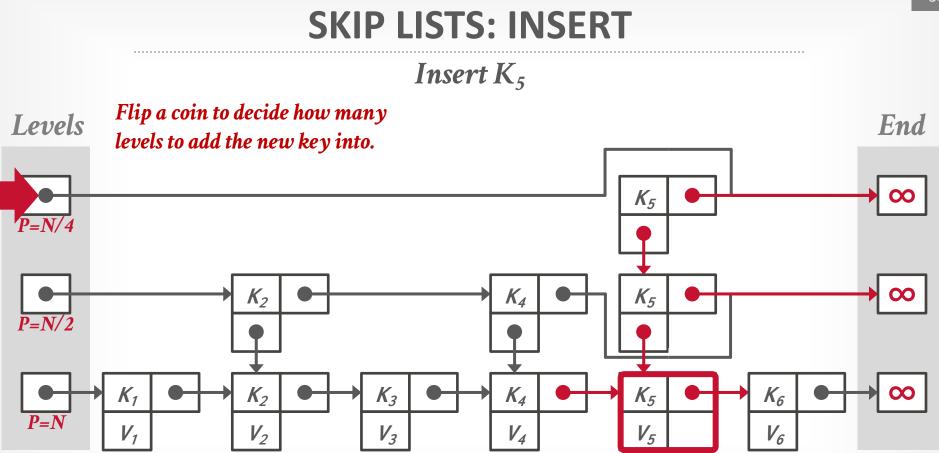


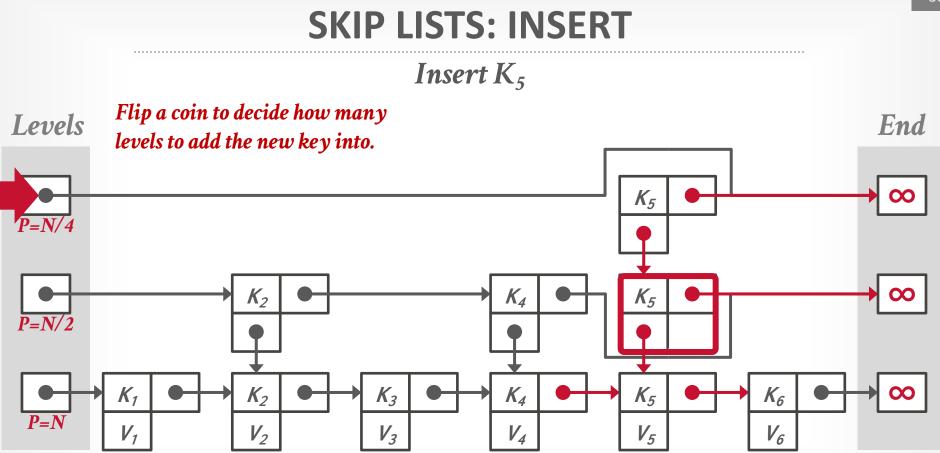


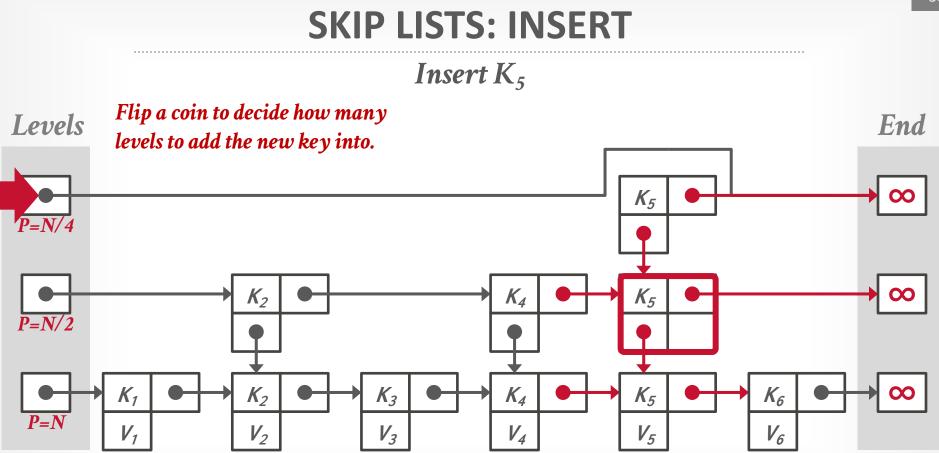


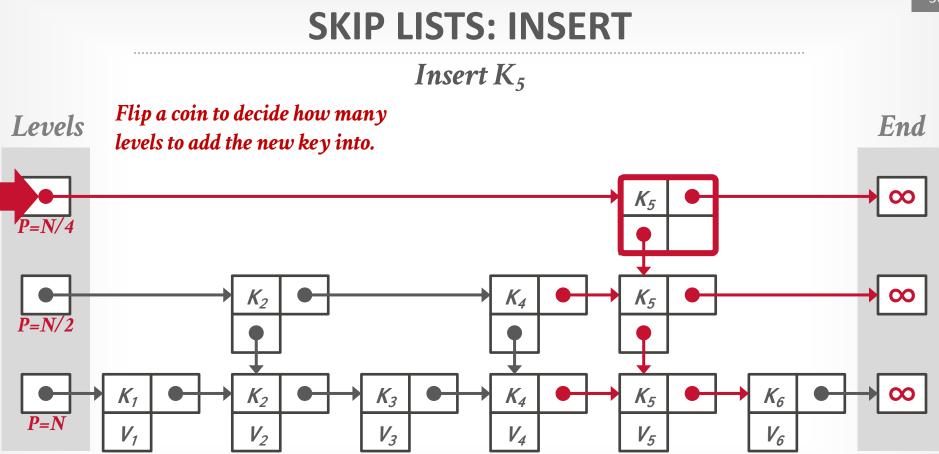


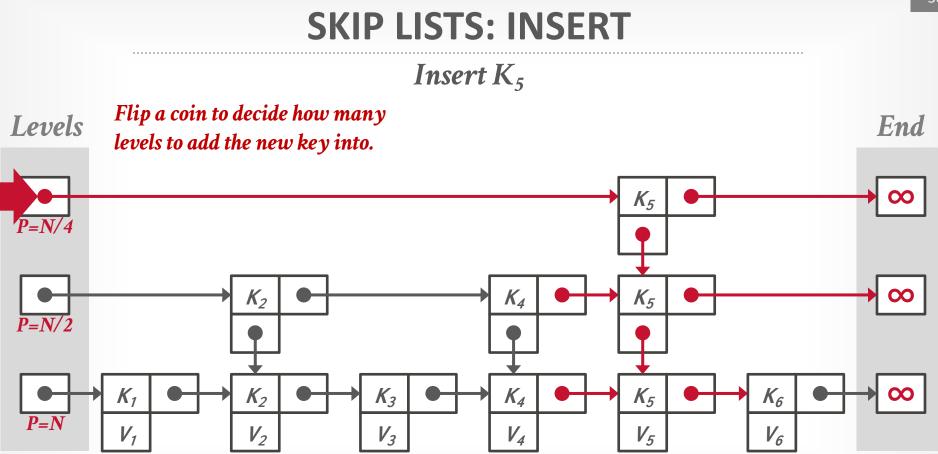


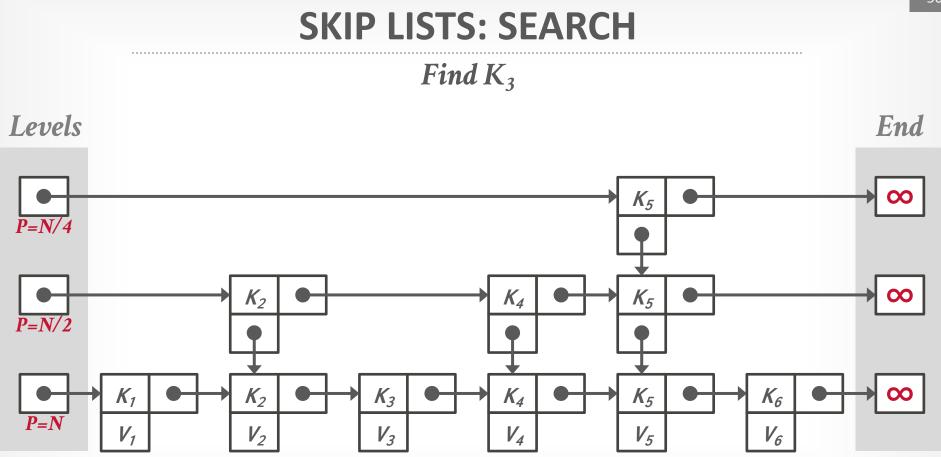


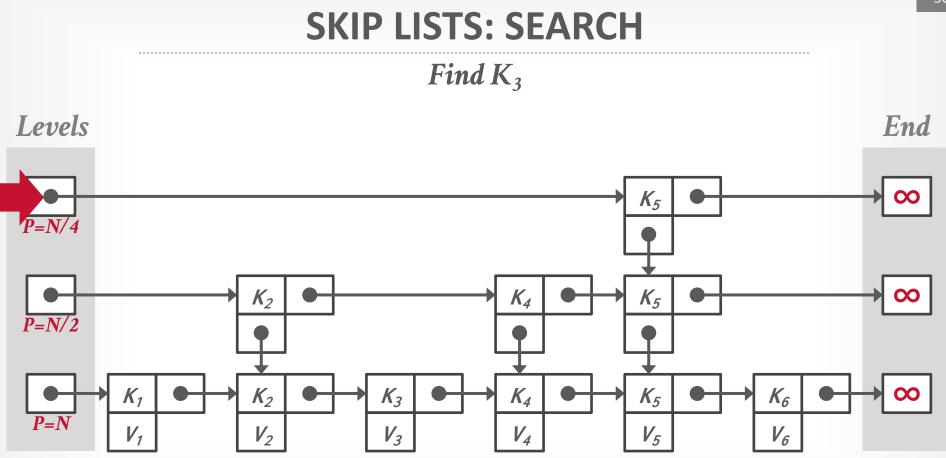


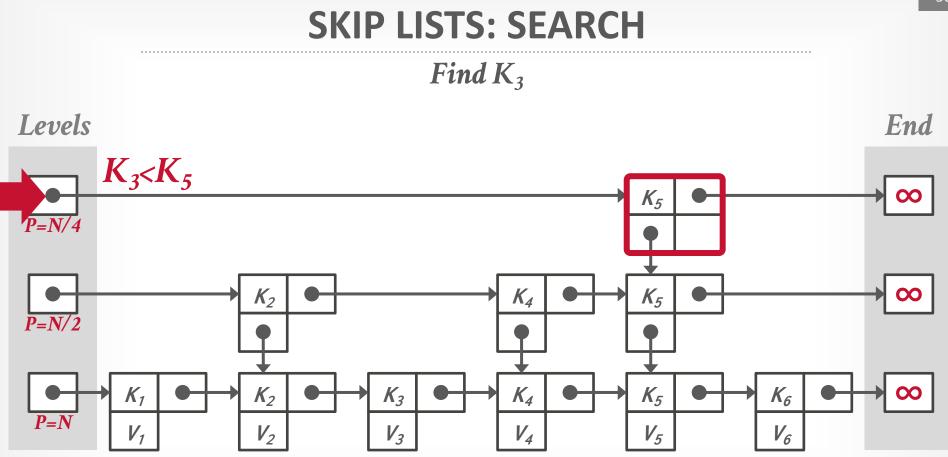


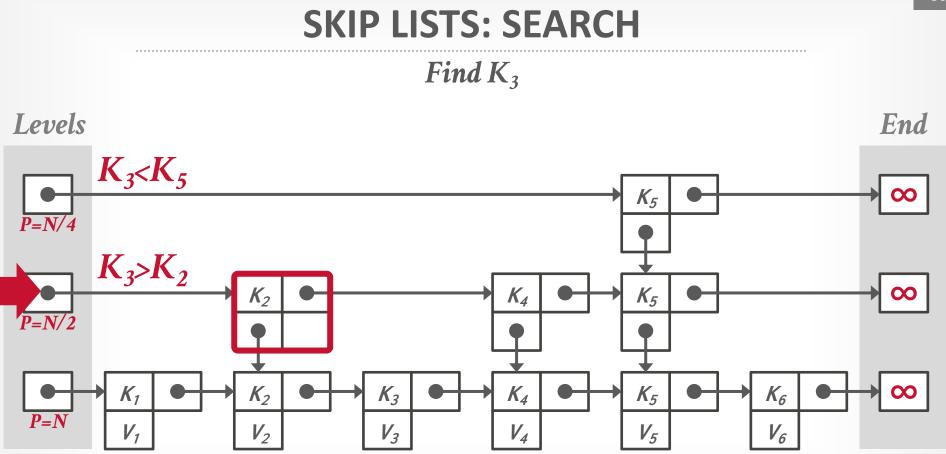


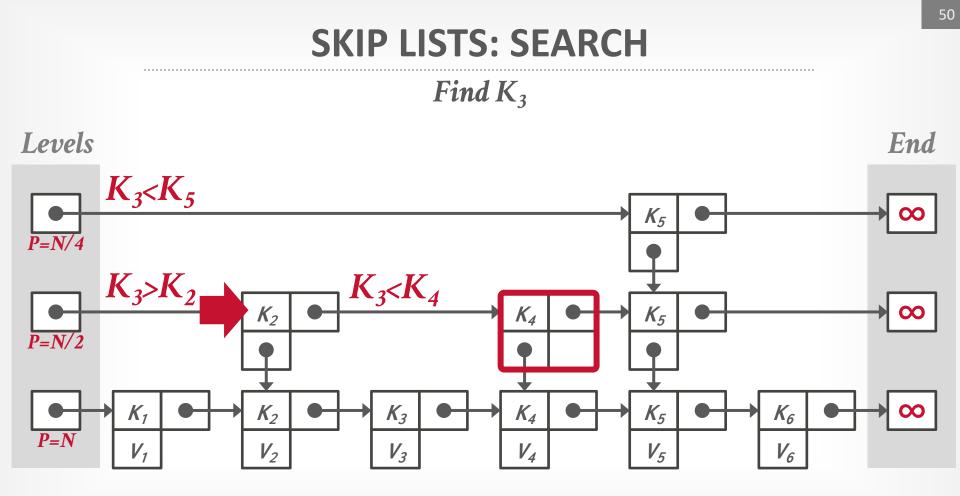


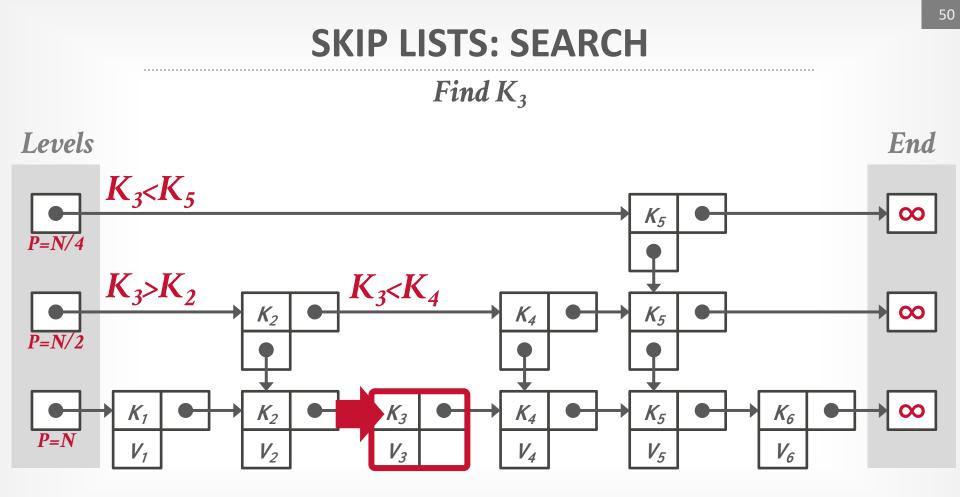










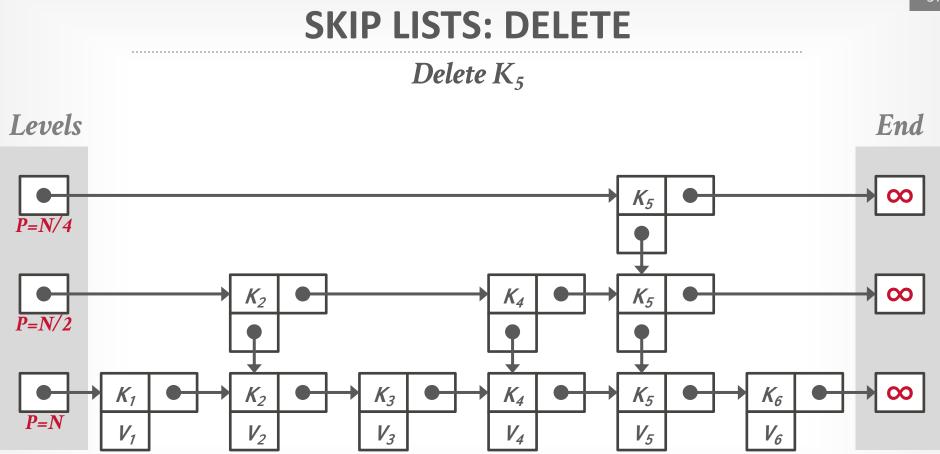


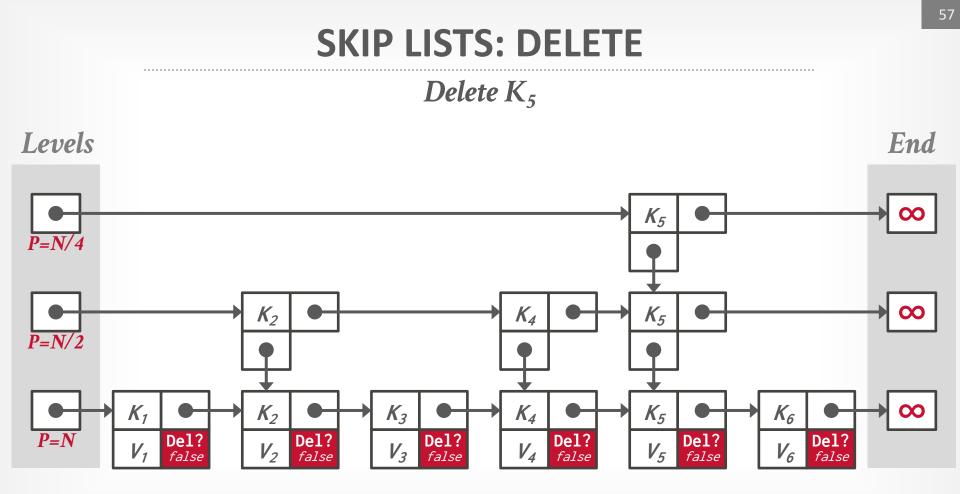
SKIP LISTS: DELETE

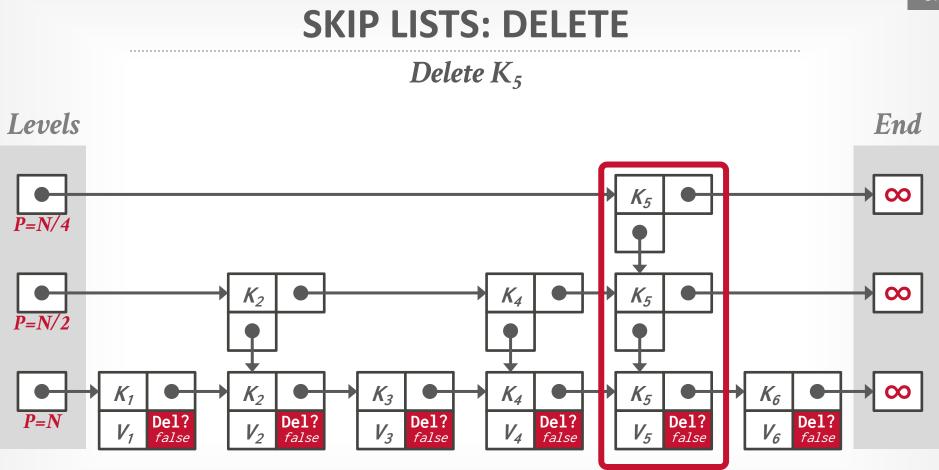
First **logically** remove a key from the index by setting a flag to tell threads to ignore.

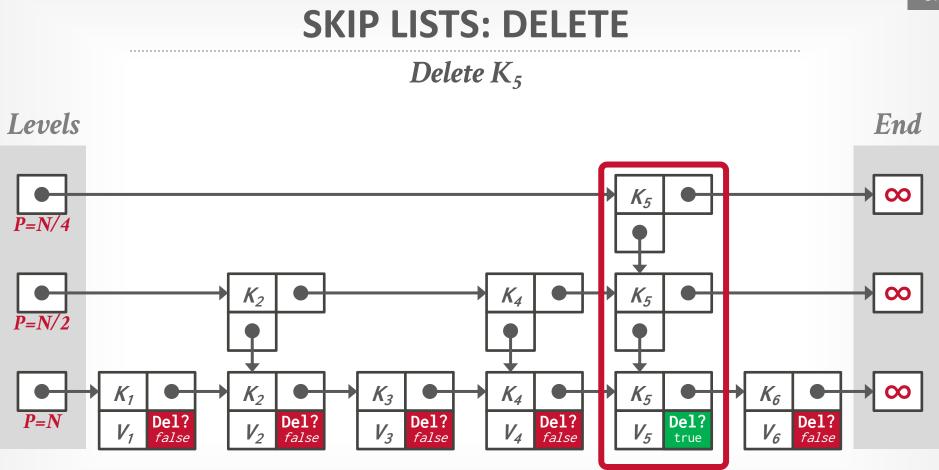
Then **physically** remove the key once we know that no other thread is holding the reference.

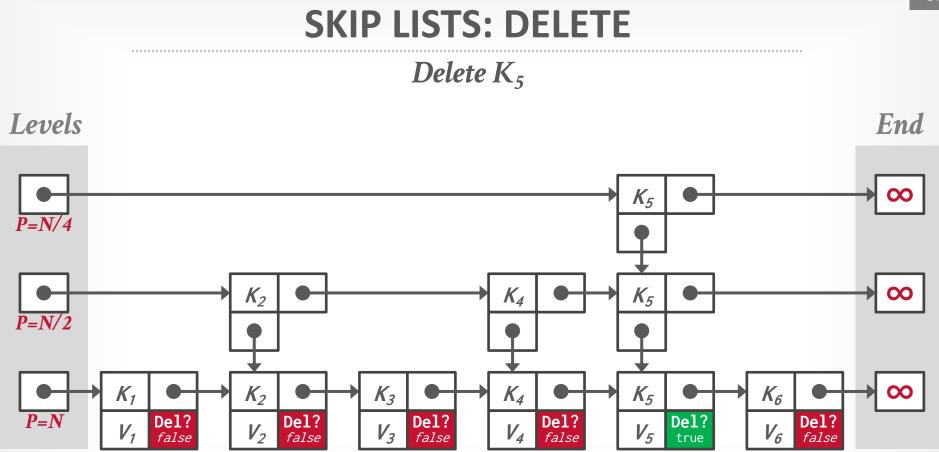


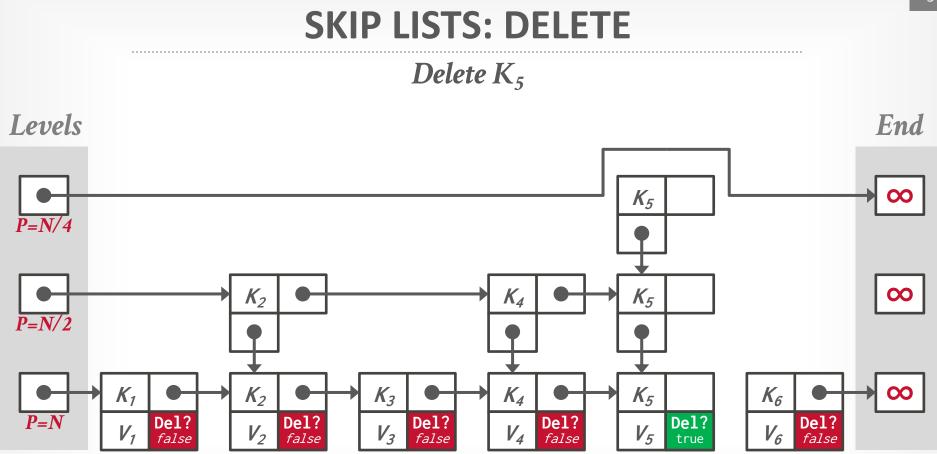


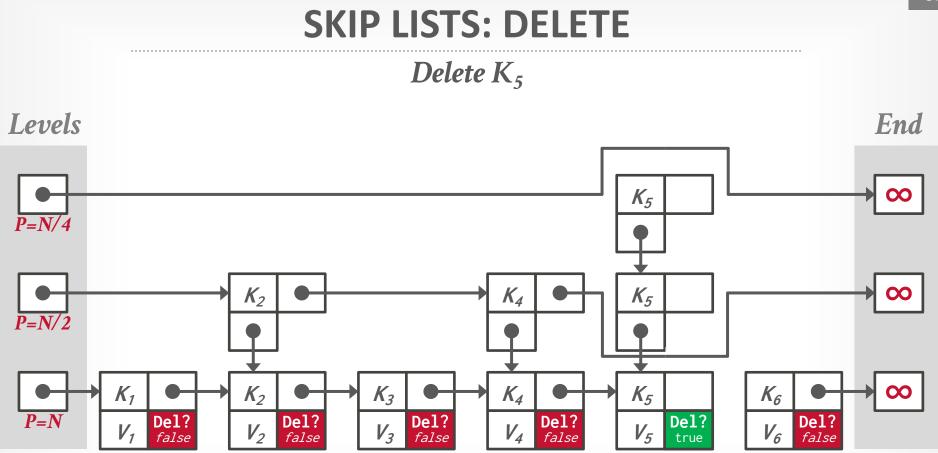


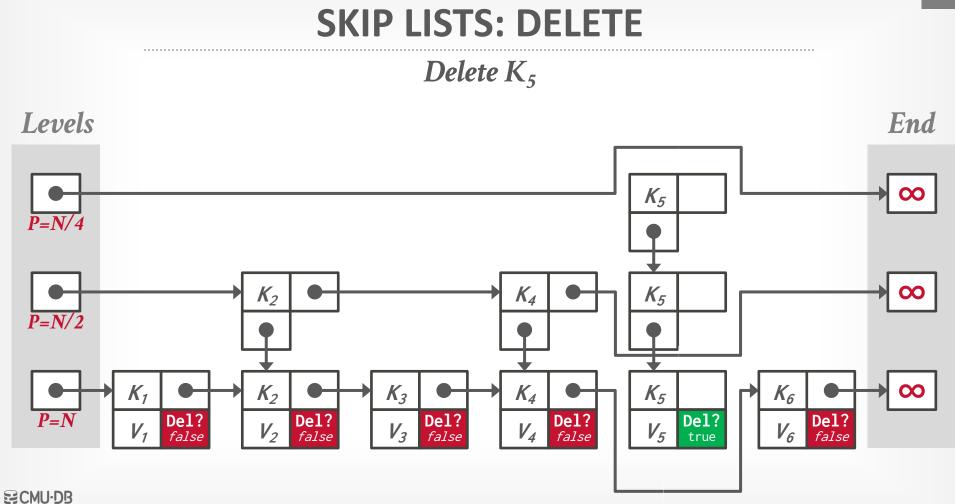


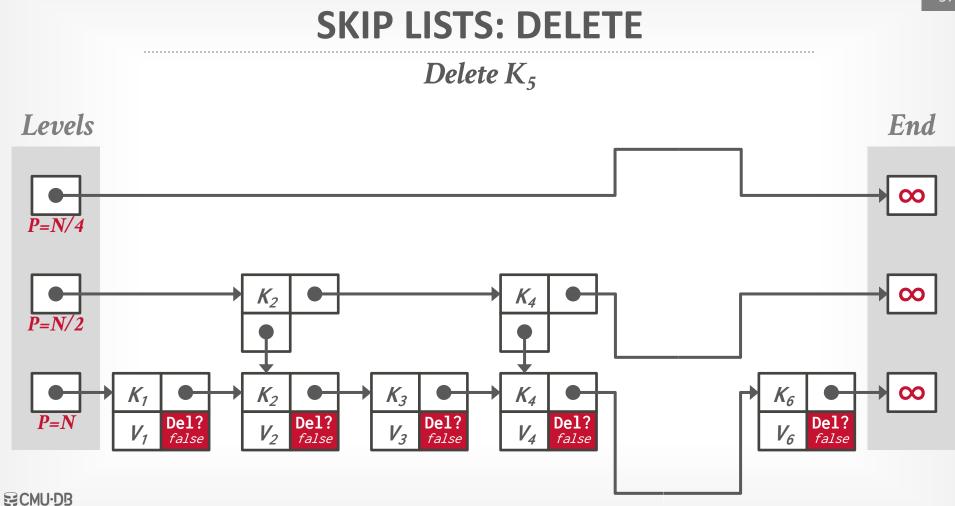












SKIP LISTS

Advantages:

- \rightarrow May use less memory than a B+Tree, if you do <u>not</u> include reverse pointers.
- \rightarrow Insertions and deletions do not require rebalancing.

Disadvantages:

- \rightarrow Not disk/cache friendly because they do not optimize locality of references.
- \rightarrow Reverse search is non-trivial.

OBSERVATION

The inner node keys in a B+Tree cannot tell you whether a key exists in the index. You must always traverse to the leaf node.

This means that you could have (at least) one buffer pool page miss per level in the tree just to find out a key does not exist.

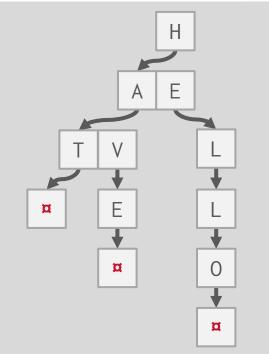
Use a digital representation of keys to examine prefixes one-by-one.

→ aka **Digital Search Tree**, **Prefix Tree**.

Shape depends on keys and lengths.

- \rightarrow Does <u>not</u> depend on existing keys or insertion order.
- \rightarrow Does <u>not</u> require rebalancing operations.
- All operations have **O(k)** complexity where **k** is the length of the key.
- \rightarrow Path to a leaf node represents a key.
- → Keys are stored implicitly and can be reconstructed from paths.

Keys: HELLO, HAT, HAVE

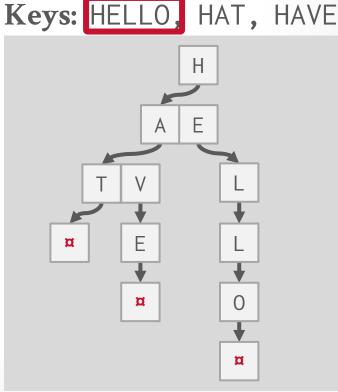


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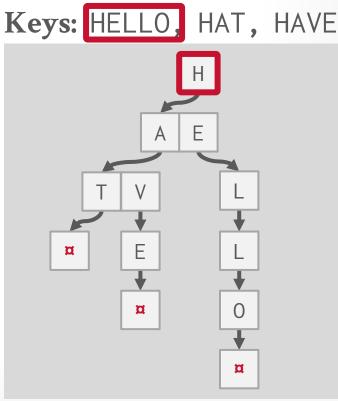
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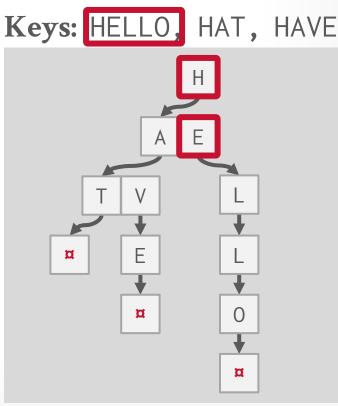
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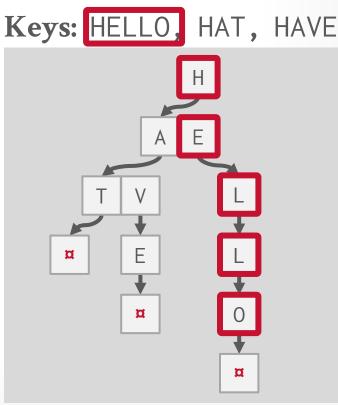
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The **<u>span</u>** of a trie level is the number of bits that each partial key / digit represents.

 \rightarrow If the digit exists in the corpus, then store a pointer to the next level in the trie branch. Otherwise, store null.

This determines the <u>fan-out</u> of each node and the physical <u>height</u> of the tree. $\rightarrow n$ -way Trie = Fan-Out of n

1-bit Span Trie

Keys: K10, K25, K31





1-bit Span Trie

Keys: K10,K25,K31

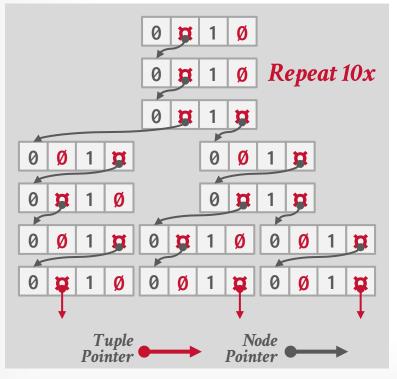
K10→ 00000000 00001010 K25→ 00000000 00011001 K31→ 00000000 00011111





1-bit Span Trie

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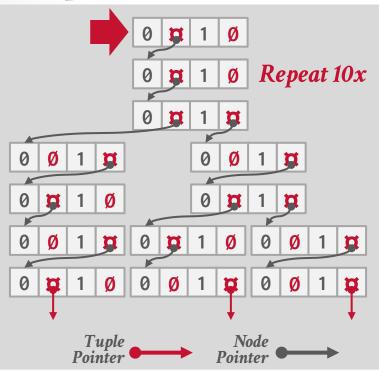


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ECMU-DB 15-445/645 (Spring 2025)

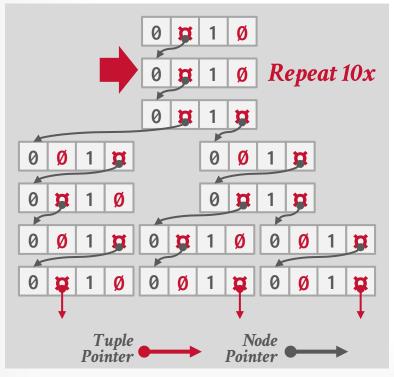


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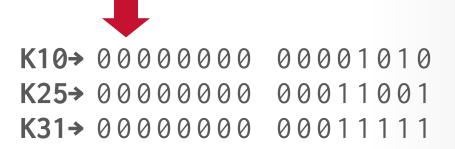
K10→ 0000000 00001010
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ECMU-DB 15-445/645 (Spring 2025)

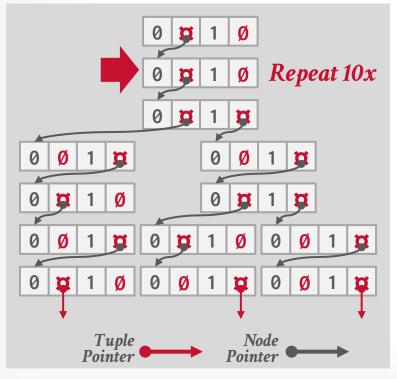


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ECMU-DB 15-445/645 (Spring 2025)

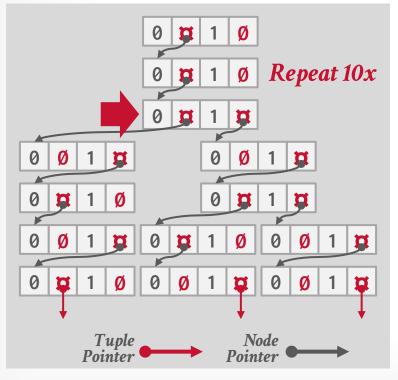


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ECMU-DB 15-445/645 (Spring 2025)

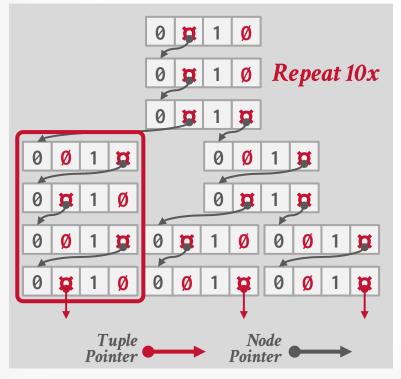




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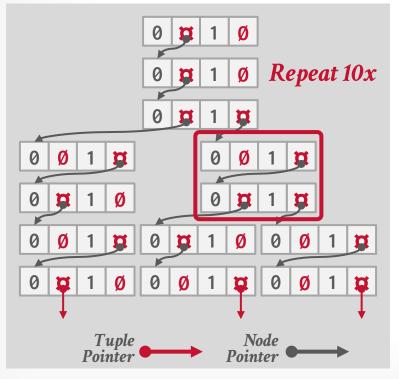


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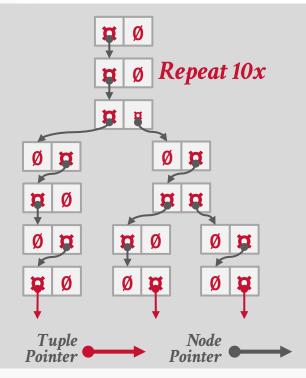


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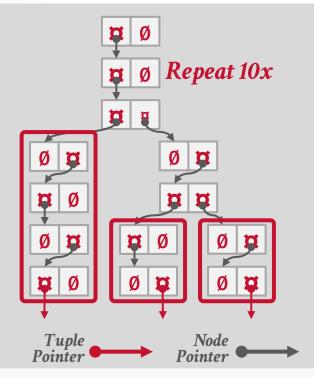


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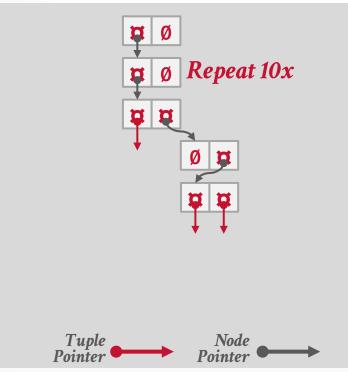
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RADIX TREE

1-bit Span Radix Tree

15-445/645 (Spring 2025)



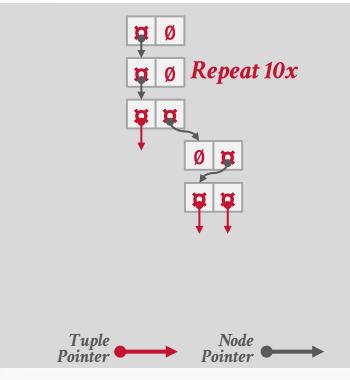
Vertically compressed trie that compacts nodes with a single child. \rightarrow Also known as *Patricia Trie*.

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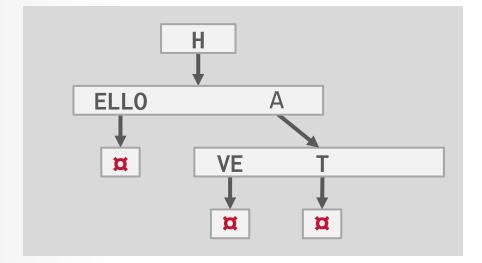
15-445/645 (Spring 2025)



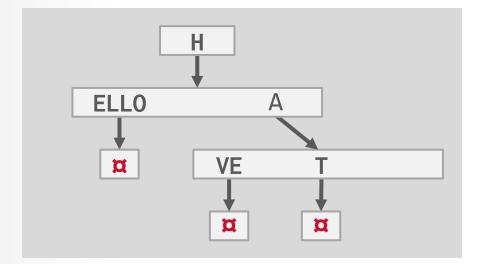
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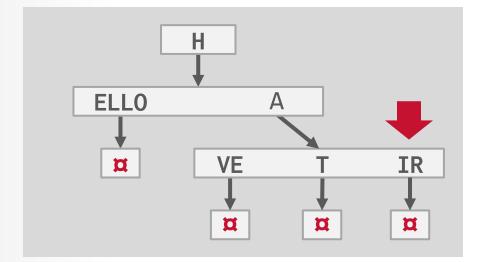




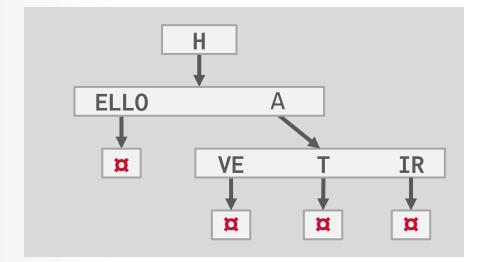




Insert HAIR

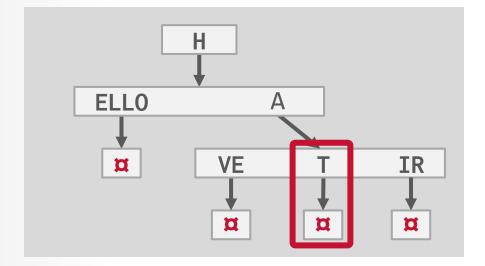


Insert HAIR



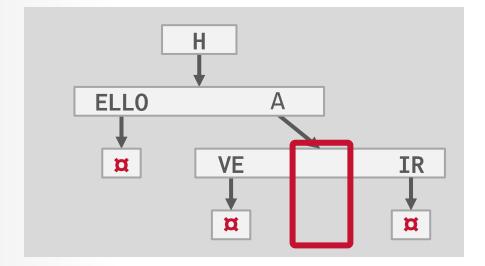
Insert HAIR Delete HAT





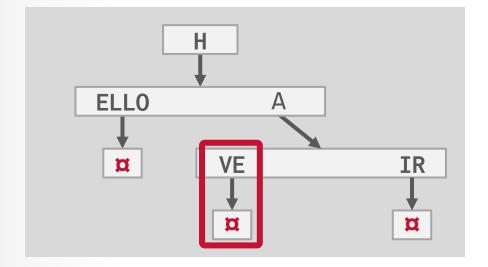
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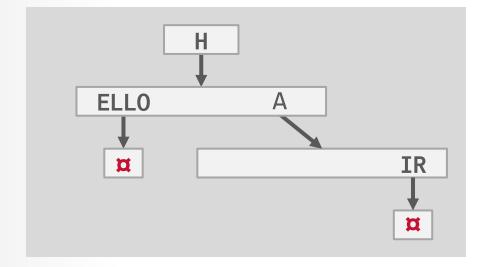


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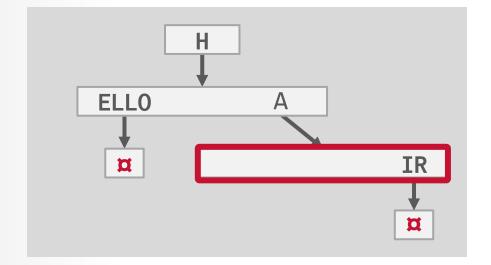




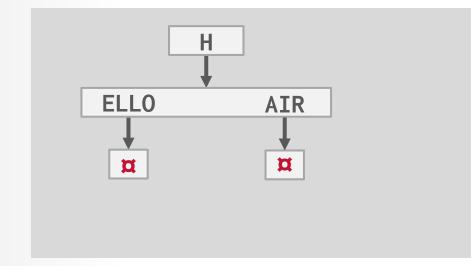












- The indexes that we've discussed are useful for "point" and "range" queries:
- \rightarrow Find all customers in the 15217 zipcode.
- → Find all orders between June 2024 and September 2024.

They are <u>**not**</u> good at keyword searches:

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id	content
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33	In computing, a database is an organized collection of data or a type of data store based on the use of a database management system (DBMS), the software
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revisions(id, content,...)

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CREATE INDEX idx_rev_cntnt
 ON revisions (content);

SELECT pageID FROM revisions
WHERE content LIKE '%Pavlo%';

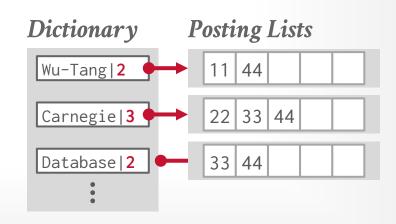
An inverted index stores a mapping of terms to records that contain those terms in the target attribute.
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Many major DBMSs support these natively. But there are also specialized

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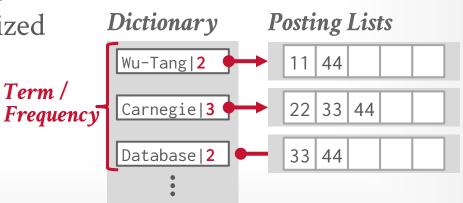
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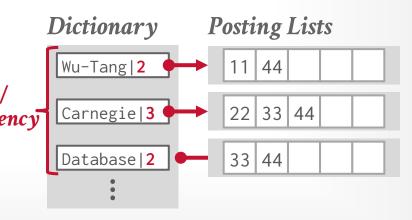
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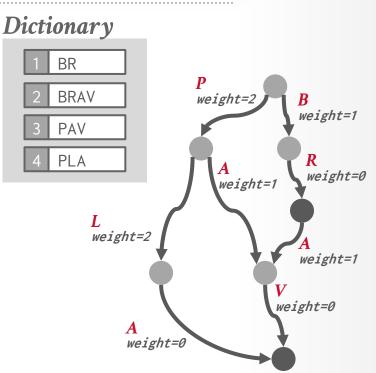
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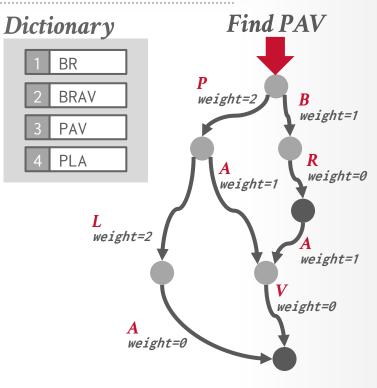
- Uses a **Finite State Transducer** for determining offset of terms in dictionary.
- Incrementally create dictionary segments and then merge them in the background.
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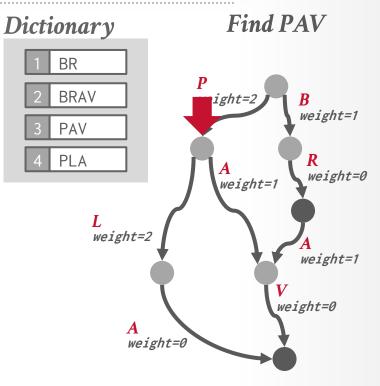


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Offset = 0

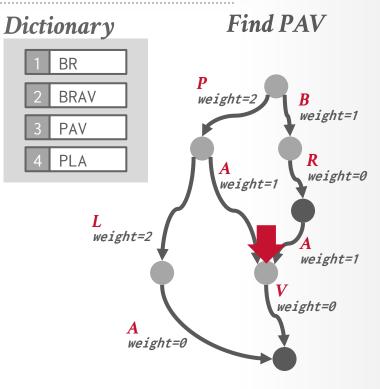
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Offset= 2

INVERTED INDEX: LUCENE

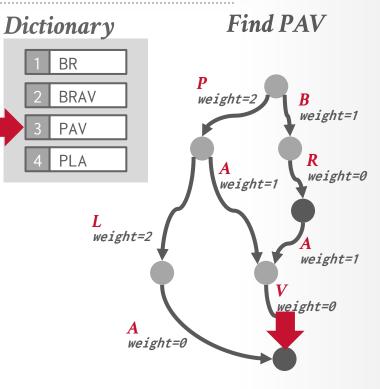
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Offset= 3

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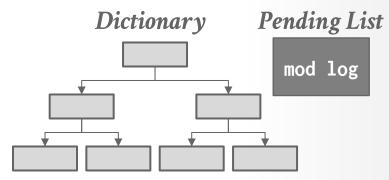


PostgreSQL's <u>Generalized Inverted</u> <u>Index</u> (GIN) uses a B+Tree for the term dictionary that map to a posting list data structure.

Posting list contents varies depending on number of records per term:

- \rightarrow **Few**: Sorted list of record ids.
- \rightarrow **Many**: Another B+Tree of record ids.

Uses a separate "pending list" log to avoid incremental updates.

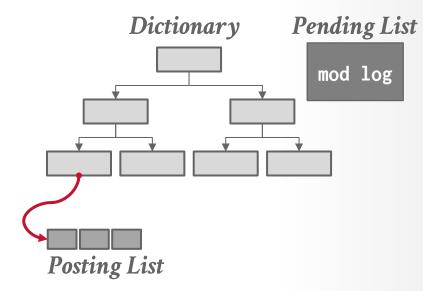


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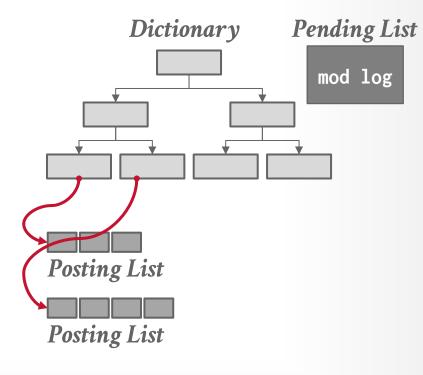
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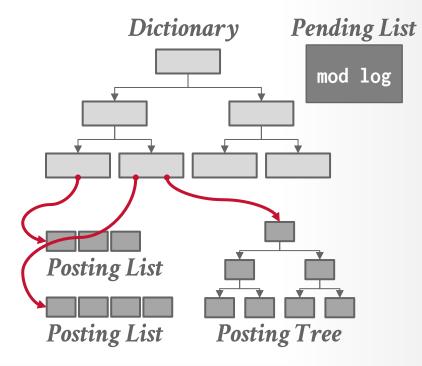


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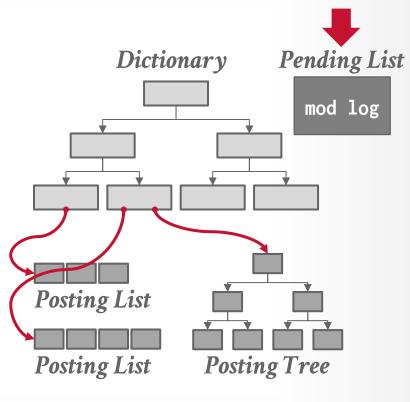
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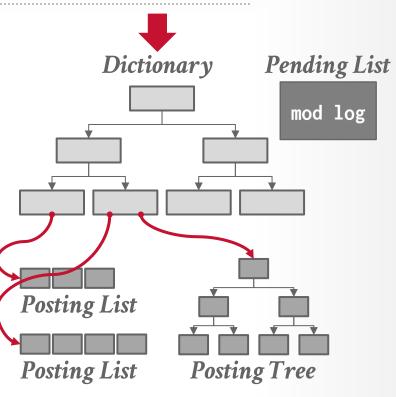
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OBSERVATION

Inverted indexes search data based on its contents.

- → There is a little magic to tweak terms based on linguistic models.
- → Example: Normalization ("Wu-Tang" matches "Wu Tang").

Instead of searching for records containing exact keywords (e.g., "Wu-Tang"), an application may want search for records that are related to topics (e.g., "hip-hop groups with songs about slinging").

VECTOR INDEXES

Specialized data structures to perform nearestneighbor searches on <u>embeddings</u>.

- \rightarrow An embedding is an array of floating point numbers.
- \rightarrow May also need to filter data before / after vector searches.

The correctness of a query depends on whether the result "feels right".



Partition vectors into smaller groups using a clustering algorithm.

To find a match, use same clustering algorithm to map into a group, then scan that group's vectors.

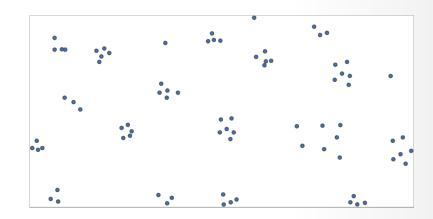
 \rightarrow Also check nearby groups to improve accuracy.

Preprocess / quantize vectors to reduce dimensionality.

Example: **IVFFlat**

Source: Chi Zhang

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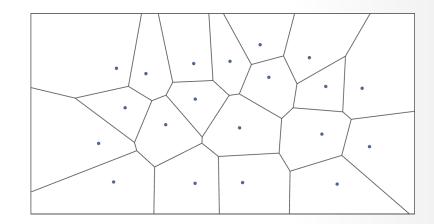
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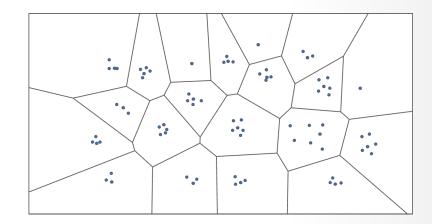
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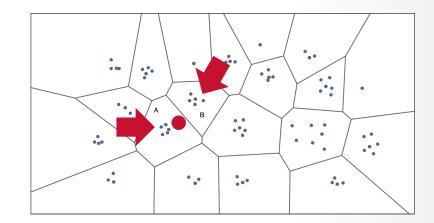
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Source: Chi Zhang CMU-DB 15-445/645 (Spring 2025)

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VECTOR INDEXES: NAVIGABLE SMALL WORLDS

Build a graph where each node represents a vector and it has edges to its *n* nearest neighbors.

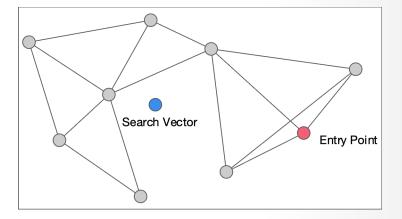
 \rightarrow Can use multiple levels of graphs (<u>HNSW</u>)

To find a match for a given vector, enter the graph and then greedily choose the next edge that moves closer to that vector.

Example: <u>Faiss</u>, <u>hnswlib</u>

Source: Chi Zhang

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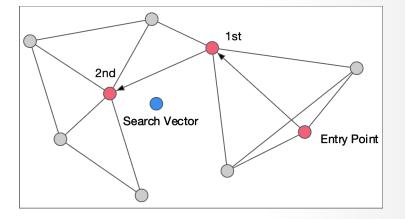
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CONCLUSION

We will see filters again this semester. B+Trees are still the way to go for tree indexes.

Inverted indexes are covered in <u>CMU 11-442</u>.

We did not discuss geo-spatial tree indexes:

- \rightarrow Examples: R-Tree, Quad-Tree, KD-Tree
- \rightarrow This is covered in <u>CMU 15-826</u>.

NEXT CLASS

How to make indexes thread-safe!

