

Carnegie Mellon University

# Database Systems

Query Planning &  
Optimization

15-445/645 SPRING 2025 » PROF. JIGNESH PATEL

# ADMINISTRIVIA

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**Project #3** is due Sunday March 30th @ 11:59pm

→ Recitation: slides, recording.

Mid-term exam:

→ Exam viewing for the next 3 OH, including today.

→ The last OH for exam viewing is on March 24.

# UPCOMING DATABASE TALKS



Mar 17

Lloyd Tabb

Malloy: A Modern Open Source Language for Analyzing, Transforming, and Modeling Data



PRQL

Mar 24

Tobias Brandt

PRQL: Pipelined Relational Query Language



StarRocks

Mar 31

Kaisen Kang

StarRocks Query Optimizer

Oxide

Apr 7

Ben Naecker

OxQL: Oximeter Query Language



MariaDB

Apr 14

Michael Widenius

MariaDB's New Query Optimizer



Apr 21

Michael Sullivan

EdgeQL with Gel

# LAST CLASS

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We talked about how to design the DBMS's architecture to execute queries in parallel.

The query plan is comprised of physical operators that specify the algorithm to invoke at each step of the plan.

**But how do we go from SQL to a query plan?**

# MOTIVATION

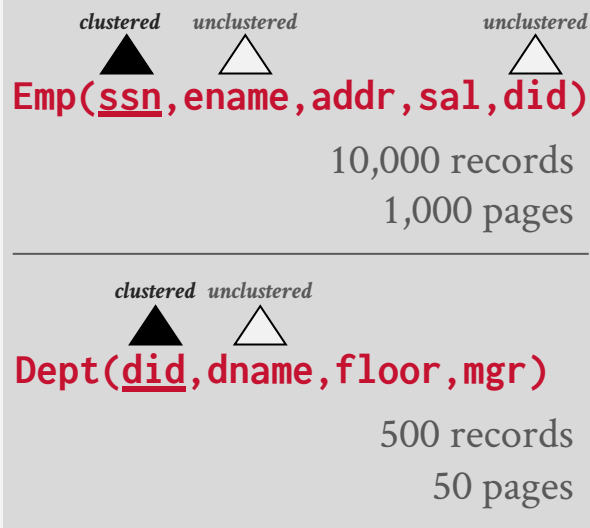
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```
SELECT DISTINCT ename  
  FROM Emp E JOIN Dept D  
    ON E.did = D.did  
 WHERE D.dname = 'Toy'
```

# MOTIVATION

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## Catalog

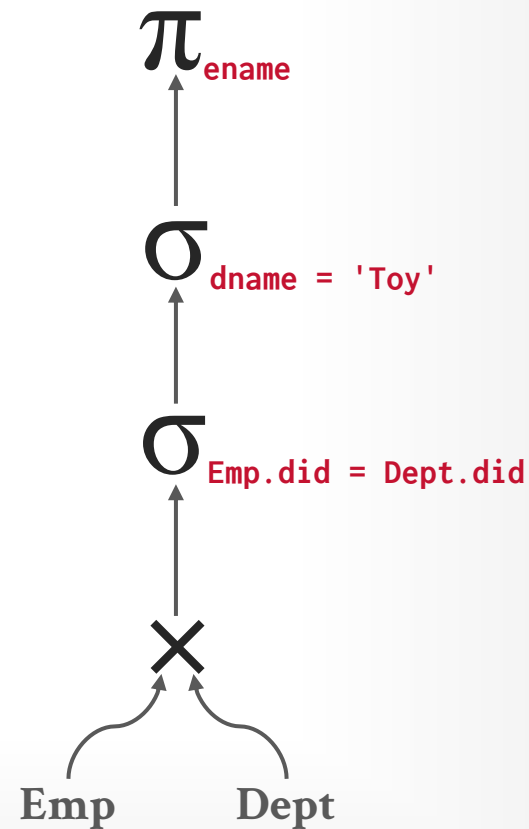


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## Catalog

<i>clustered</i>	<i>unclustered</i>	<i>unclustered</i>
▲	△	△
<b>Emp(<u>ssn</u>, ename, addr, sal, did)</b>		
10,000 records		
1,000 pages		
<i>clustered</i>	<i>unclustered</i>	
▲	△	
<b>Dept(<u>did</u>, dname, floor, mgr)</b>		
500 records		
50 pages		



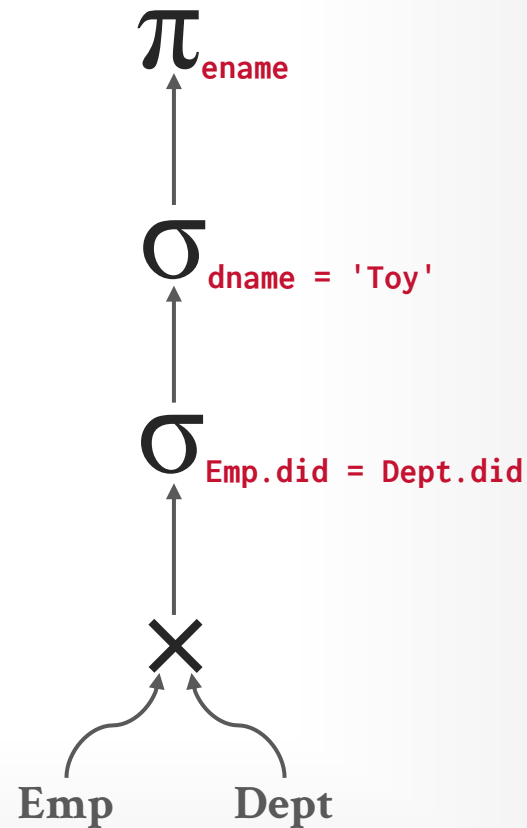
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<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

(50 + 50,000) reads  
+ 1,000,000 writes  
Write temp file T1  
5 tuples per page in T1





# MOTIVATION

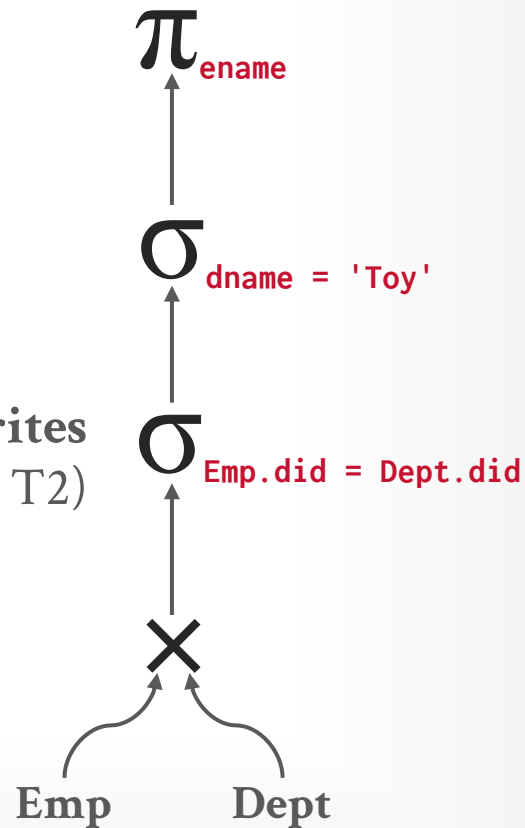
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<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

1,000,000 reads + 2,000 writes  
(FK join, 10k tuples in temp T2)

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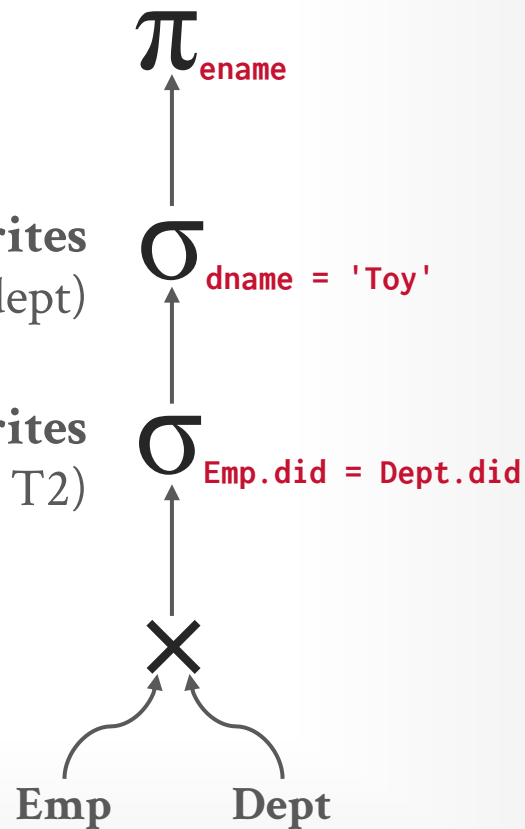
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<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
<b>Emp(ssn, ename, addr, sal, did)</b>		
10,000 records 1,000 pages		
<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

2,000 reads + 4 writes  
(10K/500 = 20 emps per dept)

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(FK join, 10k tuples in temp T2)

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<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

4 reads + 1 write

$\pi_{ename}$

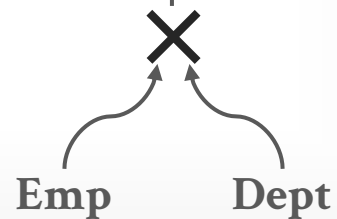
2,000 reads + 4 writes  
(10K/500 = 20 emps per dept)

$\sigma_{dname = 'Toy'}$

1,000,000 reads + 2,000 writes  
(FK join, 10k tuples in temp T2)

$\sigma_{Emp.did = Dept.did}$

(50 + 50,000) reads  
+ 1,000,000 writes  
Write temp file T1  
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<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

Total: 2M I/Os

4 reads + 1 write

$\pi_{ename}$

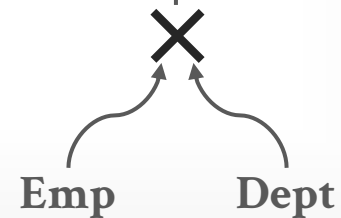
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+ 1,000,000 writes  
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5 tuples per page in T1

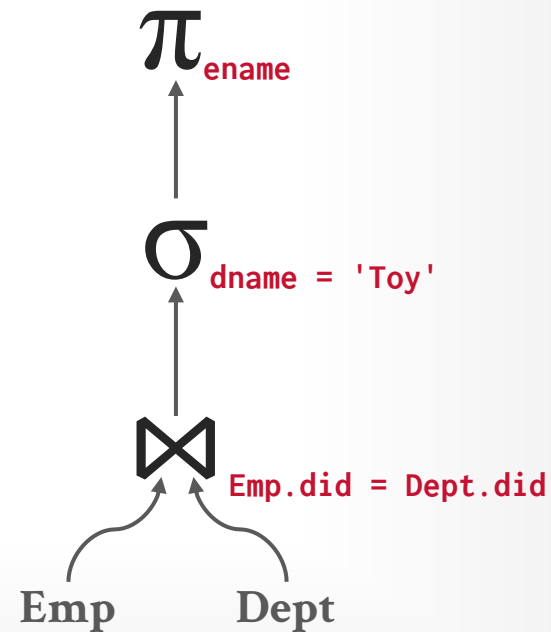


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<i>clustered</i>	<i>unclustered</i>	<i>unclustered</i>
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10,000 records		
1,000 pages		
<i>clustered</i>	<i>unclustered</i>	
▲	△	
<b>Dept(<u>did</u>, dname, floor, mgr)</b>		
500 records		
50 pages		



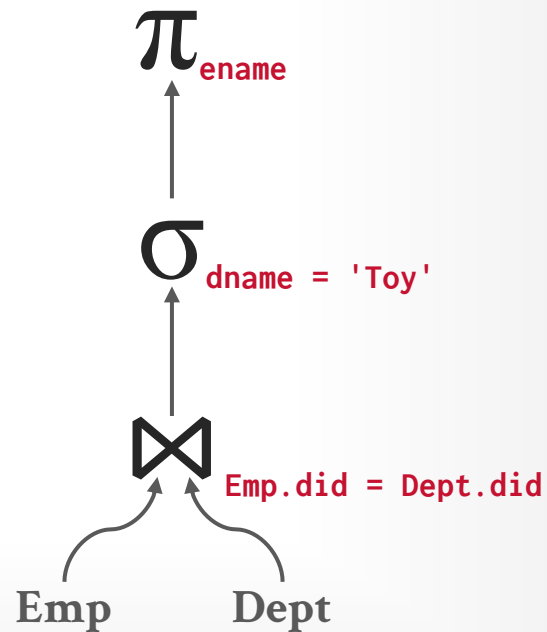
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<b>Dept(did, dname, floor, mgr)</b>		
500 records		
50 pages		

(50 + 50,000) reads  
+ 2,000 writes  
**Page Nested-Loop Join**  
Write Temp T1



# MOTIVATION

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SELECT DISTINCT ename
FROM Emp E JOIN Dept D
ON E.did = D.did
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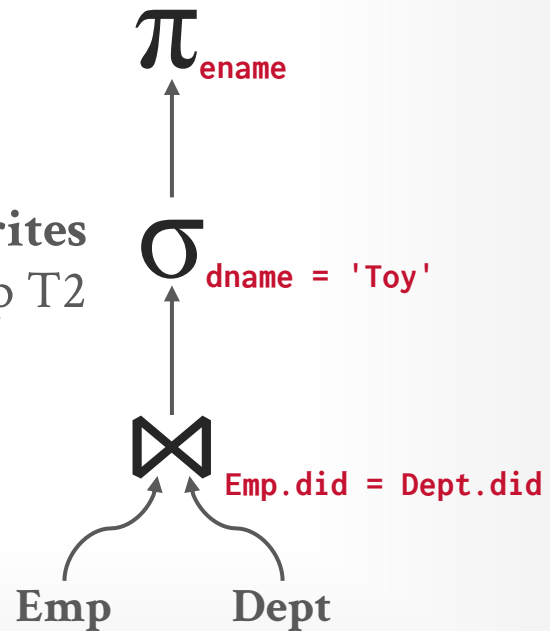
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<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
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<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

2,000 reads + 4 writes  
Read temp T1, Write temp T2

(50 + 50,000) reads  
+ 2,000 writes  
**Page Nested-Loop Join**

Write Temp T1

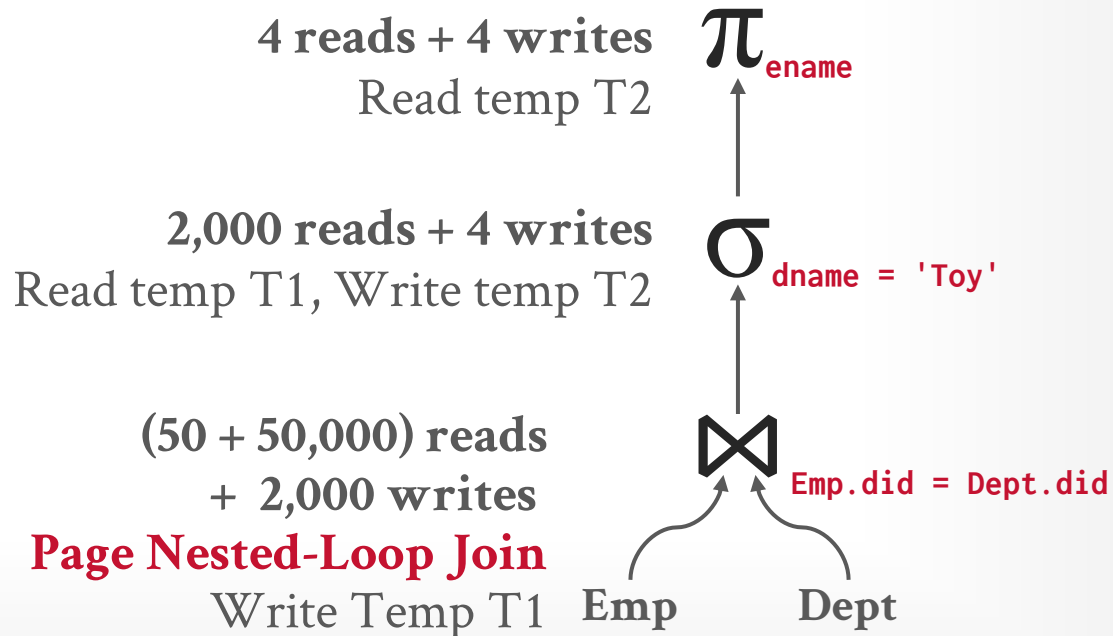


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<i>clustered</i>	<i>unclustered</i>	<i>unclustered</i>
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<b>Emp(ssn, ename, addr, sal, did)</b>		
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▲	△	
<b>Dept(did, dname, floor, mgr)</b>		
500 records		
50 pages		





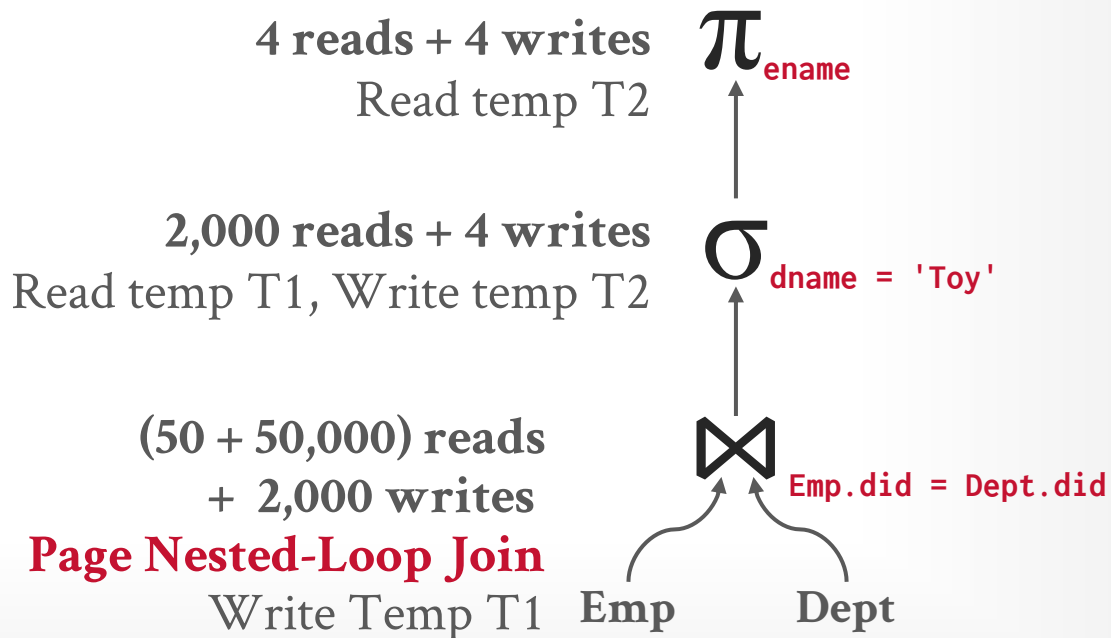
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500 records 50 pages		

Total: 54k I/Os



# MOTIVATION

```
SELECT DISTINCT ename
FROM Emp E JOIN Dept D
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```

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<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
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<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

Total: 54k I/Os

4 reads + 4 writes  
Read temp T2

$\pi_{ename}$

2,000 reads + 4 writes  
Read temp T1, Write temp T2

$\sigma_{dname = 'Toy'}$

(50 + 50,000) reads  
+ 2,000 writes  
**Page Nested-Loop Join**  
Write Temp T1

$\bowtie$

Emp.did = Dept.did

Emp

Dept

# MOTIVATION

```
SELECT DISTINCT ename
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<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
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<b>Dept(did, dname, floor, mgr)</b>		
500 records 50 pages		

Total: 7,159 I/Os

4 reads + 4 writes  
Read temp T2

$\pi_{ename}$

2,000 reads + 4 writes  
Read temp T1, Write temp T2

$\sigma_{dname = 'Toy'}$

$3 \times (|Emp| + |Dept|) =$   
3,150 reads + 2,000 writes  
**Sort-Merge Join (50 Buffers)**  
Write Temp T1

$\bowtie$   
Emp.did = Dept.did

Emp Dept

# MOTIVATION

```
SELECT DISTINCT ename
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## Catalog

<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
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Materialization Model

Total: 7,159 I/Os

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**Sort-Merge Join (50 Buffers)**

$\bowtie$   
Emp.did = Dept.did

Write Temp T1

Emp

Dept

# MOTIVATION

```
SELECT DISTINCT ename
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ON E.did = D.did
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```

No Pipelining!

↳ **Materialization Model** →

**Total: 7,159 I/Os**

## Catalog

<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
<b>Emp(ssn, ename, addr, sal, did)</b>		
10,000 records 1,000 pages		
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reads + 4 writes  
Read temp T2

$\pi_{ename}$



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Emp

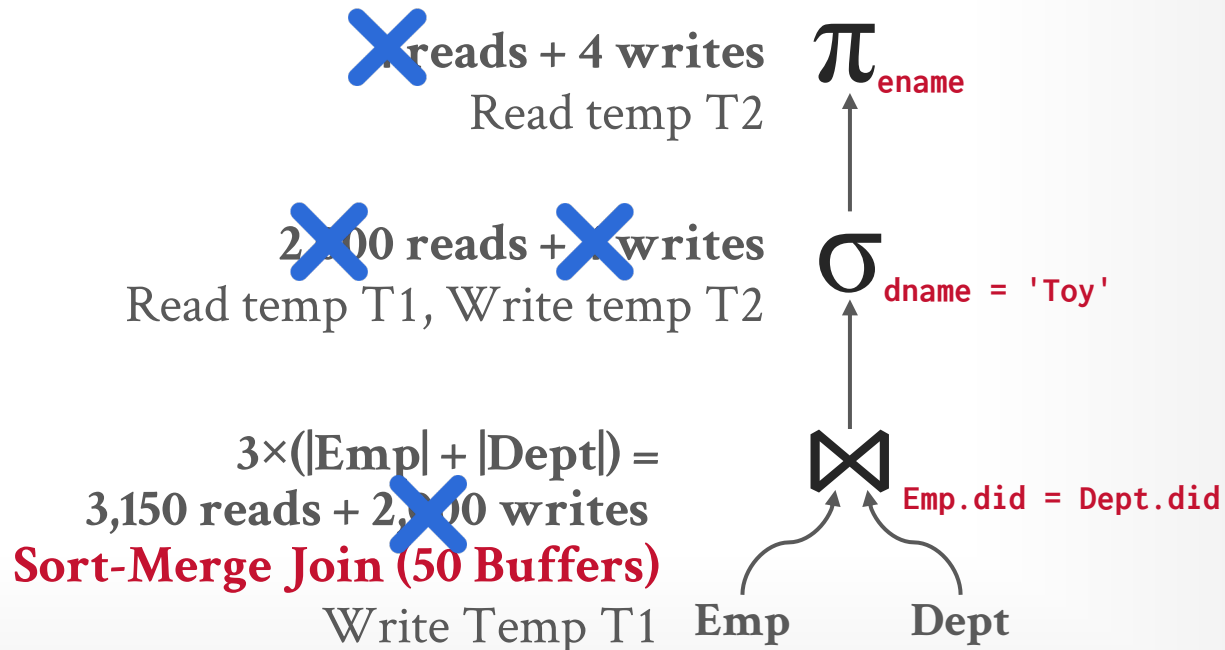
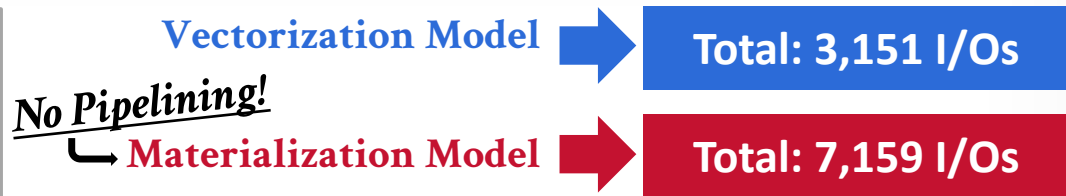
Dept

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clustered	unclustered	unclustered
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10,000 records		
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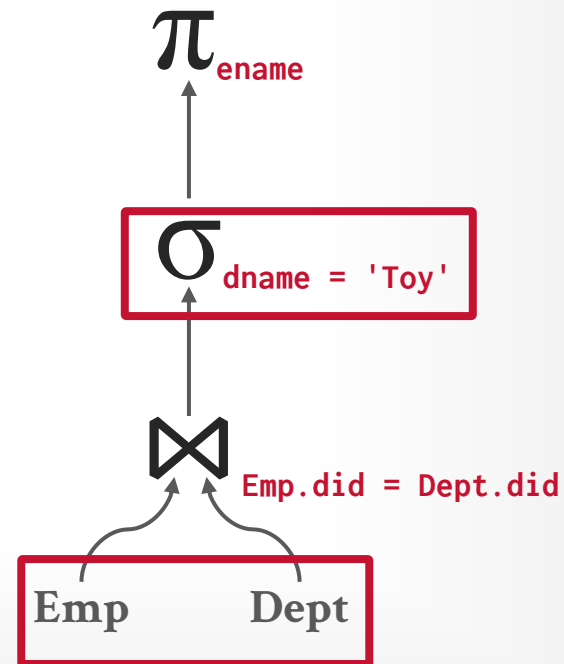


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Emp( <u>ssn</u> , ename, addr, sal, did)		
10,000 records		
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Dept( <u>did</u> , dname, floor, mgr)		
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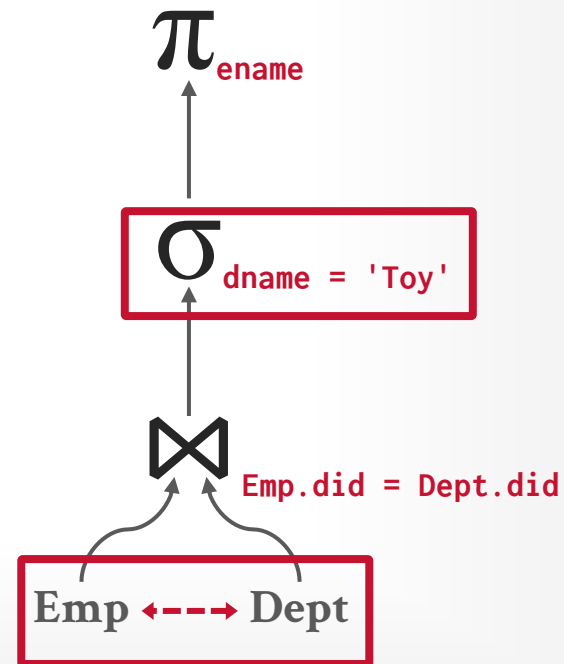


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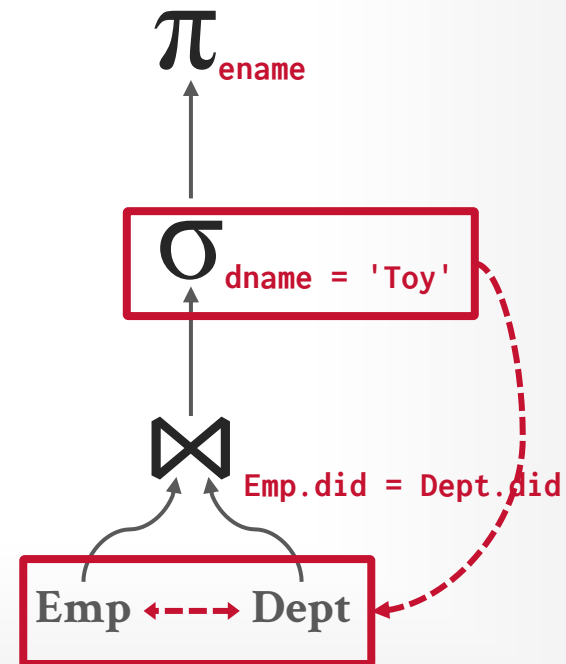


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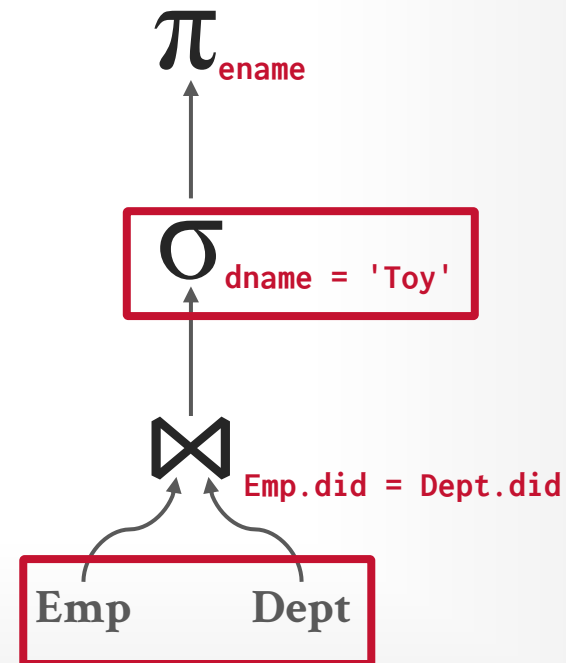


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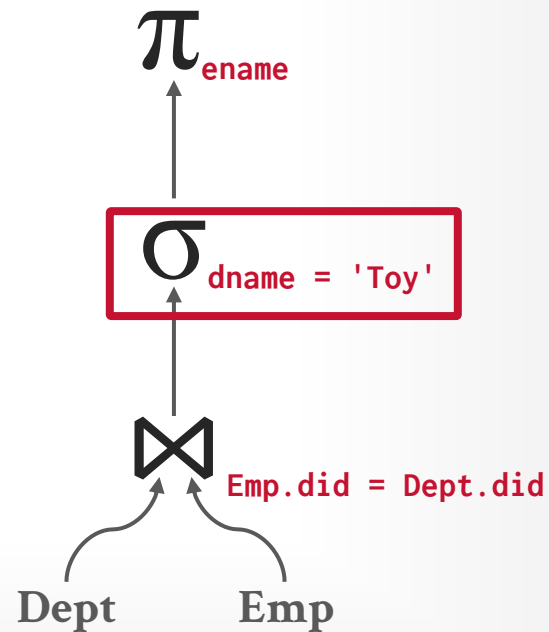


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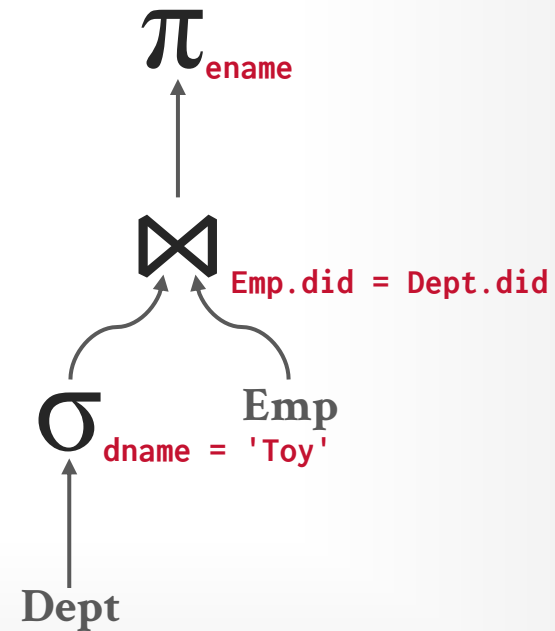


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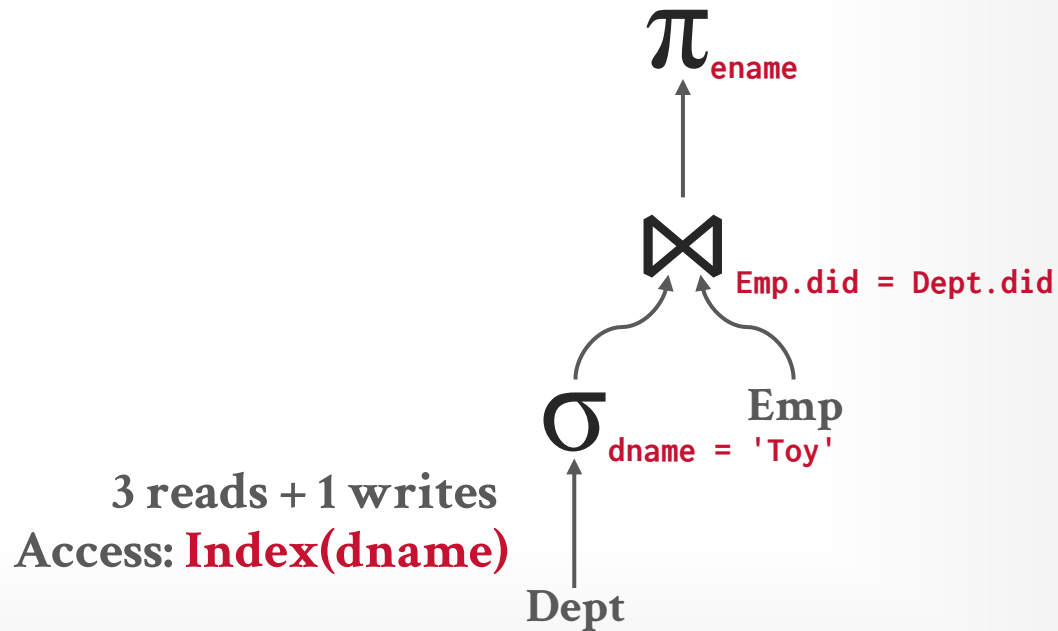


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50 pages		



# MOTIVATION

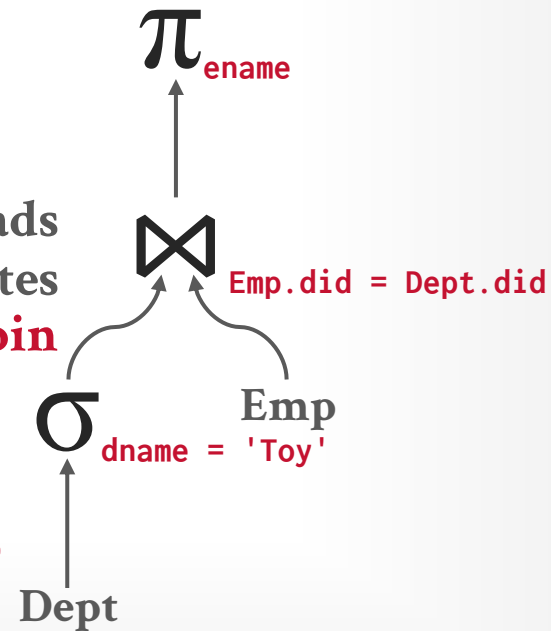
```
SELECT DISTINCT ename
FROM Emp E JOIN Dept D
ON E.did = D.did
WHERE D.dname = 'Toy'
```

## Catalog

<i>clustered</i>	<i>unclustered</i>	<i>unclustered</i>
▲	△	△
<b>Emp(<u>ssn</u>, ename, addr, sal, did)</b>		
10,000 records		
1,000 pages		
<hr/>		
<i>clustered</i>	<i>unclustered</i>	
▲	△	
<b>Dept(<u>did</u>, dname, floor, mgr)</b>		
500 records		
50 pages		

1 + 3 (idx) + 20 (ptr chase) reads  
+ 4 writes  
**Index Nested-Loop Join**

3 reads + 1 writes  
**Access: Index(dname)**

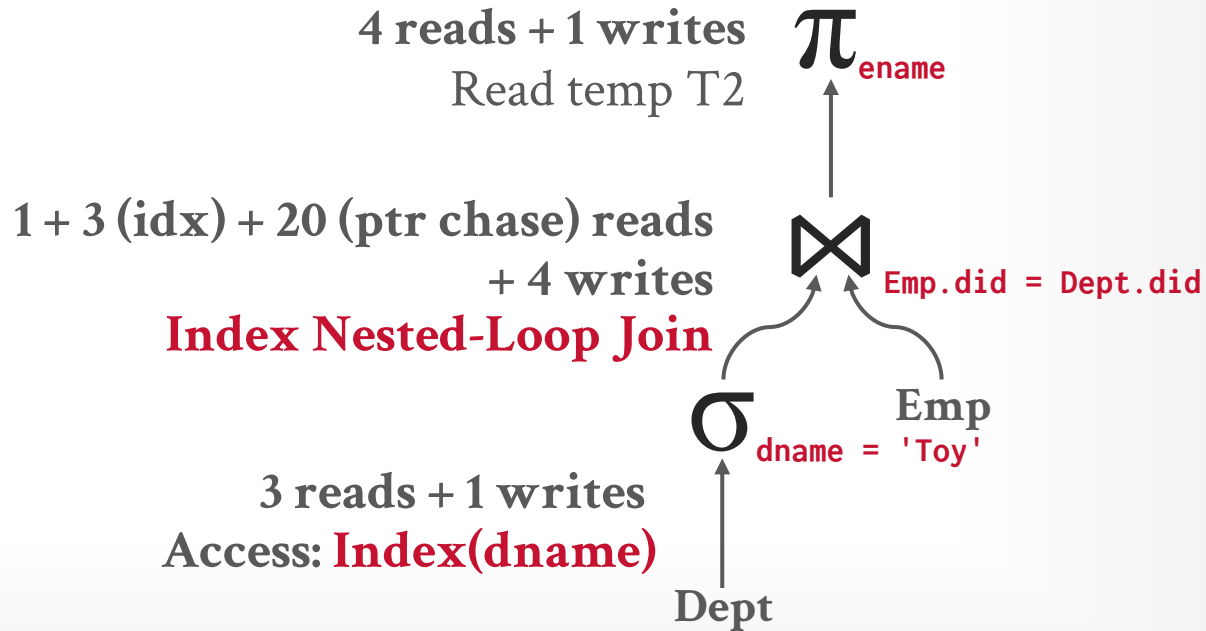


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## Catalog

clustered ▲	unclustered △	unclustered △
Emp( <u>ssn</u> , ename, addr, sal, did)		
10,000 records 1,000 pages		
<hr/>		
clustered ▲	unclustered △	
Dept( <u>did</u> , dname, floor, mgr)		
500 records 50 pages		





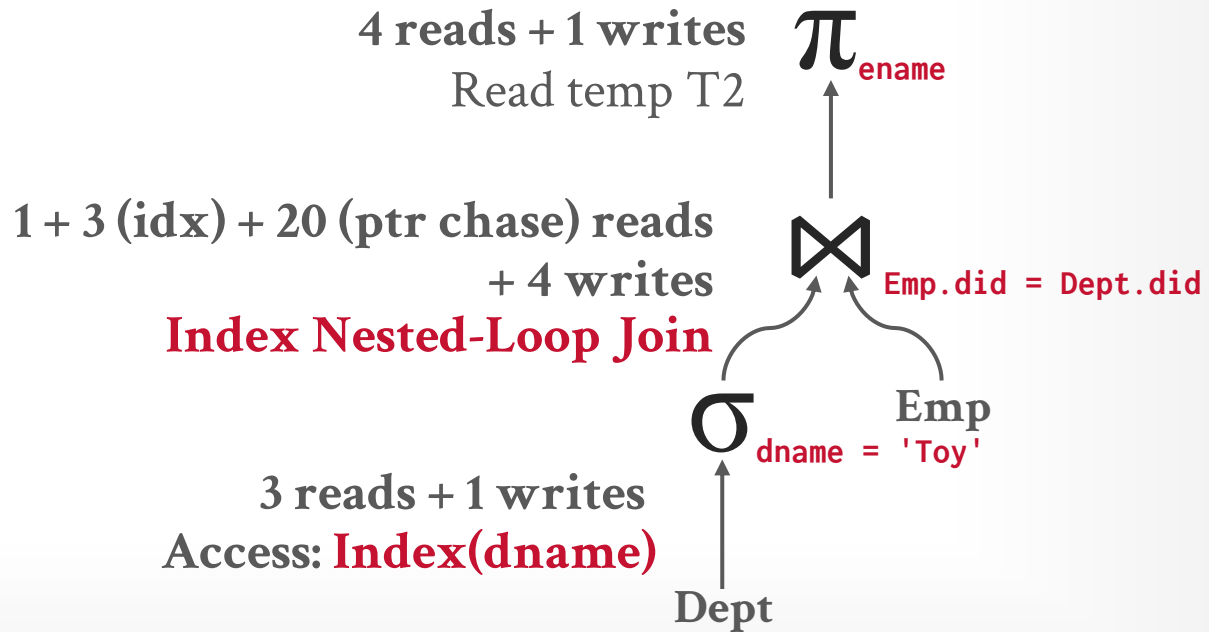
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<i>clustered</i> ▲	<i>unclustered</i> △	<i>unclustered</i> △
<b>Emp(<u>ssn</u>, ename, addr, sal, did)</b>		
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<hr/>		
<i>clustered</i> ▲	<i>unclustered</i> △	
<b>Dept(<u>did</u>, dname, floor, mgr)</b>		
500 records 50 pages		

Total: 37 I/Os



# TODAY'S AGENDA

---

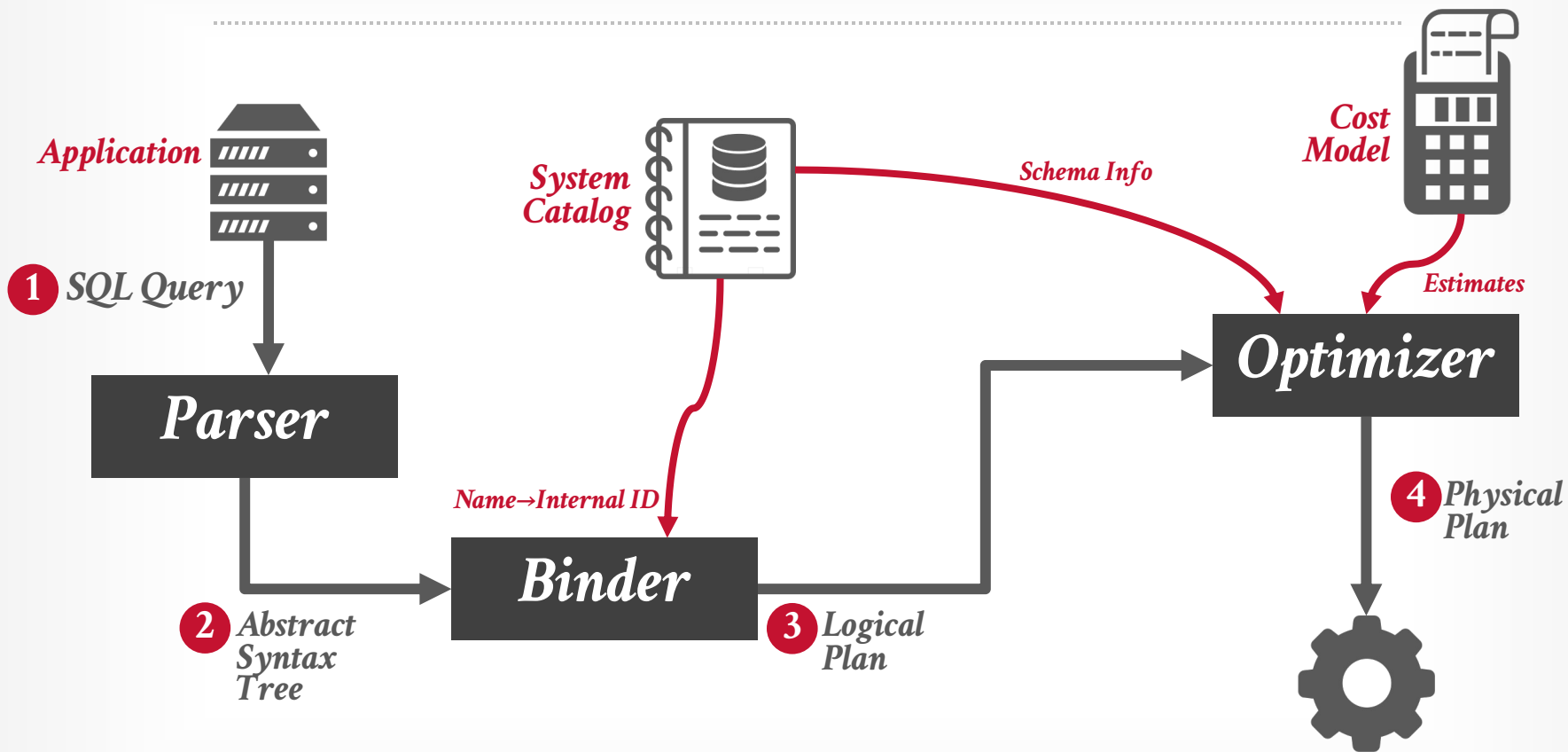
Background

Heuristic / Ruled-based Optimization

Cost-based Optimization

Cost Model Estimation

# ARCHITECTURE OVERVIEW



# LOGICAL VS. PHYSICAL PLANS

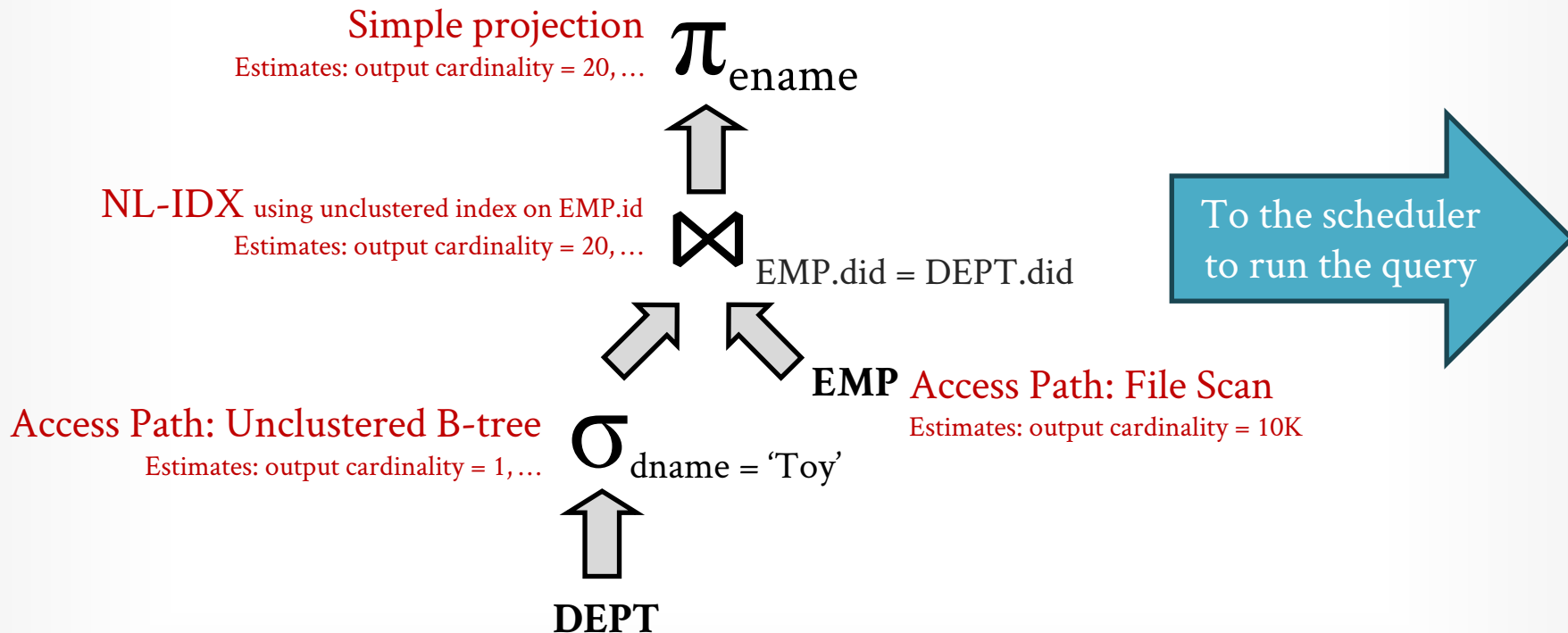
---

The optimizer generates a mapping of a logical algebra expression to the optimal equivalent physical algebra expression.

Physical operators define a specific execution strategy using an access path.

- They can depend on the physical format of the data that they process (i.e., sorting, compression).
- Not always a 1:1 mapping from logical to physical.

# Annotated RA Tree a.k.a. The Physical Plan



# QUERY OPTIMIZATION (QO)


---

1. Identify candidate equivalent trees (logical). It is an NP-hard problem, so the space is large.
2. For each candidate, find the execution plan (physical). Estimate the cost of each plan.
3. Choose the best (physical) plan.

# QUERY OPTIMIZATION (QO)

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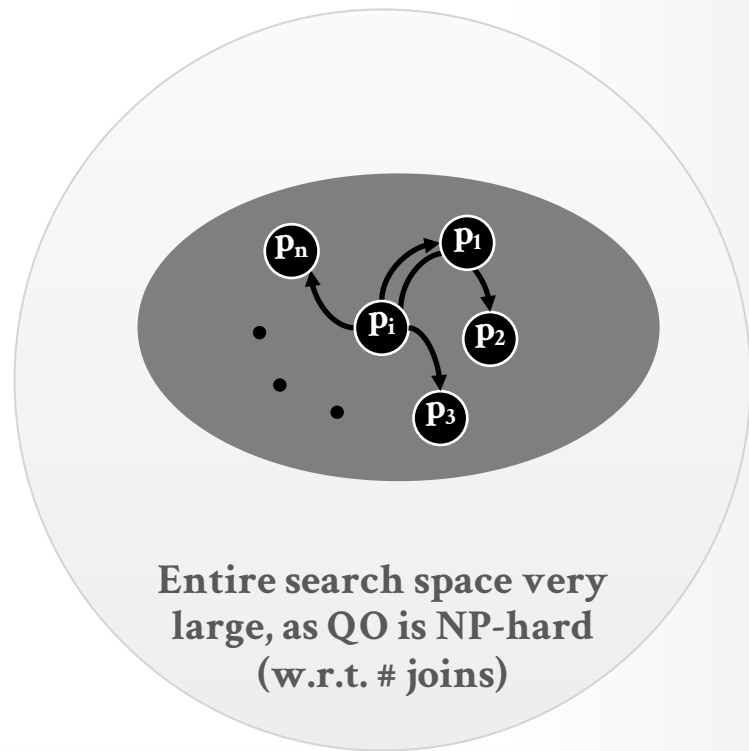


**Entire search space very large, as QO is NP-hard (w.r.t. # joins)**

# QUERY OPTIMIZATION (QO)

---

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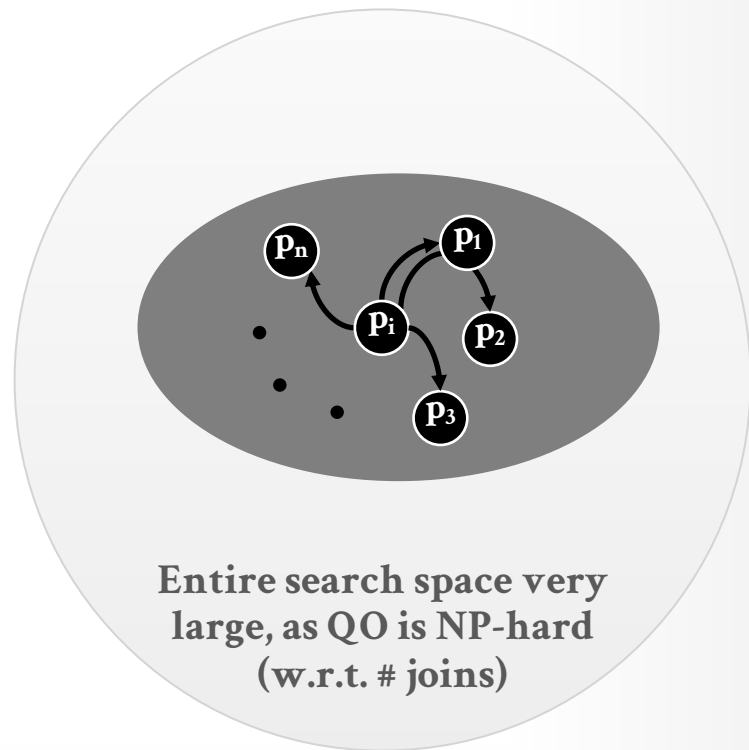




# QUERY OPTIMIZATION (QO)

1. Identify candidate equivalent trees (logical). It is an NP-hard problem, so the space is large.
2. For each candidate, find the execution plan (physical). Estimate the cost of each plan.
3. Choose the best (physical) plan.

**Practically: Choose from a subset of all possible plans.**



# QUERY OPTIMIZATION

---

## Heuristics / Rules

- Rewrite the query to remove (guessed) inefficiencies.
- Examples: always do selections first or push down projections as early as possible.
- These techniques may need to examine catalog, but they do not need to examine data.

## Cost-based Search

- Use a model to estimate the cost of executing a plan.
- Enumerate multiple equivalent plans for a query and pick the one with the lowest cost.

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# LOGICAL PLAN OPTIMIZATION

---

Transform a logical plan into an equivalent logical plan using pattern matching rules.

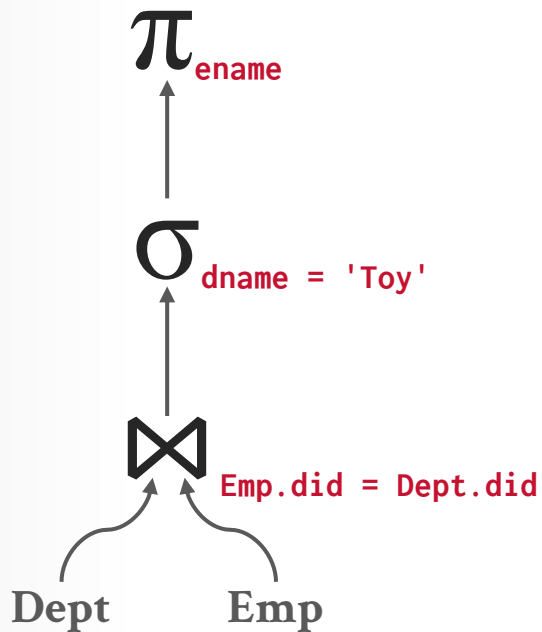
The goal is to increase the likelihood of enumerating the optimal plan in the search.

→ Many equivalence rules for relational algebra!

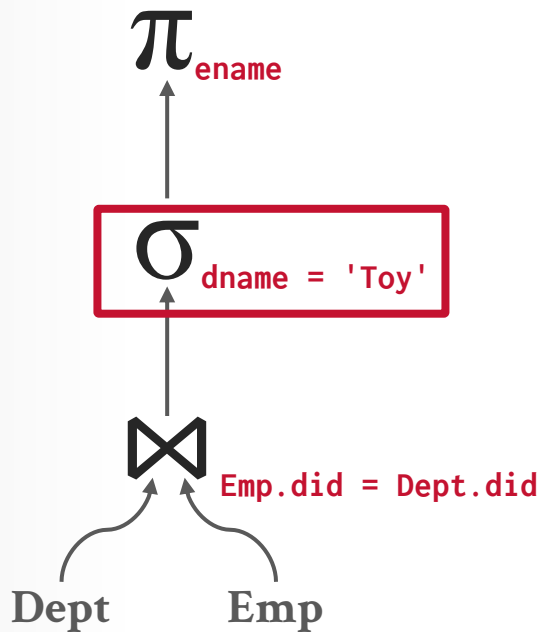
Cannot compare plans because there is no cost model but can "direct" a transformation to a preferred side.

# PREDICATE PUSHDOWN

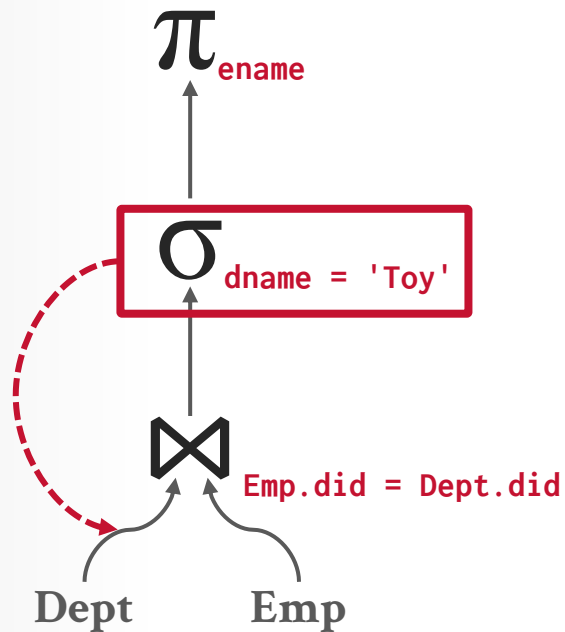
---


$$\pi_{\text{ename}} \left( \sigma_{\text{dname} = \text{'Toy'}} (\text{Dept} \bowtie \text{Emp}) \right)$$

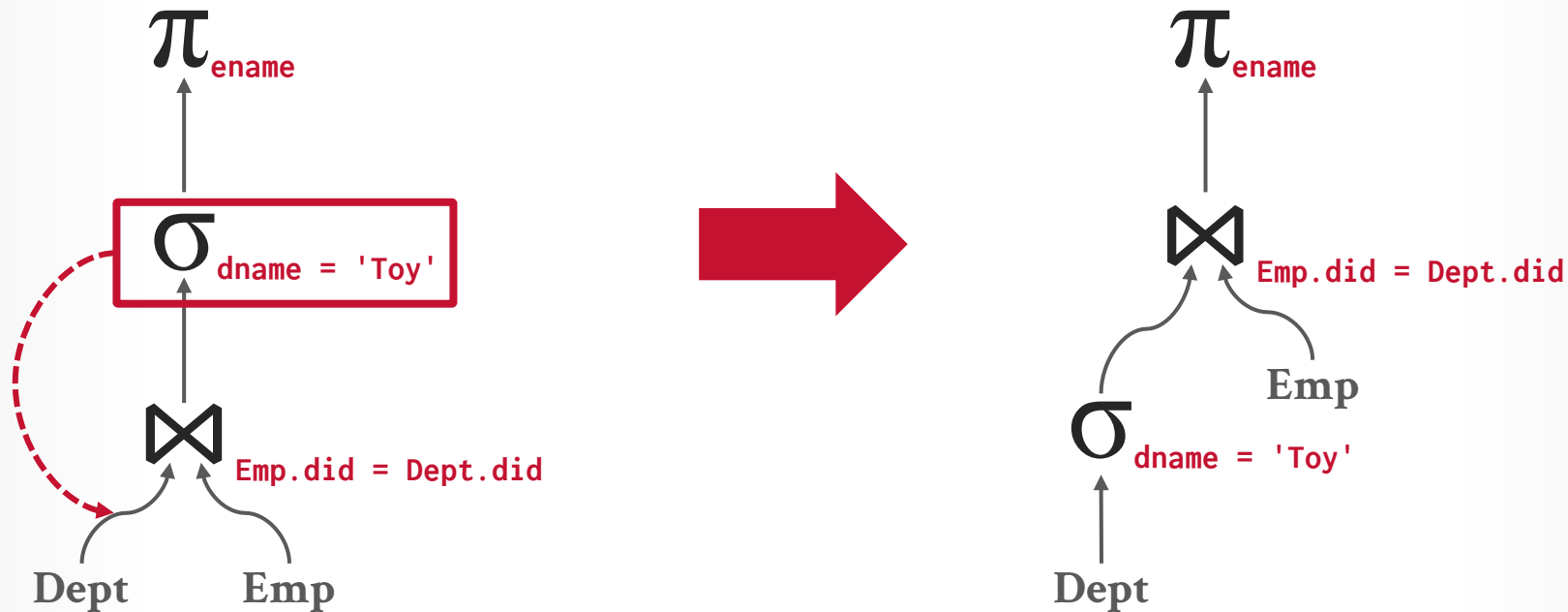
# PREDICATE PUSHDOWN


$$\pi_{\text{ename}} \left( \sigma_{\text{dname} = \text{'Toy'}} (\text{Dept} \bowtie \text{Emp}) \right)$$

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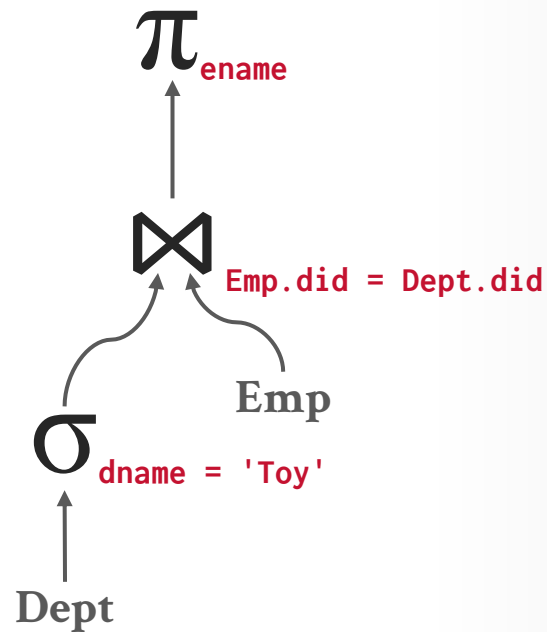
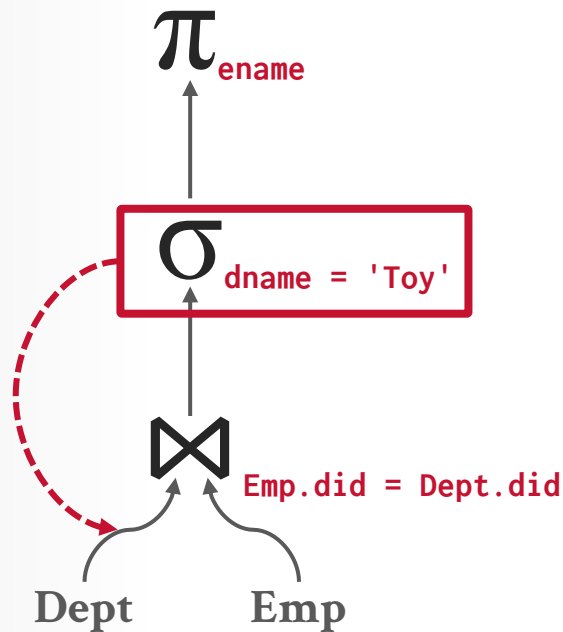
# PREDICATE PUSHDOWN



$$\pi_{ename} \left( \sigma_{dname = 'Toy'} (Dept \bowtie Emp) \right)$$



# PREDICATE PUSHDOWN



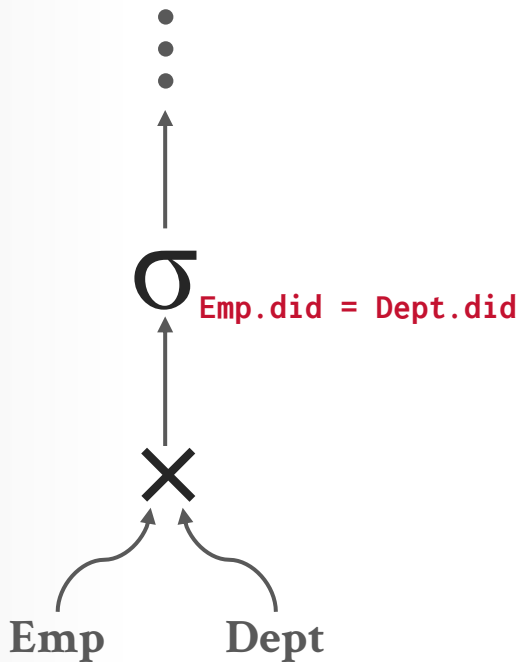
$$\pi_{ename} \left( \sigma_{dname = 'Toy'} (Dept \bowtie Emp) \right)$$

*Rewrite*

$$\pi_{ename} \left( Emp \bowtie \sigma_{dname = 'Toy'} (Dept) \right)$$

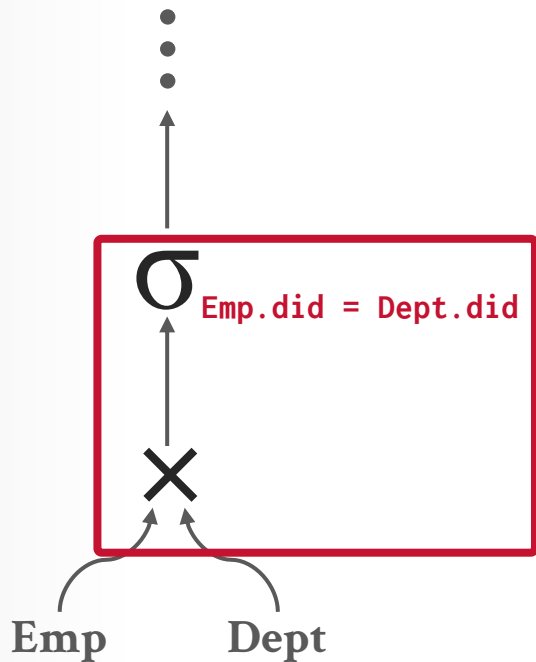
# REPLACE CARTESIAN PRODUCT

---



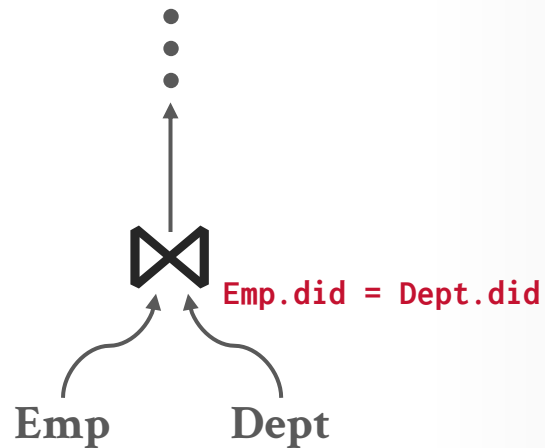
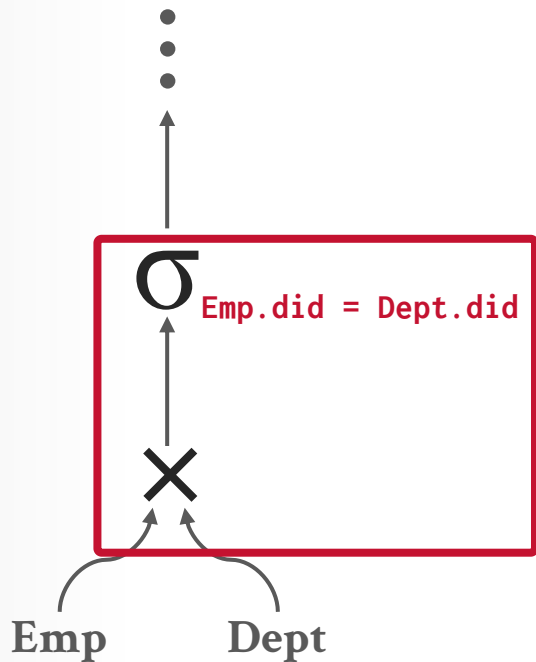
$\dots (\sigma_{\text{Dept.did} = \text{Emp.did}} (\text{Dept} \times \text{Emp}))$

# REPLACE CARTESIAN PRODUCT



$\dots (\sigma_{\text{Dept.did} = \text{Emp.did}} (\text{Dept} \times \text{Emp}))$

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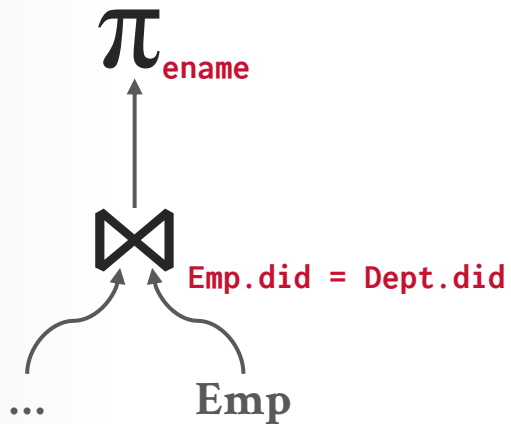
$\dots (\sigma_{\text{Dept.did} = \text{Emp.did}} (\text{Dept} \times \text{Emp}))$

*Rewrite*

$\dots (\text{Emp} \bowtie_{\text{Emp.did} = \text{Dept.did}} \text{Dept})$

# PROJECTION PUSHDOWN

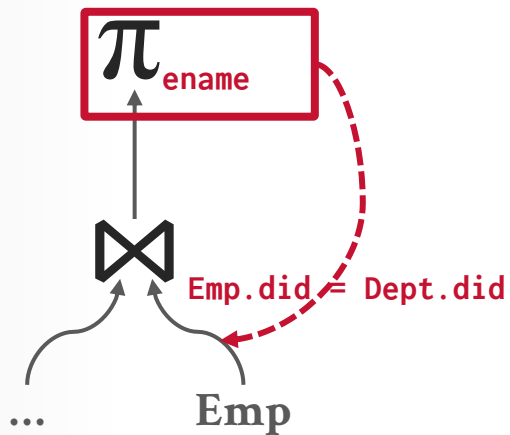
---



$\pi_{Emp.ename} (\dots \bowtie_{did} Emp)$

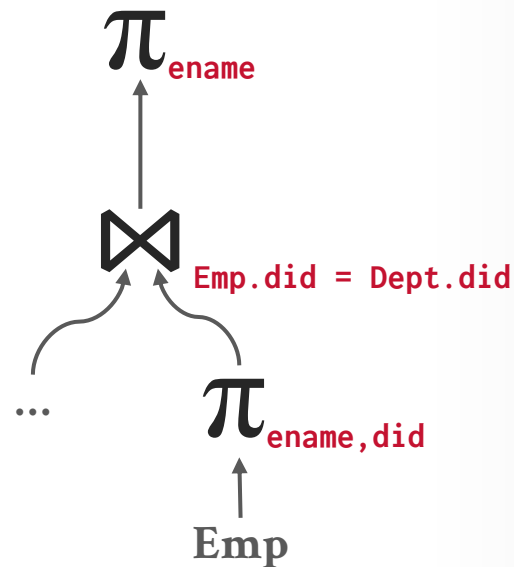
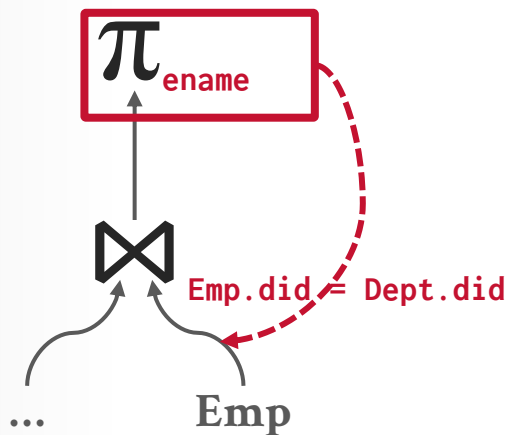
# PROJECTION PUSHDOWN

---



$\pi_{\text{Emp.ename}} (\dots \bowtie_{\text{did}} \text{Emp})$

# PROJECTION PUSHDOWN



$$\pi_{Emp.ename} (\dots \bowtie_{did} Emp)$$

*Rewrite*

$$\pi_{Emp.ename} (\dots \bowtie_{did} (\pi_{ename, did} Emp))$$

# QUERY OPTIMIZATION

---

## Heuristics / Rules

- Rewrite the query to remove (guessed) inefficiencies.
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## Cost-based Search

- Use a model to estimate the cost of executing a plan.
- Enumerate multiple equivalent plans for a query and pick the one with the lowest cost.



# COST-BASED QUERY OPTIMIZATION

---

We will start with cost-based, bottom-up QO

→ a.k.a. the "classic" IBM System R optimizer

Approach: Enumerate different plans for the query and estimate their costs.

→ Single relation.

→ Multiple relations.

→ Nested sub-queries.

It chooses the best plan it has seen for the query after exhausting all plans or some timeout.

# SINGLE-RELATION QUERY PLANNING

---

Pick the best access method.

- Sequential Scan
- Binary Search (clustered indexes)
- Index Scan

Predicate evaluation ordering.

Simple heuristics are often good enough for this.

# MULTI-RELATION QUERY PLANNING

---

## Approach #1: Generative / Bottom-Up

- Start with nothing and then iteratively assemble and add building blocks to generate a query plan.
- **Examples:** System R, Starburst

## Approach #2: Transformation / Top-Down

- Start with the outcome that the query wants, and then transform it to equivalent alternative sub-plans to find the optimal plan that gets to that goal.
- **Examples:** Volcano, Cascades

# BOTTOM-UP OPTIMIZATION

---

Use static rules to perform initial optimization.  
Then use dynamic programming to determine the best join order for tables using a divide-and-conquer search method

**Examples:** IBM System R, DB2, MySQL, Postgres, most open-source DBMSs.

# SYSTEM R OPTIMIZER

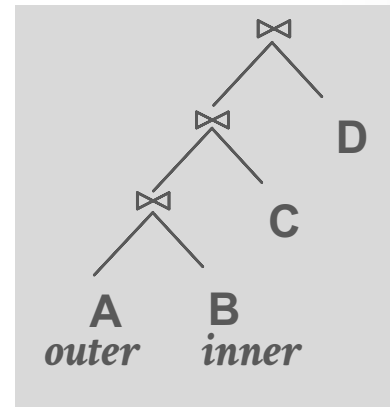
Break query into blocks and generate logical operators for each block.

For each logical operator, generate a set of physical operators that implement it.

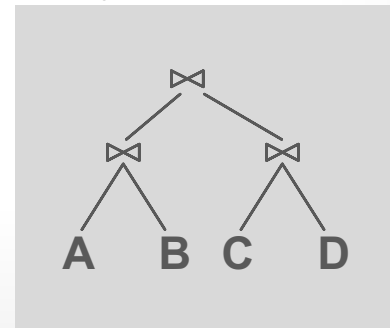
→ All combinations of join algorithms and access paths

Then, iteratively construct a “left-deep” join tree that minimizes the estimated amount of work to execute the plan.

*Left-Deep Tree*



*Bushy Tree*



# SYSTEM R OPTIMIZER

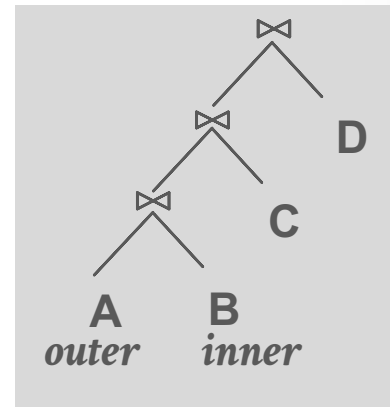
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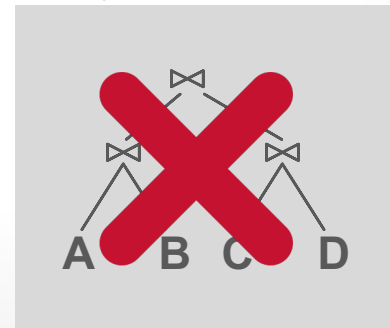
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*Left-Deep Tree*



*Bushy Tree*



# SYSTEM R OPTIMIZER

---

```
SELECT ARTIST.NAME
  FROM ARTIST, APPEARS, ALBUM
 WHERE ARTIST.ID=APPEARS.ARTIST_ID
       AND APPEARS.ALBUM_ID=ALBUM.ID
       AND ALBUM.NAME="Andy's OG Remix"
 ORDER BY ARTIST.ID
```

# SYSTEM R OPTIMIZER

---

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**Step #1:** Choose the best access paths  
to each table



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**ARTIST:** Sequential Scan

**APPEARS:** Sequential Scan

**ALBUM:** Index Look-up on **NAME**

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ARTIST	⊗	APPEARS	⊗	ALBUM
APPEARS	⊗	ALBUM	⊗	ARTIST
ALBUM	⊗	APPEARS	⊗	ARTIST
APPEARS	⊗	ARTIST	⊗	ALBUM
ARTIST	×	ALBUM	⊗	APPEARS
ALBUM	×	ARTIST	⊗	APPEARS
⋮		⋮		⋮

# SYSTEM R OPTIMIZER

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**Step #1:** Choose the best access paths to each table

**Step #2:** Enumerate all possible join orderings for tables

**Step #3:** Determine the join ordering with the lowest cost

ARTIST	⊗	APPEARS	⊗	ALBUM
APPEARS	⊗	ALBUM	⊗	ARTIST
ALBUM	⊗	APPEARS	⊗	ARTIST
APPEARS	⊗	ARTIST	⊗	ALBUM
ARTIST	×	ALBUM	⊗	APPEARS
ALBUM	×	ARTIST	⊗	APPEARS
⋮		⋮		⋮

*Logical Op*

*Physical Op*

# SYSTEM R OPTIMIZER

---

ARTIST  $\bowtie$  APPEARS  $\bowtie$  ALBUM

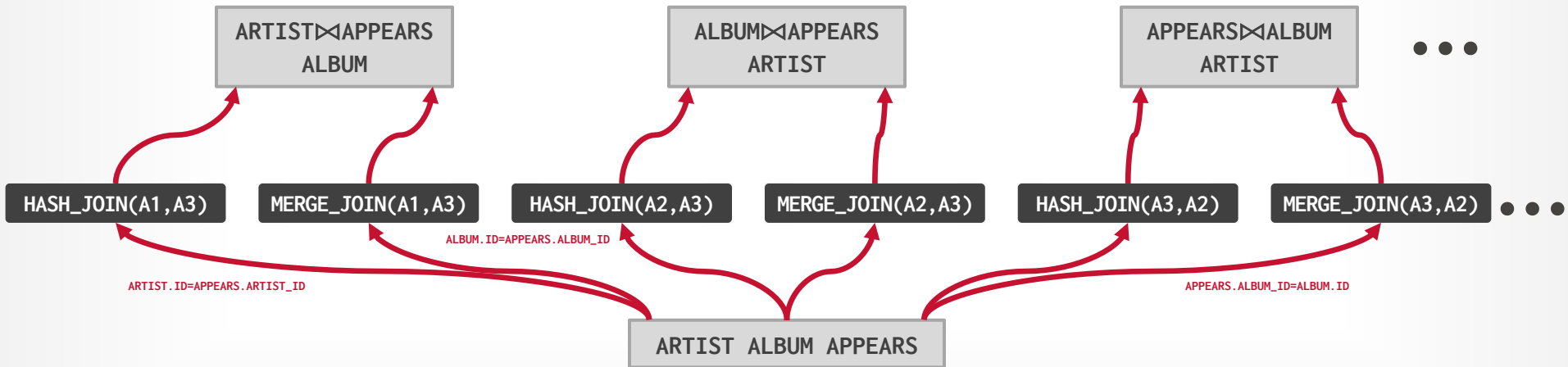
ARTIST ALBUM APPEARS

□ Logical Op

■ Physical Op

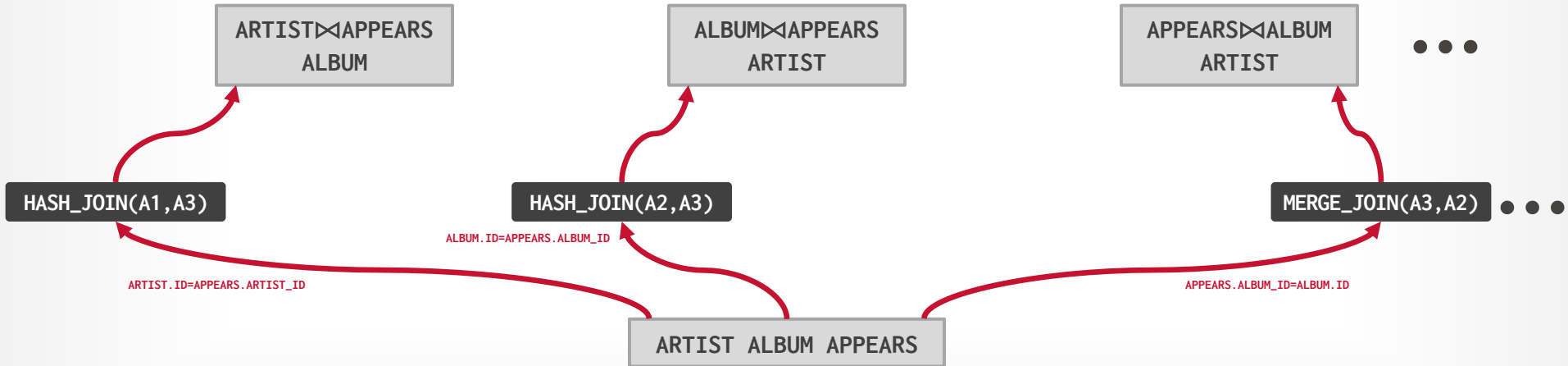
# SYSTEM R OPTIMIZER

ARTIST ⋈ APPEARS ⋈ ALBUM



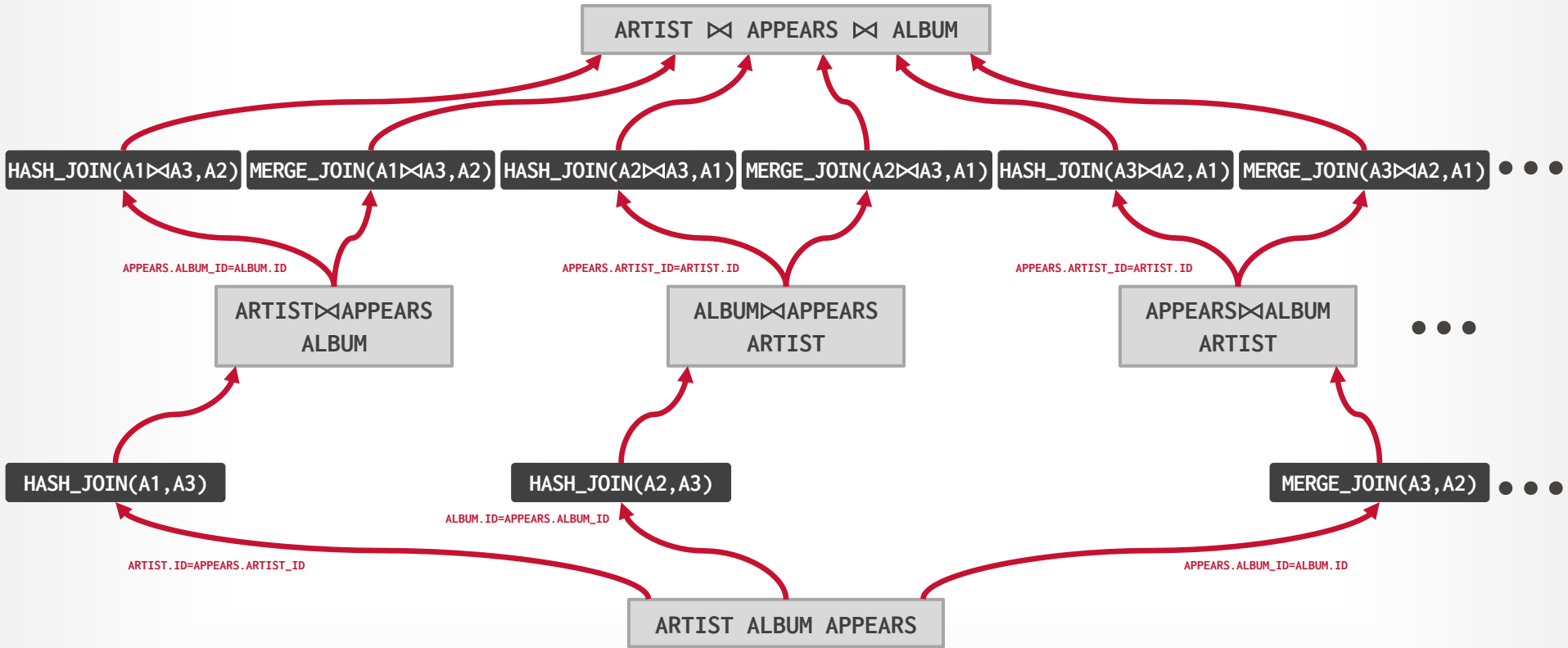
# SYSTEM R OPTIMIZER

ARTIST ⋈ APPEARS ⋈ ALBUM



# SYSTEM R OPTIMIZER

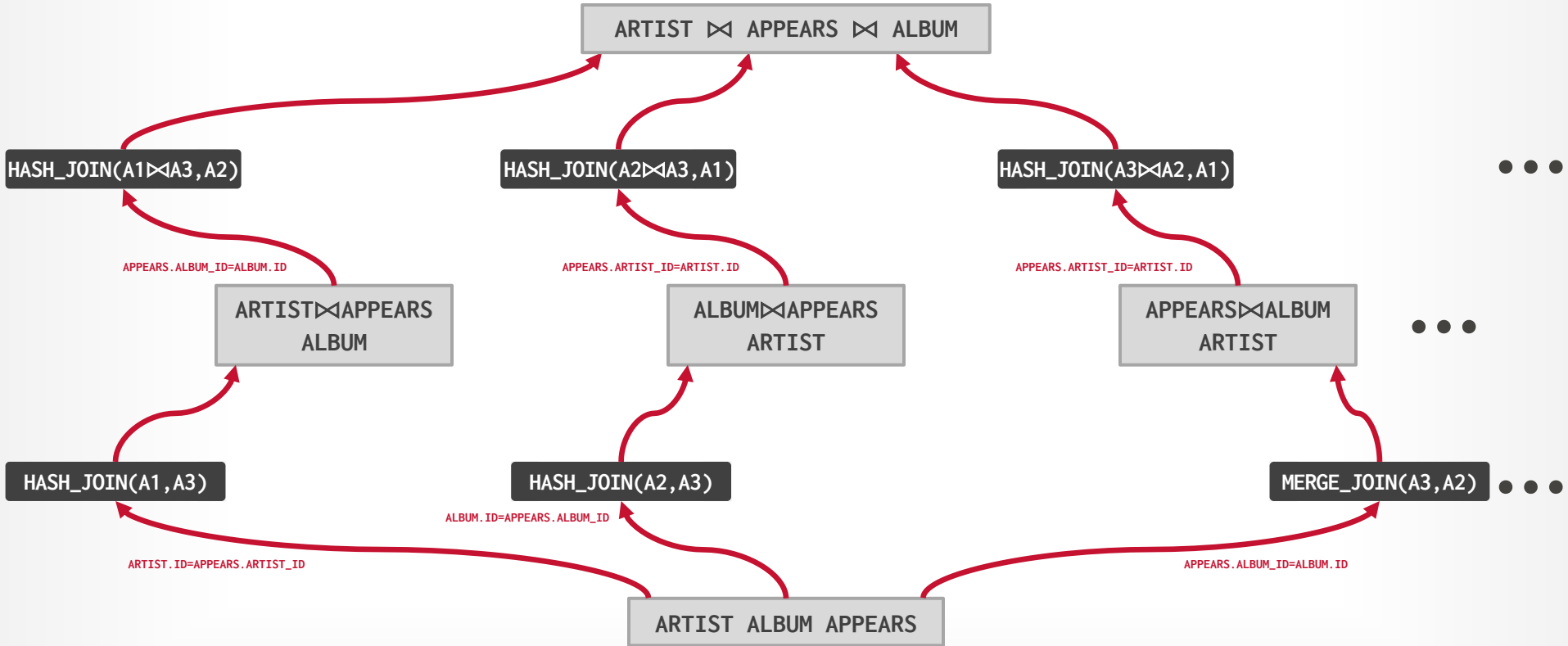
- Logical Op  
 Physical Op





# SYSTEM R OPTIMIZER

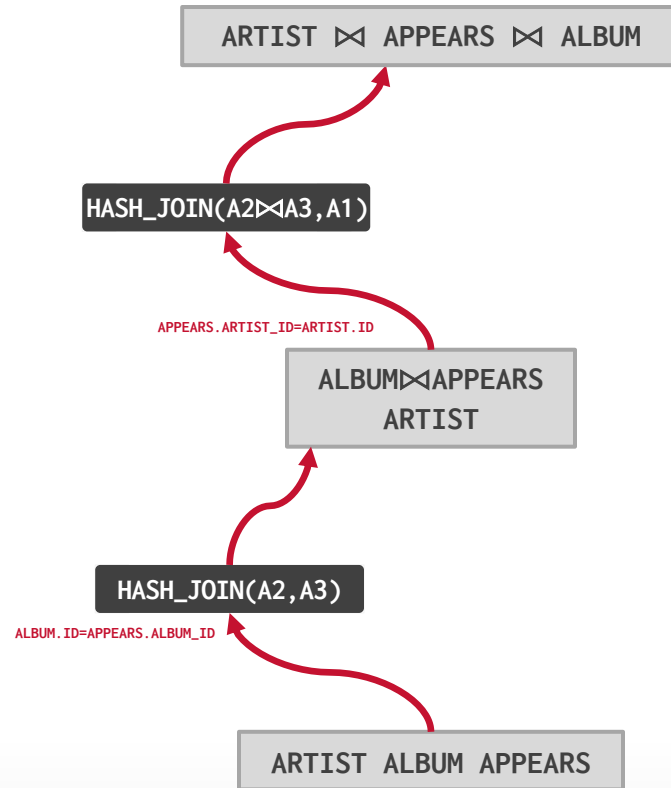
Logical Op  
 Physical Op



□ Logical Op

■ Physical Op

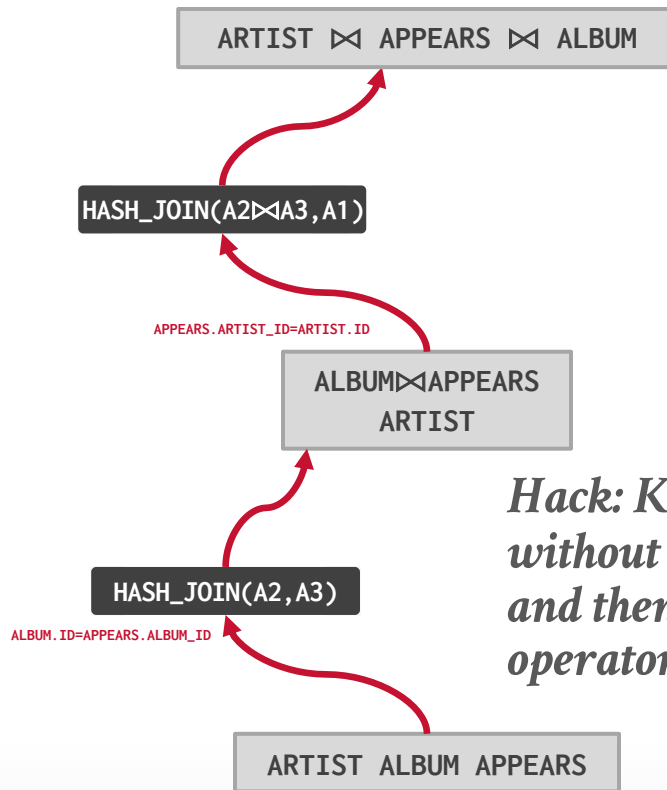
# SYSTEM R OPTIMIZER



Logical Op

Physical Op

# SYSTEM R OPTIMIZER

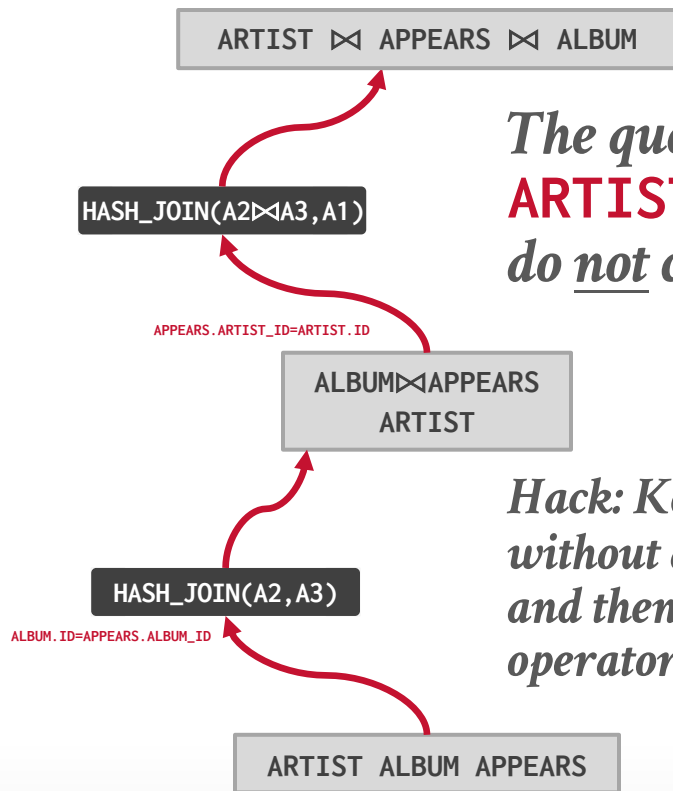


*Hack: Keep track of best plans with and without data in proper physical form, and then check whether tacking on a sort operator at the end is better.*

Logical Op

Physical Op

# SYSTEM R OPTIMIZER



The query has **ORDER BY** on **ARTIST.ID** but the logical plans do not contain sorting properties.

Hack: Keep track of best plans with and without data in proper physical form, and then check whether tacking on a sort operator at the end is better.

# TOP-DOWN OPTIMIZATION

---

Start with a logical plan of what we want the query to be. Perform a branch-and-bound search to traverse the plan tree by converting logical operators into physical operators.

- Keep track of global best plan during search.
- Treat physical properties of data as first-class entities during planning.

**Examples:** MSSQL, Greenplum, CockroachDB

# Example Logical Rules

---

$$\sigma_{P_1} (\sigma_{P_2}(R)) \equiv \sigma_{P_2} (\sigma_{P_1}(R)) \quad (\sigma \text{ commutativity})$$

$$\sigma_{P_1 \wedge P_2 \dots \wedge P_n} (R) \equiv \sigma_{P_1} (\sigma_{P_2} (\dots \sigma_{P_n}(R))) \quad (\text{cascading } \sigma)$$

$$\prod_{a_1}(R) \equiv \prod_{a_1} (\prod_{a_2} (\dots \prod_{a_k} (R) \dots)), \quad a_i \subseteq a_{i+1} \quad (\text{cascading } \prod)$$

$$R \bowtie S \equiv S \bowtie R \quad (\text{join commutativity})$$

$$R \bowtie (S \bowtie T) \equiv (R \bowtie S) \bowtie T \quad (\text{join associativity})$$

$$\sigma_P (R \bowtie S) \equiv (R \bowtie_P S), \text{ if } P \text{ is a join predicate}$$

$$\sigma_P (R \bowtie S) \equiv \sigma_{P_1} (\sigma_{P_2}(R) \bowtie_{P_4} \sigma_{P_3}(S)), \text{ where } P = p_1 \wedge p_2 \wedge p_3 \wedge p_4$$

$$\prod_{A_1, A_2, \dots, A_n} (\sigma_P (R)) \equiv \prod_{A_1, A_2, \dots, A_n} (\sigma_P (\prod_{A_1, \dots, A_n, B_1, \dots, B_M} R)), \text{ where } B_1 \dots B_M \text{ are columns in } P$$

...

*Logical Op*

*Physical Op*

# TOP-DOWN OPTIMIZATION

---

Start with a logical plan of what we want the query to be.

*Logical Op*

*Physical Op*

# TOP-DOWN OPTIMIZATION

---

Start with a logical plan of what we want the query to be.

```
ARTIST ⋈ APPEARS ⋈ ALBUM  
ORDER-BY(ARTIST.ID)
```



☐ *Logical Op*

■ *Physical Op*

# TOP-DOWN OPTIMIZATION

---

Start with a logical plan of what we want the query to be.

```
ARTIST ⋈ APPEARS ⋈ ALBUM  
ORDER-BY(ARTIST.ID)
```

Invoke rules to create new nodes and traverse tree.

→ **Logical**→**Logical**:

JOIN(A, B) to JOIN(B, A)

→ **Logical**→**Physical**:

JOIN(A, B) to HASH\_JOIN(A, B)

□ *Logical Op*

■ *Physical Op*

# TOP-DOWN OPTIMIZATION

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ARTIST⋈APPEARS

ALBUM⋈APPEARS

ARTIST⋈ALBUM

ARTIST

ALBUM

APPEARS

☐ *Logical Op*

■ *Physical Op*

# TOP-DOWN OPTIMIZATION

Start with a logical plan of what we want the query to be.



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ORDER-BY(ARTIST.ID)

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ARTIST⋈APPEARS

ALBUM⋈APPEARS

ARTIST⋈ALBUM

ARTIST

ALBUM

APPEARS

□ *Logical Op*

■ *Physical Op*

# TOP-DOWN OPTIMIZATION

Start with a logical plan of what we want the query to be.

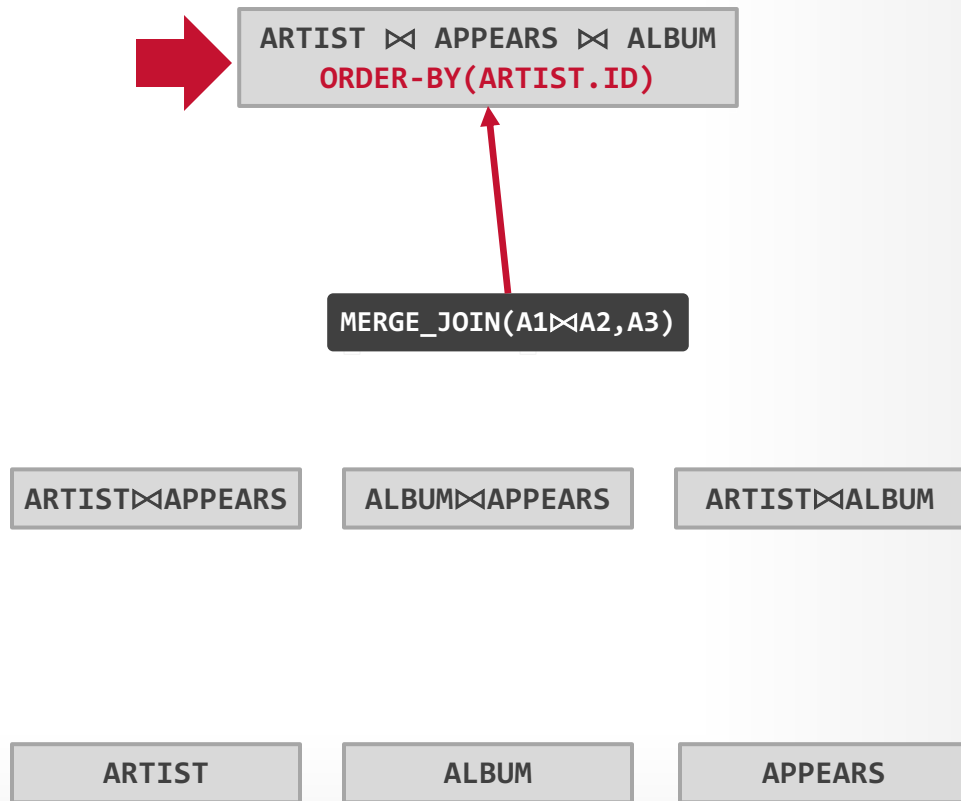
Invoke rules to create new nodes and traverse tree.

→ **Logical**→**Logical**:

JOIN(A, B) to JOIN(B, A)

→ **Logical**→**Physical**:

JOIN(A, B) to HASH\_JOIN(A, B)



□ *Logical Op*

■ *Physical Op*

# TOP-DOWN OPTIMIZATION

Start with a logical plan of what we want the query to be.

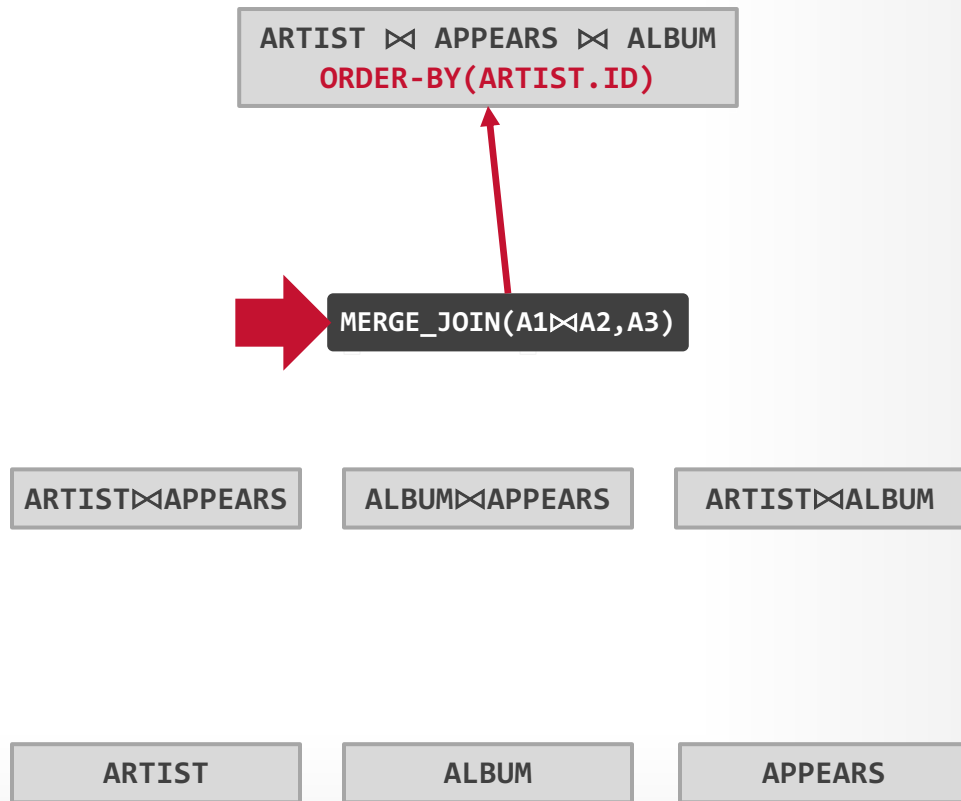
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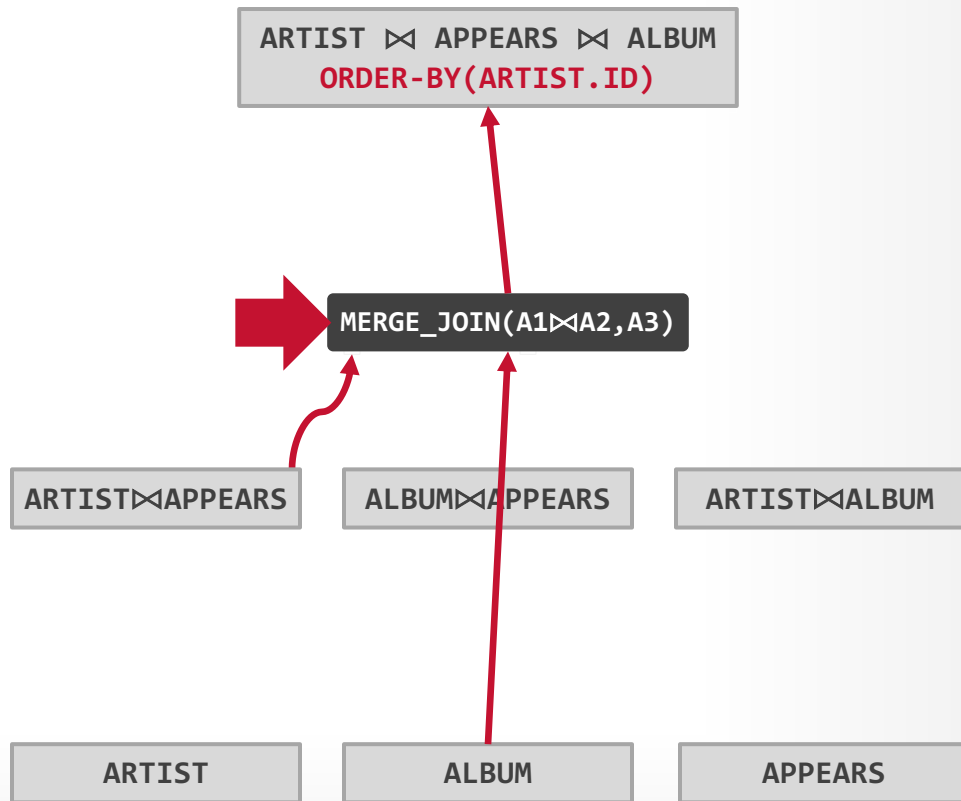
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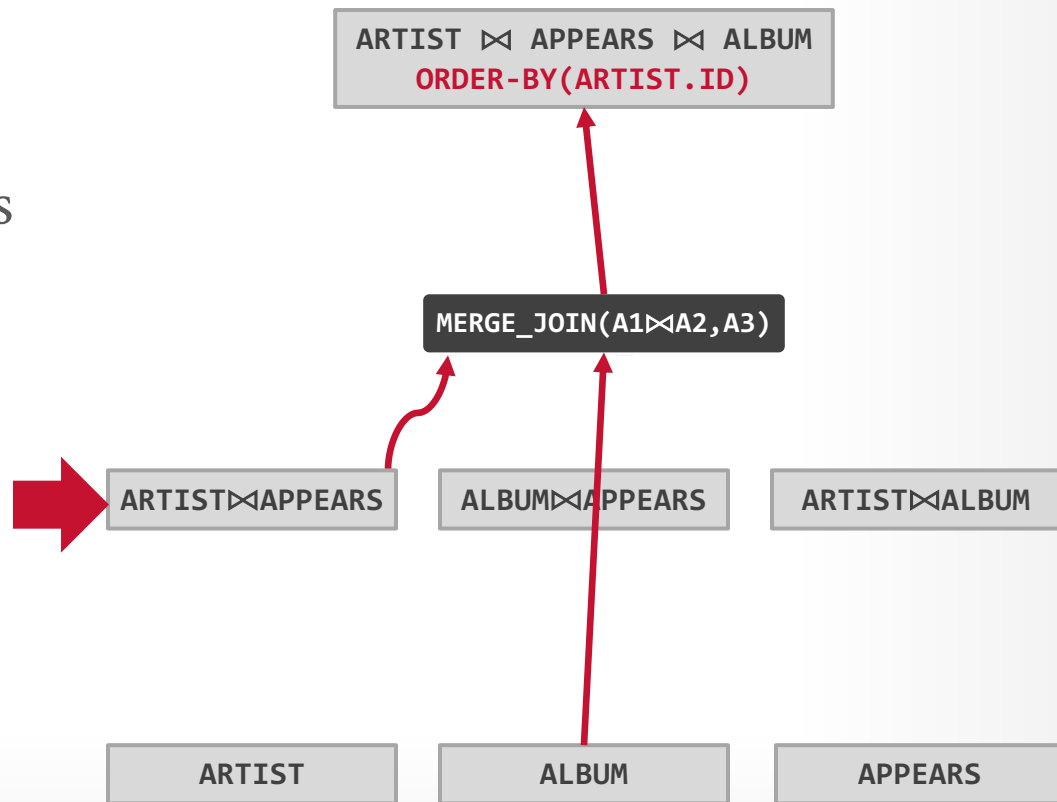
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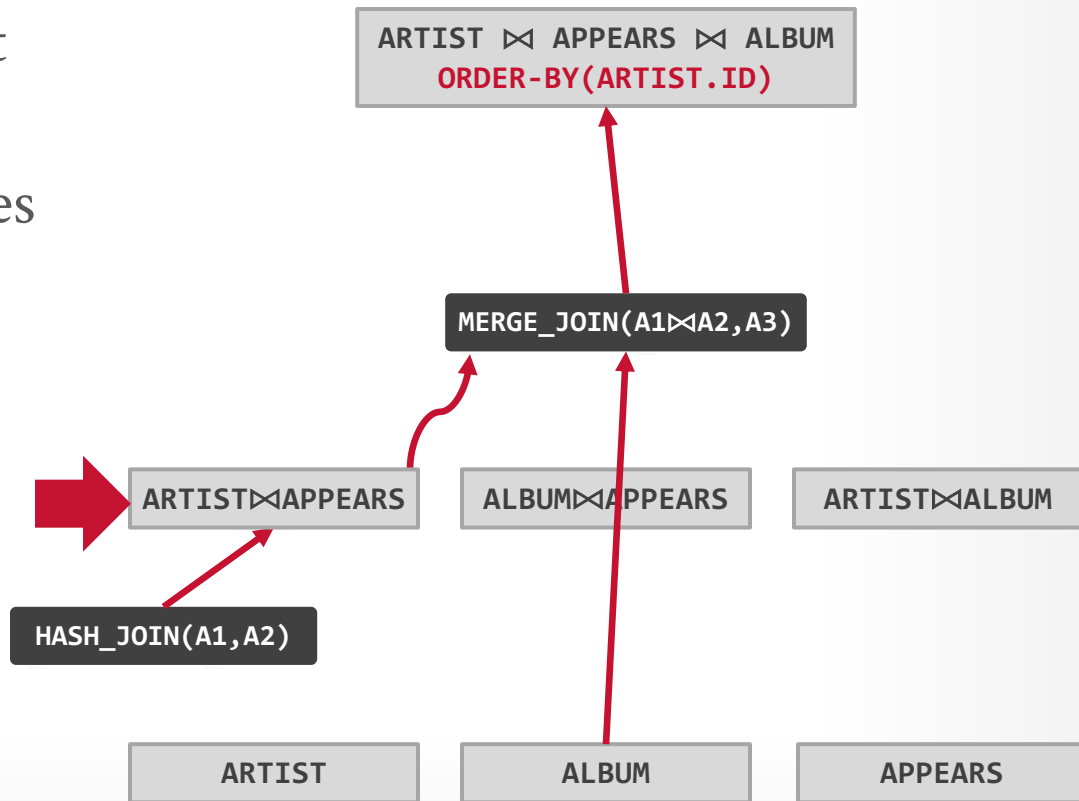
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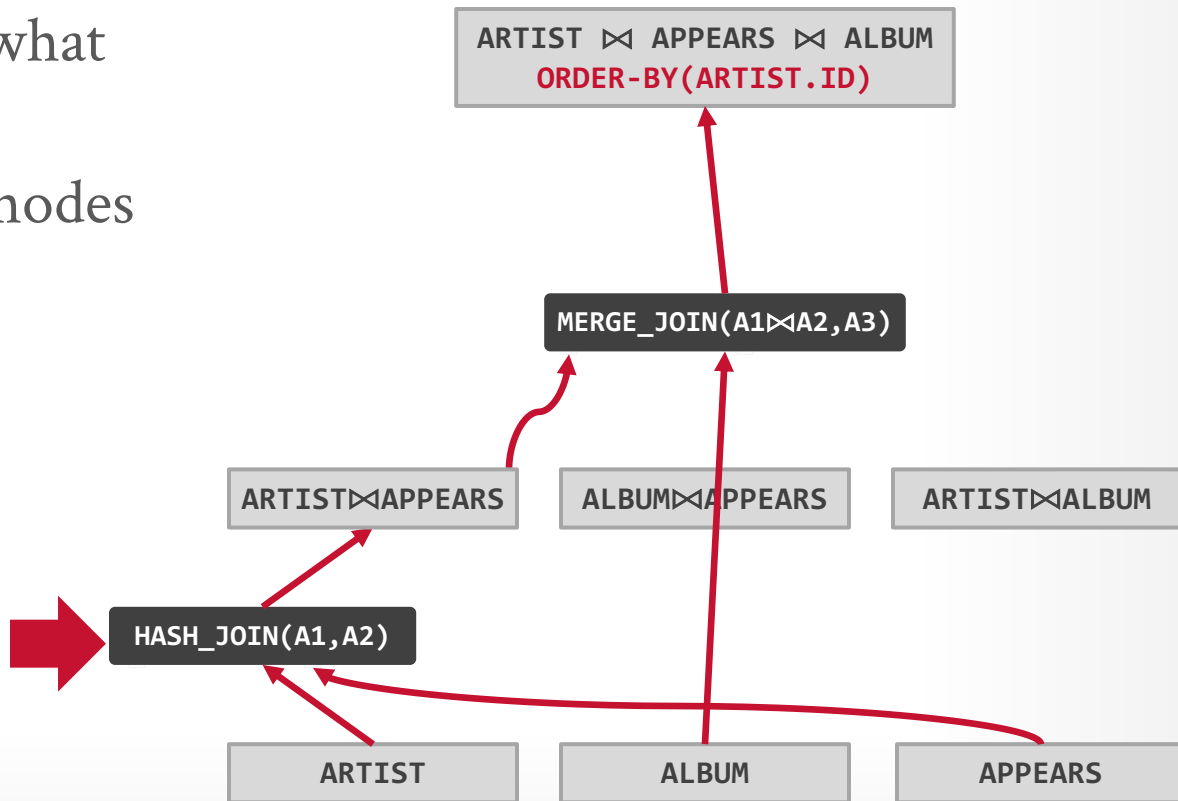
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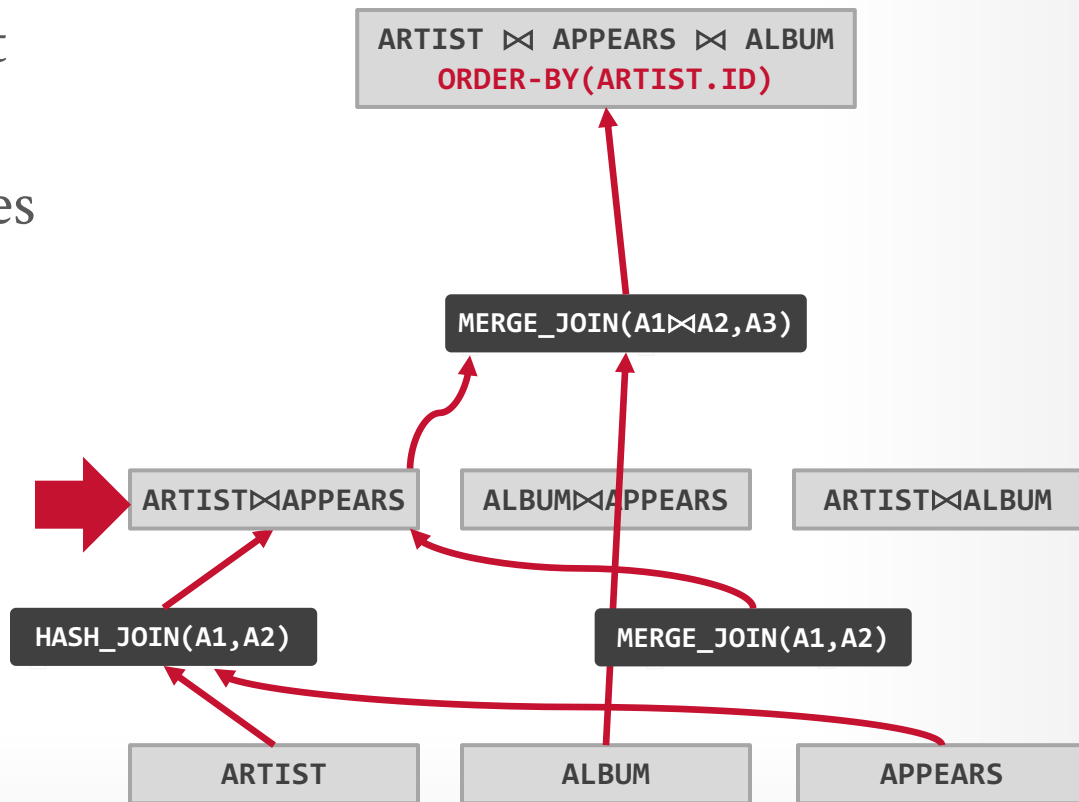
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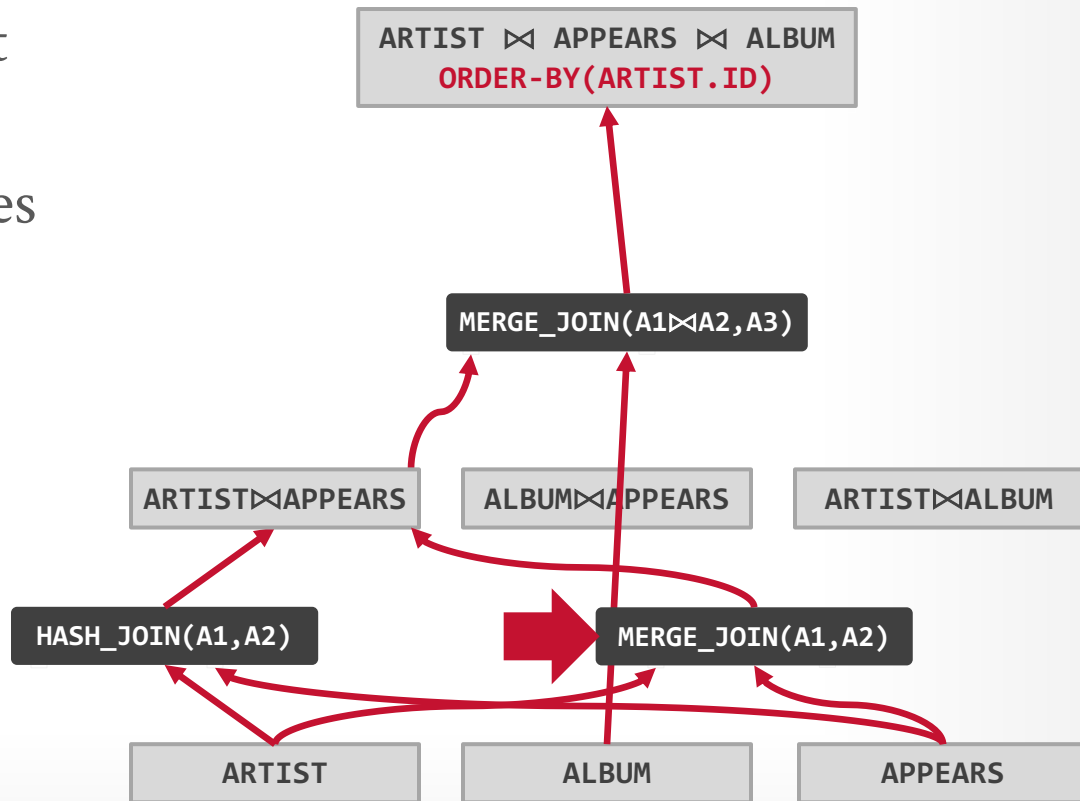
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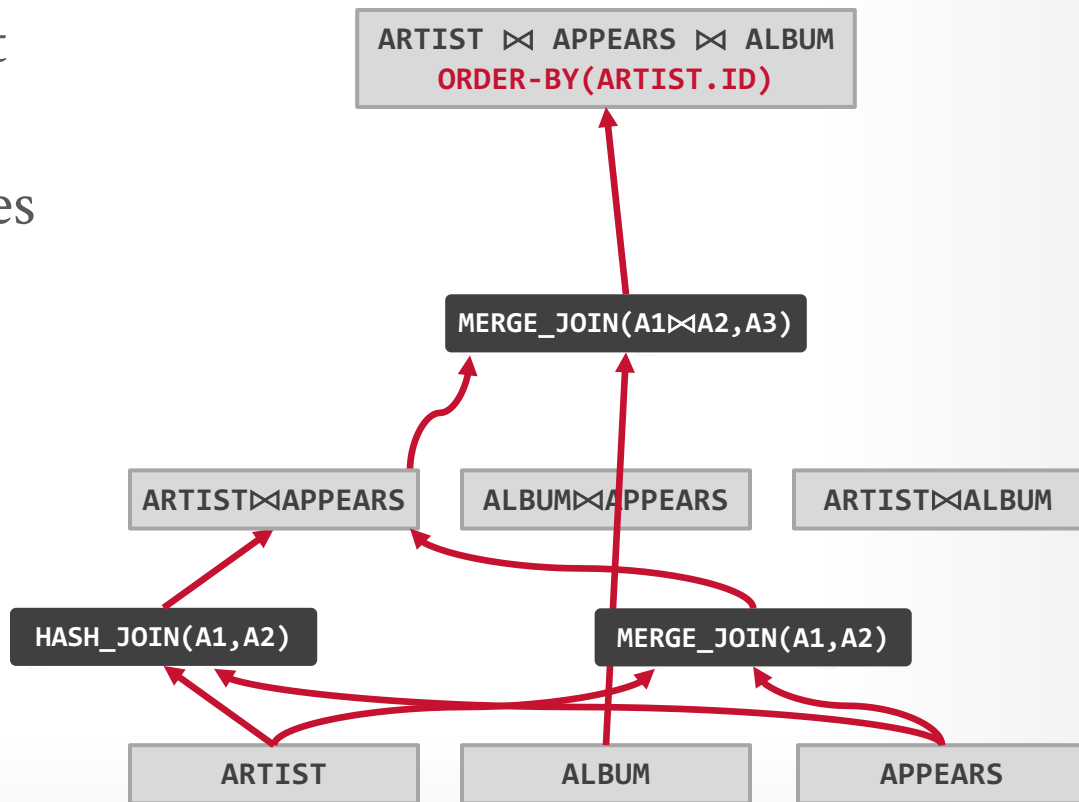
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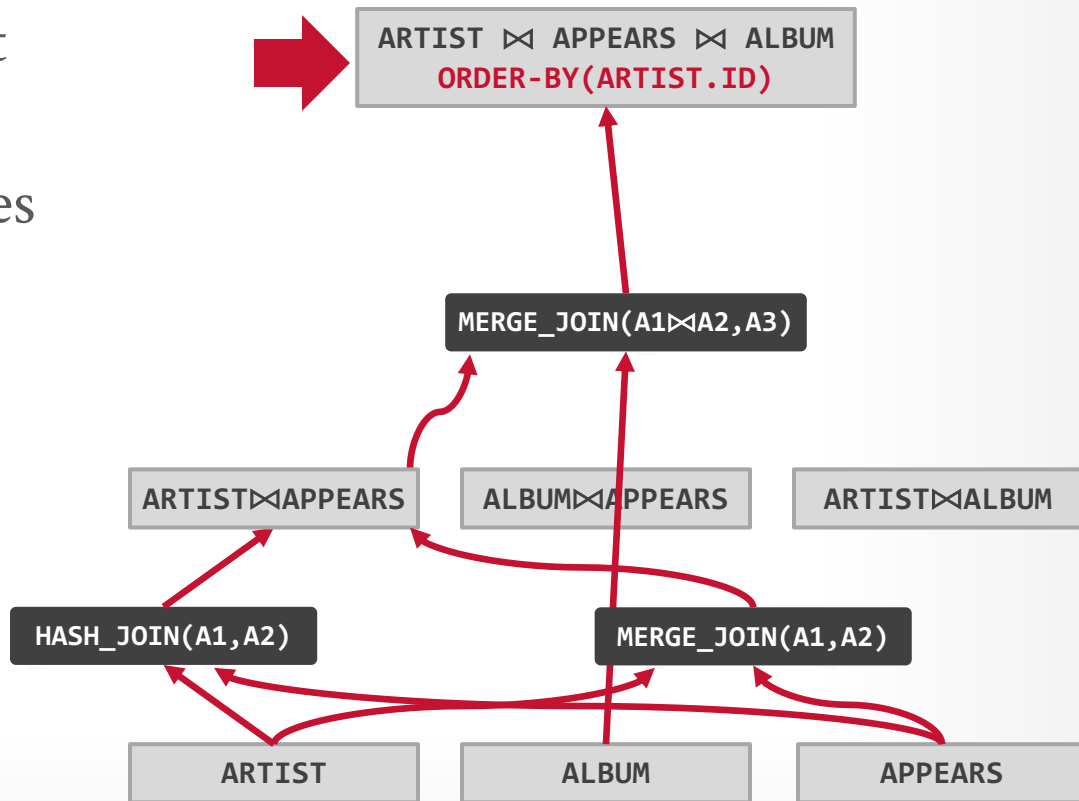
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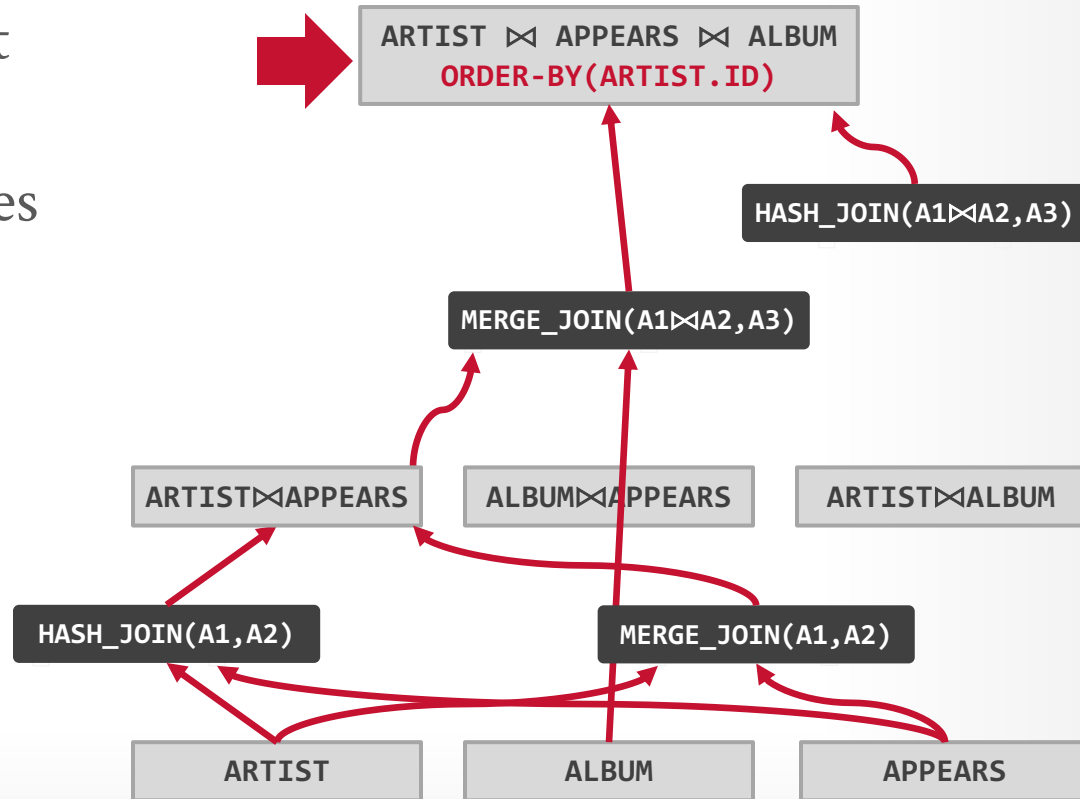
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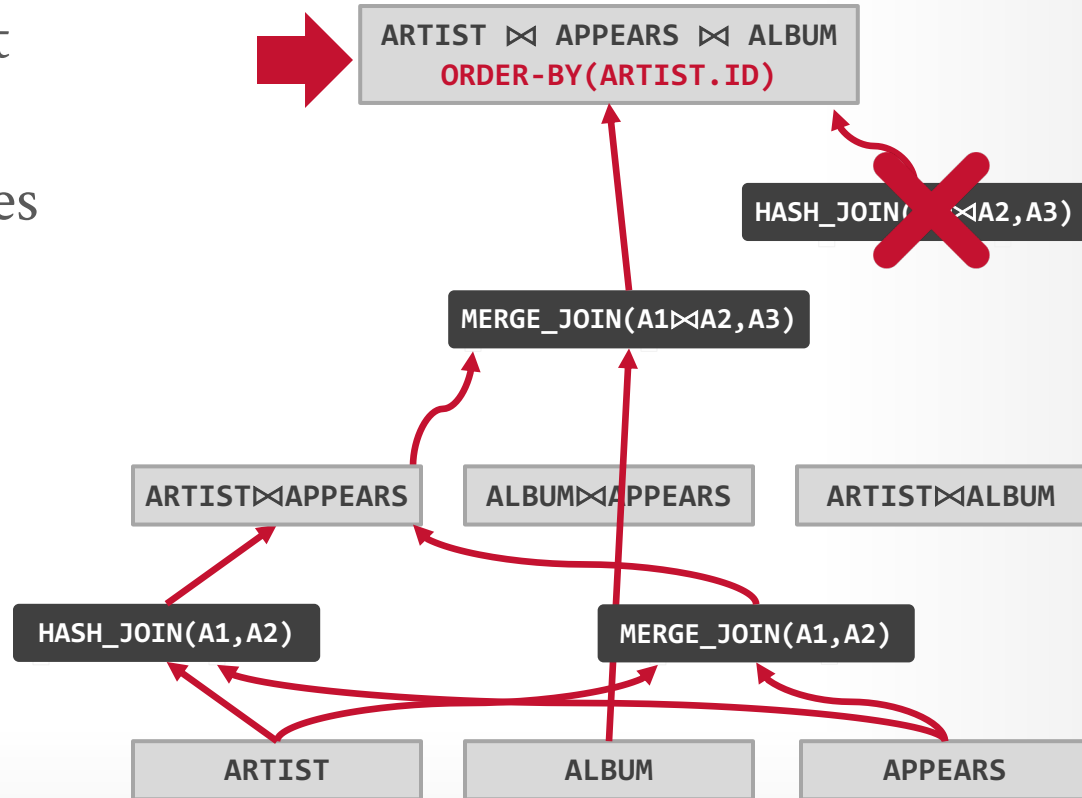
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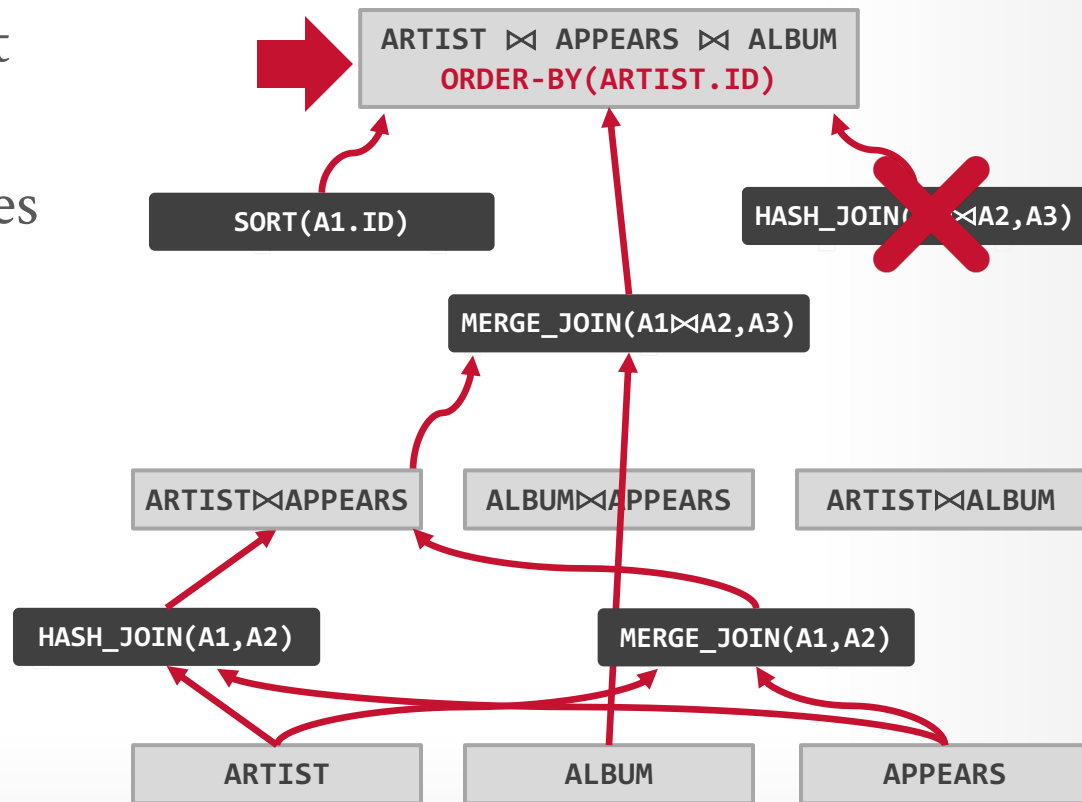
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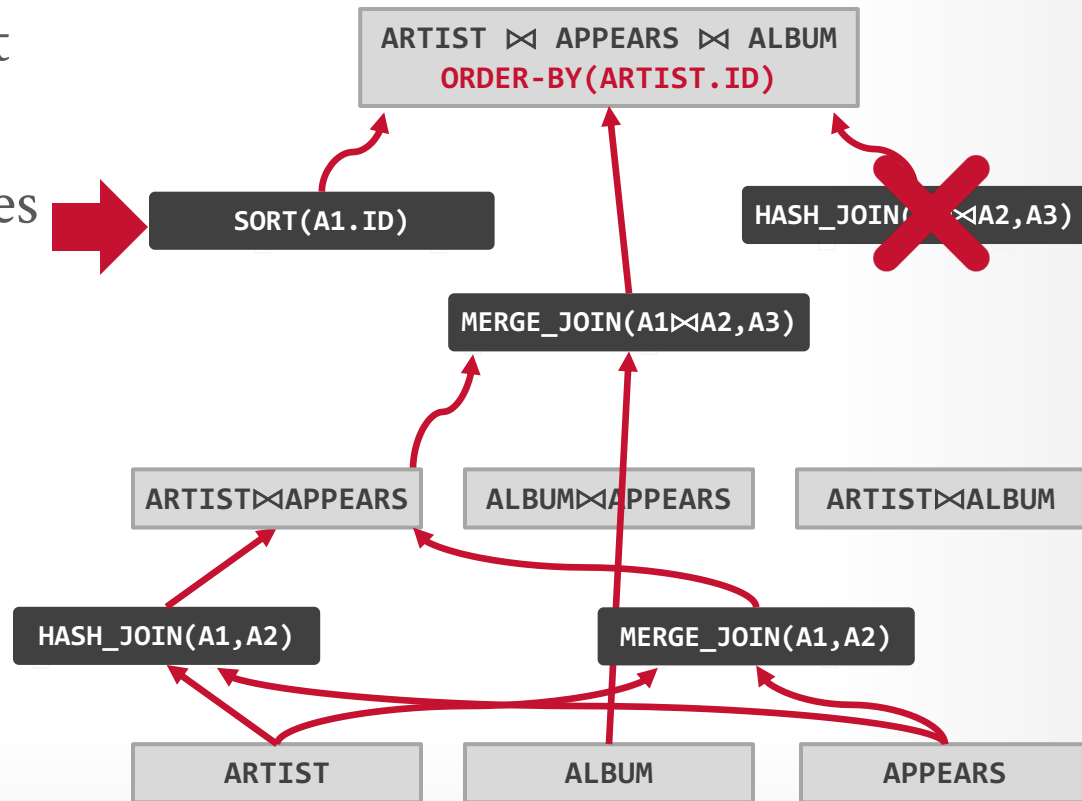
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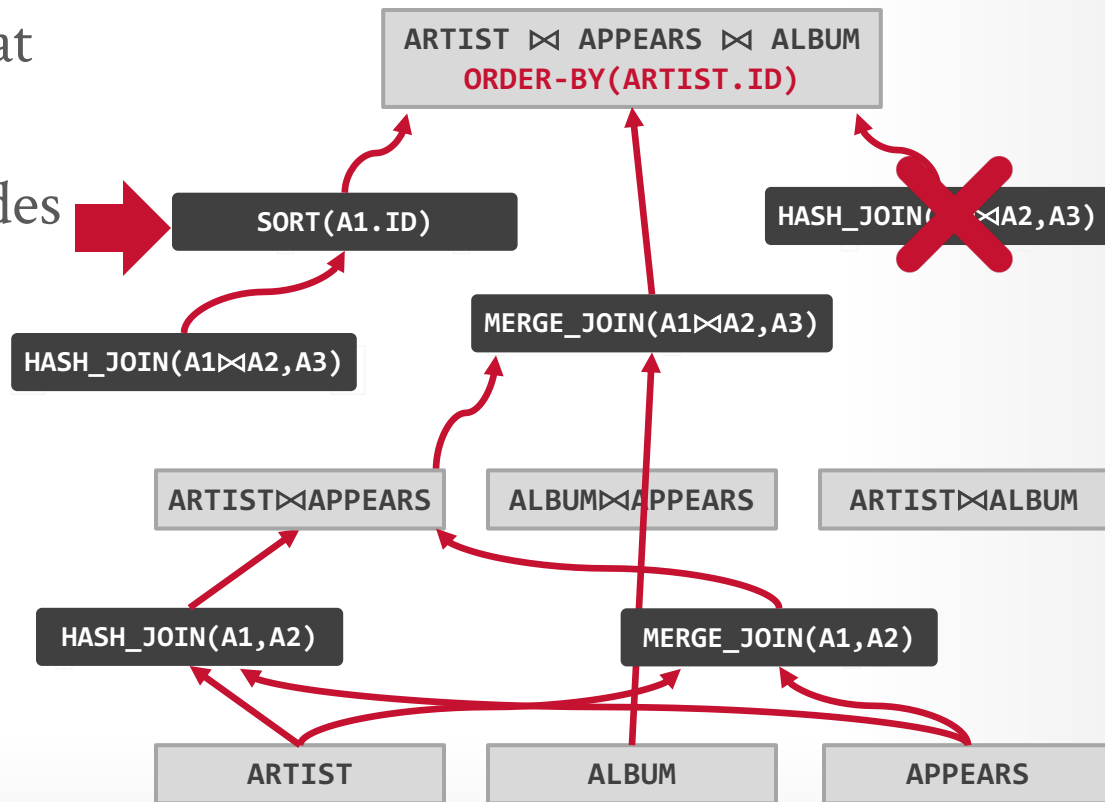
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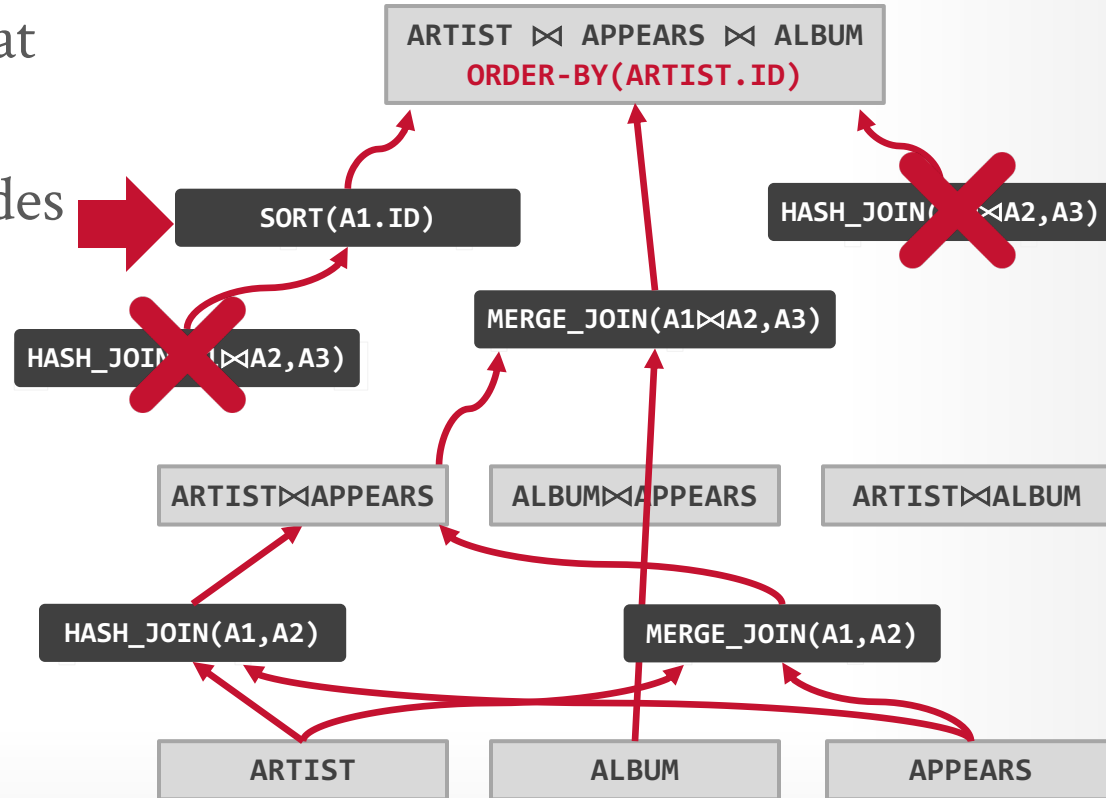
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Can create "enforcer" rules that require input to have certain properties.



# OBSERVATION

---

Applications often execute nested queries.

- We could optimize each block using the methods we have discussed.
- However, this may be inefficient since we optimize each block separately without a global approach.

What if we could flatten a nested query into a single block and optimize it?

- Then, apply single-block query optimization methods.
- Even if one cannot flatten to a single block, flattening to fewer blocks is still beneficial.

# NESTED SUB-QUERIES

---

The DBMS treats nested sub-queries in the where clause as functions that take parameters and return a single value or set of values.

**Approach #1: Rewrite to de-correlate and/or flatten them.**

**Approach #2: Decompose nested query and store results in a temporary table.**

# NESTED SUB-QUERIES: REWRITE

---

```
SELECT name FROM sailors AS S
WHERE EXISTS (
  SELECT * FROM reserves AS R
  WHERE S.sid = R.sid
  AND R.day = '2024-10-25'
)
```

# NESTED SUB-QUERIES: REWRITE

---

```
SELECT name FROM sailors AS S
WHERE EXISTS (
  SELECT * FROM reserves AS R
  WHERE S.sid = R.sid
  AND R.day = '2024-10-25'
)
```

# NESTED SUB-QUERIES: REWRITE

---

```
SELECT name FROM sailors AS S
WHERE EXISTS (
  SELECT * FROM reserves AS R
  WHERE S.sid = R.sid
  AND R.day = '2024-10-25'
)
```



```
SELECT name
FROM sailors AS S, reserves AS R
WHERE S.sid = R.sid
AND R.day = '2024-10-25'
```



# DECOMPOSING QUERIES

---

For harder queries, the optimizer breaks up queries into blocks and then concentrates on one block at a time.

Sub-queries are written to temporary tables that are discarded after the query finishes.

# DECOMPOSING QUERIES

---

```
SELECT S.sid, MIN(R.day)
  FROM sailors S, reserves R, boats B
 WHERE S.sid = R.sid
   AND R.bid = B.bid
   AND B.color = 'red'
   AND S.rating = (SELECT MAX(S2.rating)
                   FROM sailors S2)

GROUP BY S.sid
HAVING COUNT(*) > 1
```

# DECOMPOSING QUERIES

---

```
SELECT S.sid, MIN(R.day)
  FROM sailors S, reserves R, boats B
 WHERE S.sid = R.sid
    AND R.bid = B.bid
    AND B.color = 'red'
    AND S.rating = (SELECT MAX(S2.rating)
                    FROM sailors S2)

 GROUP BY S.sid
HAVING COUNT(*) > 1
```

*Nested Block*

# DECOMPOSING QUERIES

---

```
SELECT MAX(rating) FROM sailors
```

```
SELECT S.sid, MIN(R.day)
FROM sailors S, reserves R, boats B
WHERE S.sid = R.sid
AND R.bid = B.bid
AND B.color = 'red'
AND S.rating = (SELECT MAX(S2.rating)
                FROM sailors S2)

GROUP BY S.sid
HAVING COUNT(*) > 1
```

*Nested Block*

# DECOMPOSING QUERIES

---

```
SELECT MAX(rating) FROM sailors
```

```
SELECT S.sid, MIN(R.day)
FROM sailors S, reserves R, boats B
WHERE S.sid = R.sid
      AND R.bid = B.bid
      AND B.color = 'red'
      AND S.rating = ###

GROUP BY S.sid
HAVING COUNT(*) > 1
```

*Nested Block*

# DECOMPOSING QUERIES

---

```
SELECT MAX(rating) FROM sailors
```

```
SELECT S.sid, MIN(R.day)
FROM sailors S, reserves R, boats B
WHERE S.sid = R.sid
      AND R.bid = B.bid
      AND B.color = 'red'
      AND S.rating = ### ←
GROUP BY S.sid
HAVING COUNT(*) > 1
```

# DECOMPOSING QUERIES

---

*Inner Block*

```
SELECT MAX(rating) FROM sailors
```

```
SELECT S.sid, MIN(R.day)
FROM sailors S, reserves R, boats B
WHERE S.sid = R.sid
      AND R.bid = B.bid
      AND B.color = 'red'
      AND S.rating = ### ←
GROUP BY S.sid
HAVING COUNT(*) > 1
```

*Outer Block*

# EXPRESSION REWRITING

---

An optimizer transforms a query's expressions (e.g., **WHERE/ON** clause predicates) into the minimal set of expressions.

Implemented using if/then/else clauses or a pattern-matching rule engine.

- Search for expressions that match a pattern.
- When a match is found, rewrite the expression.
- Halt if there are no more rules that match.



# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE 1 = 0;
```

# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE 1 = 0
```

# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
```

# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
```

```
SELECT * FROM A WHERE NOW() IS NULL;
```

# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
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```
SELECT * FROM A WHERE NOW() IS NULL;
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# EXPRESSION REWRITING

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# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
```

```
SELECT * FROM A WHERE false;
```

## Merging Predicates

```
SELECT * FROM A  
WHERE val BETWEEN 1 AND 100  
OR val BETWEEN 50 AND 150;
```

# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
```

```
SELECT * FROM A WHERE false;
```

## Merging Predicates

```
SELECT * FROM A  
WHERE val BETWEEN 1 AND 100  
OR val BETWEEN 50 AND 150;
```



# EXPRESSION REWRITING

---

## Impossible / Unnecessary Predicates

```
SELECT * FROM A WHERE false;
```

```
SELECT * FROM A WHERE false;
```

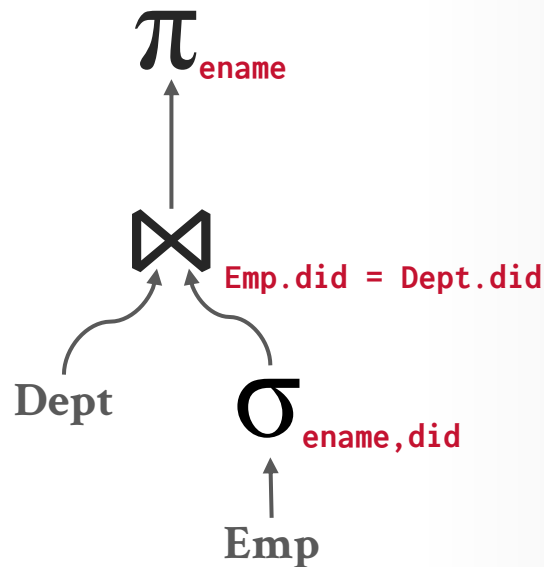
## Merging Predicates

```
SELECT * FROM A  
WHERE val BETWEEN 1 AND 150;
```

# OBSERVATION

---

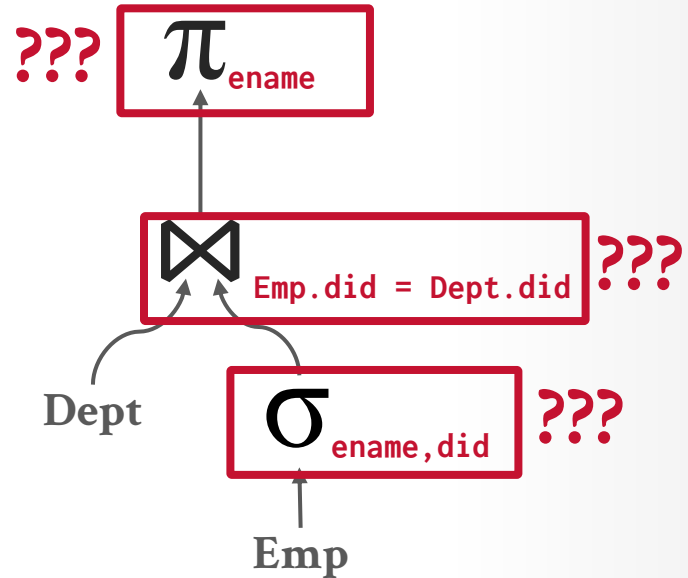
We have formulas for the operator algorithms (e.g. the cost formulas for hash join, sort merge join, ...), but we also need to estimate the size of the output that an operator produces.



# OBSERVATION

---

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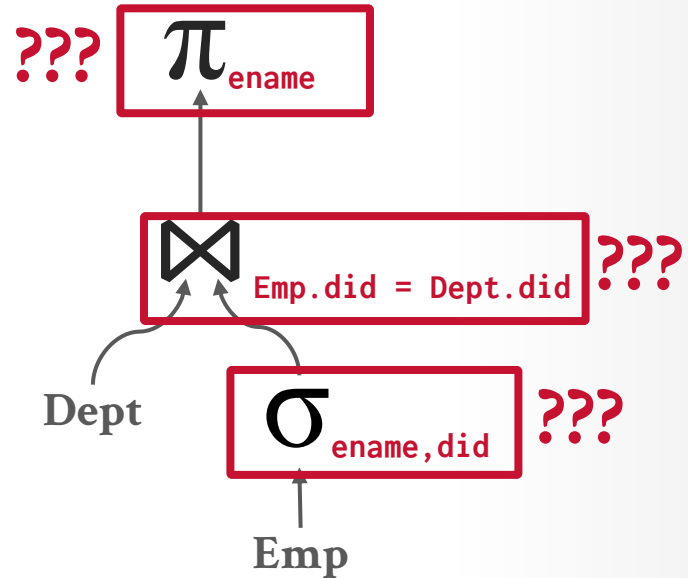


# OBSERVATION

---

We have formulas for the operator algorithms (e.g. the cost formulas for hash join, sort merge join, ...), but we also need to estimate the size of the output that an operator produces.

This is hard because the output of each operators depends on its input.



# COST ESTIMATION

---

The DBMS uses a cost model to predict the behavior of a query plan given a database state.

→ This is an internal cost that allows the DBMS to compare one plan with another.

It is too expensive to run every possible plan to determine this information, so the DBMS need a way to derive this information.

# COST MODEL COMPONENTS

---

## Choice #1: Physical Costs

- Predict CPU cycles, I/O, cache misses, RAM consumption, network messages...
- Depends heavily on hardware.

## Choice #2: Logical Costs

- Estimate output size per operator.
- Independent of the operator algorithm.
- Need estimations for operator result sizes.

# POSTGRES COST MODEL

---

Uses a combination of CPU and I/O costs that are weighted by “magic” constant factors.

Default settings are obviously for a disk-resident database without a lot of memory:

- Processing a tuple in memory is **400x** faster than reading a tuple from disk.
- Sequential I/O is **4x** faster than random I/O.

### 19.7.2. Planner Cost Constants

The *cost* variables described in this section are measured on an arbitrary scale. Only their relative values matter, hence scaling them all up or down by the same factor will result in no change in the planner's choices. By default, these cost variables are based on the cost of sequential page fetches; that is, `seq_page_cost` is conventionally set to 1.0 and the other cost variables are set with reference to that. But you can use a different scale if you prefer, such as actual execution times in milliseconds on a particular machine.

**Note:** Unfortunately, there is no well-defined method for determining ideal values for the cost variables. They are best treated as averages over the entire mix of queries that a particular installation will receive. This means that changing them on the basis of just a few experiments is very risky.

`seq_page_cost` (floating point)

Sets the planner's estimate of the cost of a disk page fetch that is part of a series of sequential fetches. The default is 1.0. This value can be overridden for tables and indexes in a particular tablespace by setting the tablespace parameter of the same name (see [ALTER TABLESPACE](#)).

`random_page_cost` (floating point)



# STATISTICS

---

The DBMS stores internal statistics about tables, attributes, and indexes in its internal catalog.

Different systems update them at different times.

Manual invocations:

- Postgres/SQLite: **ANALYZE**
- Oracle/MySQL: **ANALYZE TABLE**
- SQL Server: **UPDATE STATISTICS**
- DB2: **RUNSTATS**

# SELECTION CARDINALITY

---

The selectivity (**sel**) of a predicate **P** is the fraction of tuples that qualify.

**Equality Predicate:  $A = \text{constant}$**

→  **$\text{sel}(A = \text{constant}) = \# \text{occurrences} / |R|$**

```
SELECT * FROM people
WHERE age = 9
```

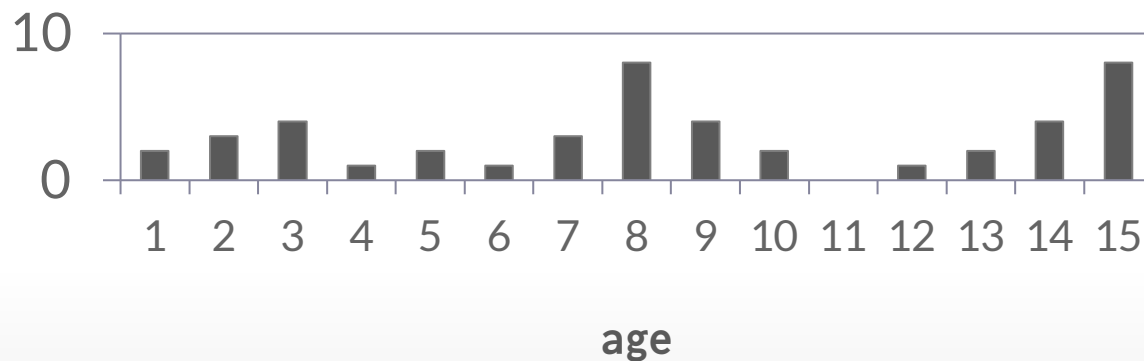
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# SELECTION CARDINALITY

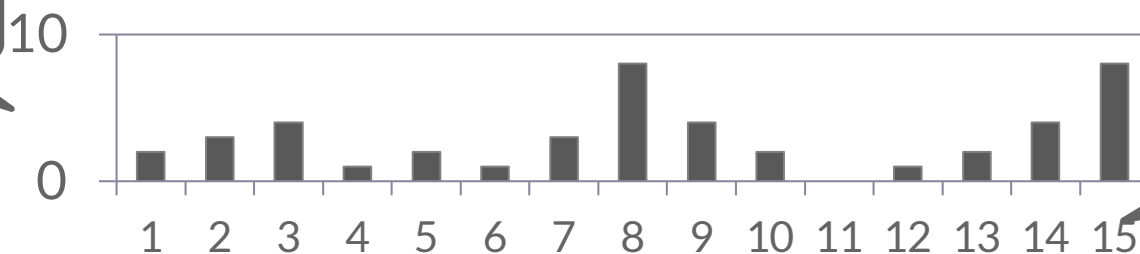
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*# of occurrences*



*Distinct values of attribute*

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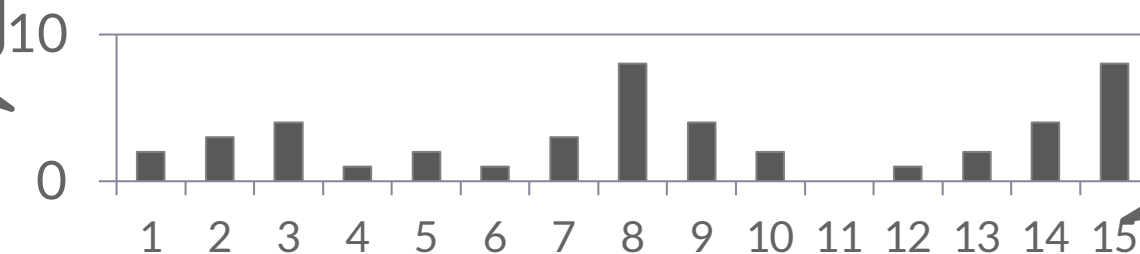
**Equality Predicate:  $A = \text{constant}$**

→  $\text{sel}(A = \text{constant}) = \text{\#occurrences} / |R|$

→ Example:  $\text{sel}(\text{age} = 9) =$

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SELECT * FROM people
WHERE age = 9
```

*# of occurrences*



*Distinct values of attribute*

# SELECTION CARDINALITY

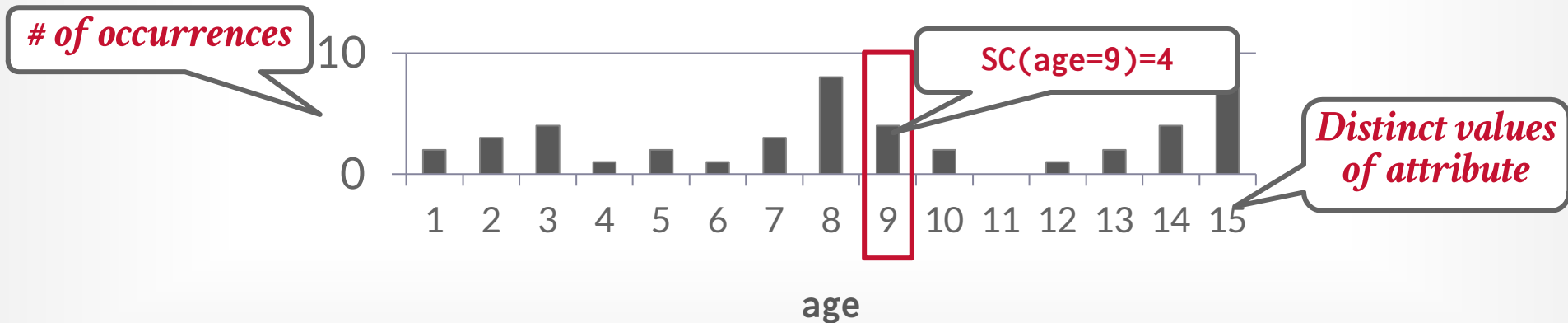
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# SELECTION CARDINALITY

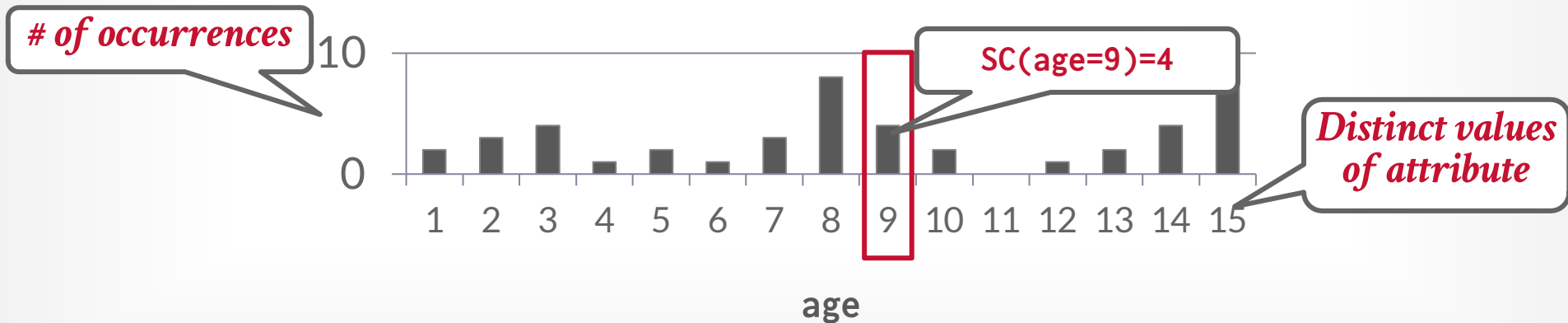
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→ Example:  $\text{sel}(\text{age} = 9) = 4/45$

```
SELECT * FROM people
WHERE age = 9
```



# SELECTION CARDINALITY

---

## **Assumption #1: Uniform Data**

→ The distribution of values (except for the heavy hitters) is the same.

## **Assumption #2: Independent Predicates**

→ The predicates on attributes are independent

## **Assumption #3: Inclusion Principle**

→ The domain of join keys overlap such that each key in the inner relation will also exist in the outer table.



# CORRELATED ATTRIBUTES

---

Consider a database of automobiles:

→ # of Makes = 10, # of Models = 100

And the following query:

→ (make="Honda" **AND** model="Accord")

With the independence and uniformity assumptions, the selectivity is:

→  $1/10 \times 1/100 = 0.001$

But since only Honda makes Accords the real selectivity is  $1/100 = 0.01$

# STATISTICS

---

## Choice #1: Histograms

→ Maintain an occurrence count per value (or range of values) in a column.

## Choice #2: Sketches

→ Probabilistic data structure that gives an approximate count for a given value.

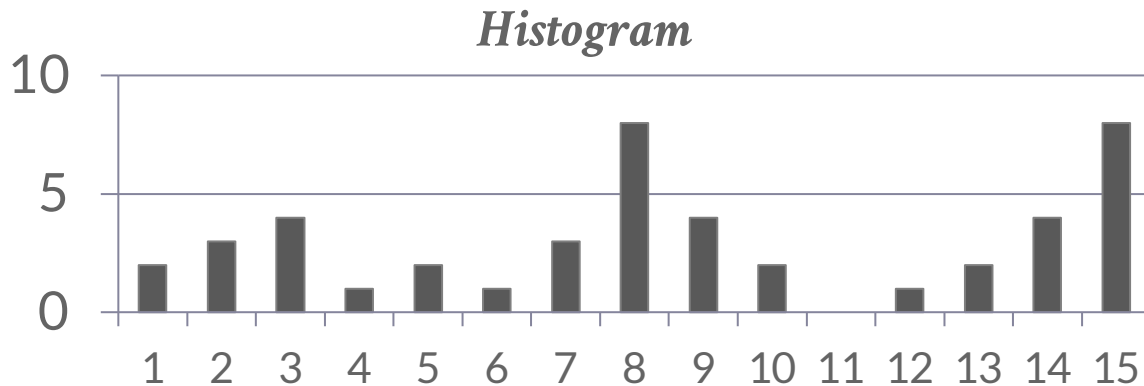
## Choice #3: Sampling

→ DBMS maintains a small subset of each table that it then uses to evaluate expressions to compute selectivity.

# HISTOGRAMS

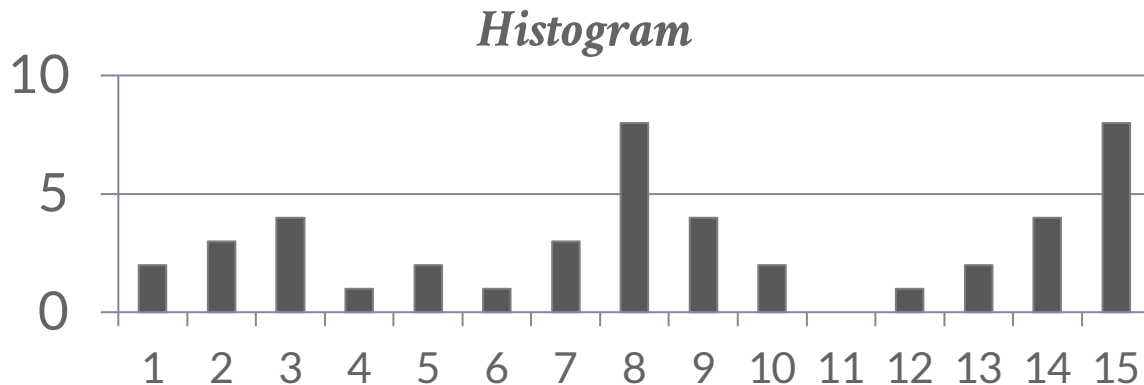
---

Our formulas are nice, but we assume that data values are uniformly distributed.



# HISTOGRAMS

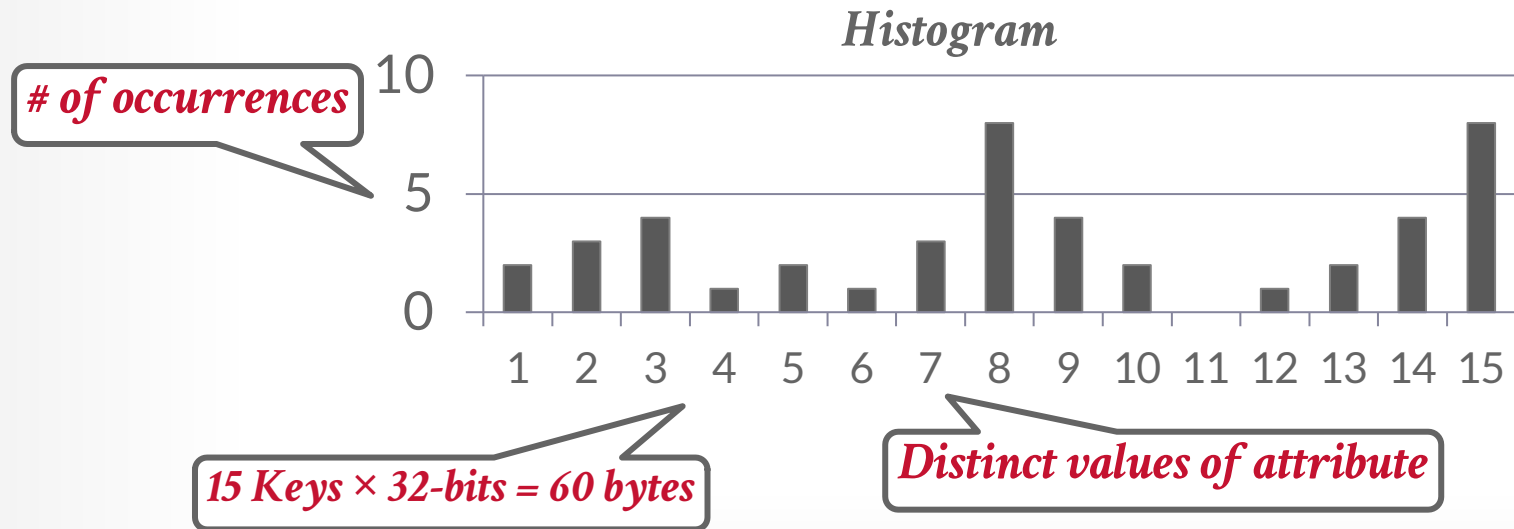
Our formulas are nice, but we assume that data values are uniformly distributed.



***15 Keys × 32-bits = 60 bytes***

# HISTOGRAMS

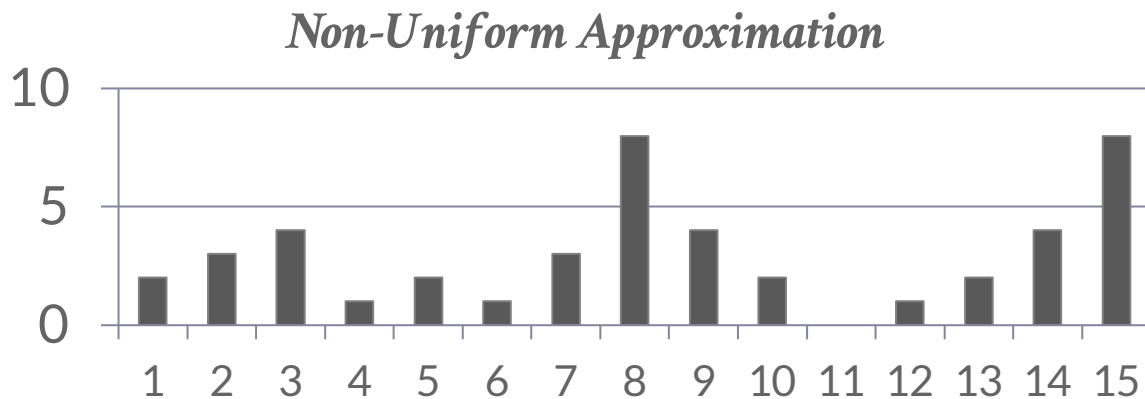
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# EQUI-WIDTH HISTOGRAM

---

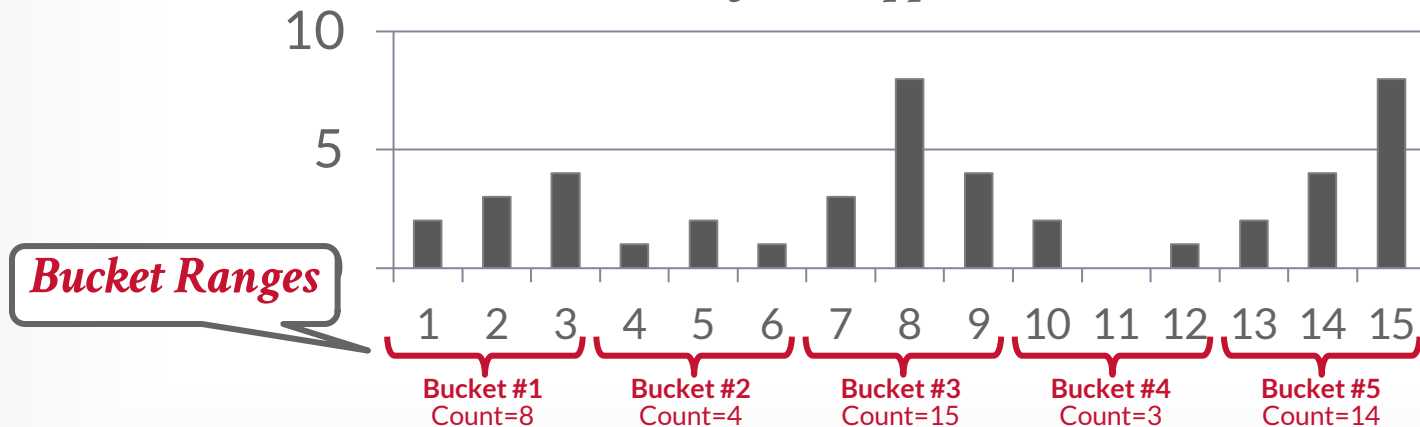
Maintain counts for a group of values instead of each unique key. All buckets have the same width (i.e., same # of value).



# EQUI-WIDTH HISTOGRAM

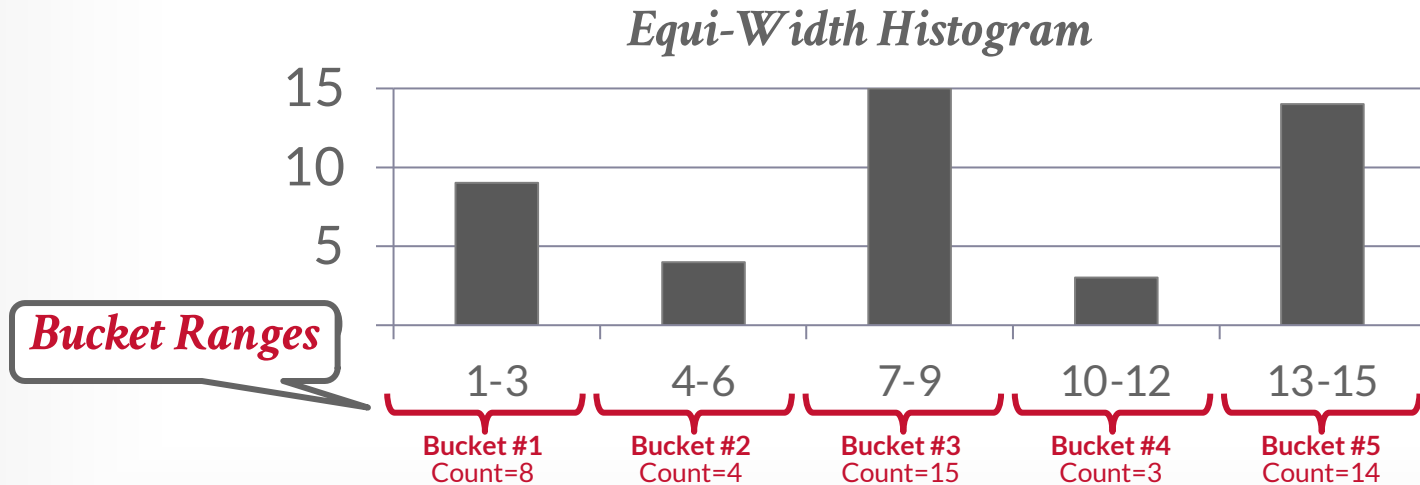
Maintain counts for a group of values instead of each unique key. All buckets have the same width (i.e., same # of value).

*Non-Uniform Approximation*



# EQUI-WIDTH HISTOGRAM

Maintain counts for a group of values instead of each unique key. All buckets have the same width (i.e., same # of value).

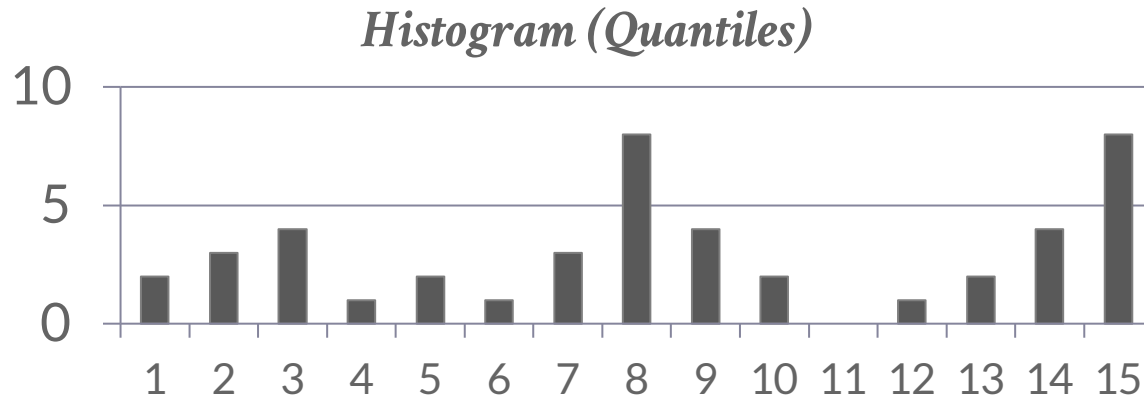




# EQUI-DEPTH HISTOGRAMS

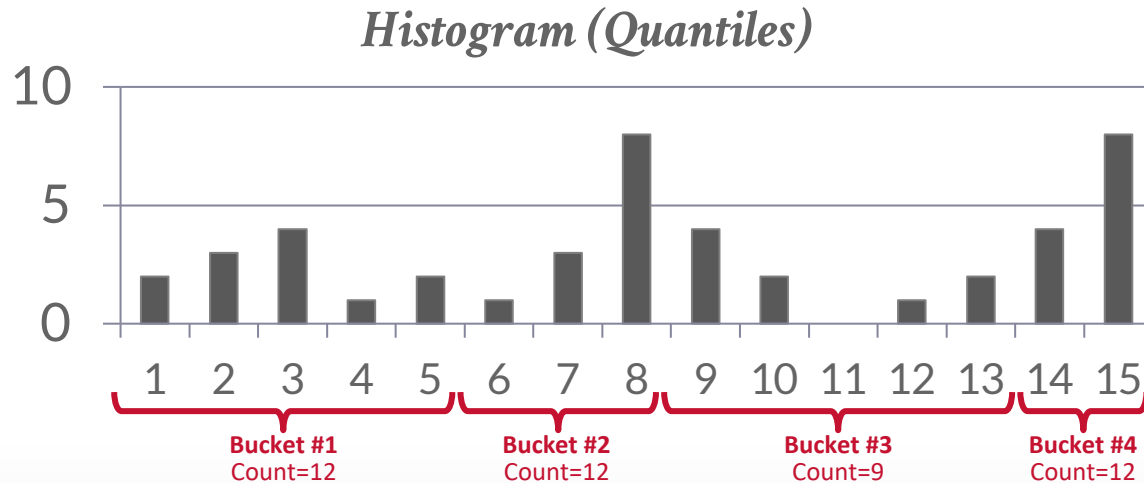
---

Vary the width of buckets so that the total number of occurrences for each bucket is roughly the same.



# EQUI-DEPTH HISTOGRAMS

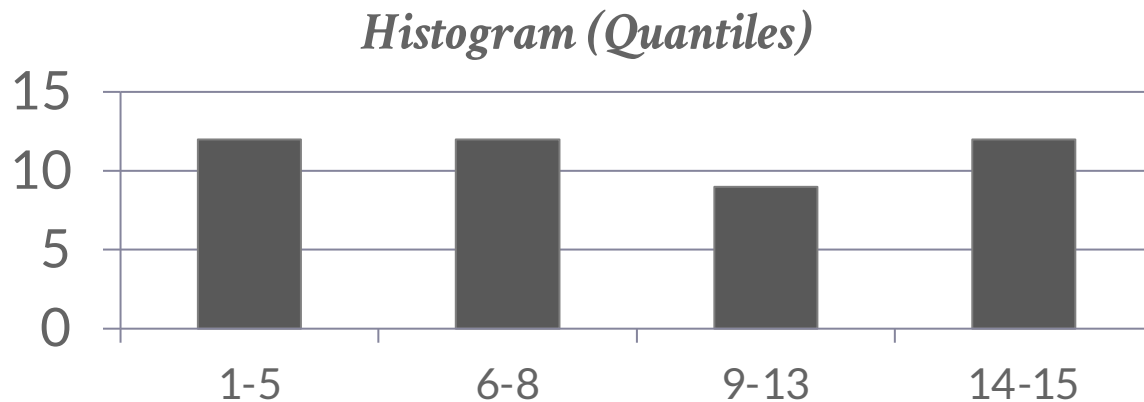
Vary the width of buckets so that the total number of occurrences for each bucket is roughly the same.



# EQUI-DEPTH HISTOGRAMS

---

Vary the width of buckets so that the total number of occurrences for each bucket is roughly the same.



# SKETCHES

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Probabilistic data structures that generate approximate statistics about a data set.

Cost-model can replace histograms with sketches to improve its selectivity estimate accuracy.

Most common examples:

- Count-Min Sketch (1988): Approximate frequency count of elements in a set.
- HyperLogLog (2007): Approximate the number of distinct elements in a set.

# SAMPLING

---

Modern DBMSs also collect samples from tables to estimate selectivities.

Update samples when the underlying tables changes significantly.

```
SELECT AVG(age)
FROM people
WHERE age > 50
```

id	name	age	status
1001	Obama	63	Rested
1002	Swift	34	Paid
1003	Tupac	25	Dead
1004	Bieber	30	Crunk
1005	Andy	43	Illin
1006	TigerKing	61	Jailed

⋮

*1 billion tuples*


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## *Table Sample*

1001	Obama	63	Rested
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Update samples when the underlying tables changes significantly.

## *Table Sample*

1001	Obama	63	Rested
1003	Tupac	25	Dead
1005	Andy	43	Illin

$sel(age > 50) =$

```
SELECT AVG(age)
FROM people
WHERE age > 50
```



id	name	age	status
1001	Obama	63	Rested
1002	Swift	34	Paid
1003	Tupac	25	Dead
1004	Bieber	30	Crunk
1005	Andy	43	Illin
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## *Table Sample*

1001	Obama	63	Rested
1003	Tupac	25	Dead
1005	Andy	43	Illin

$sel(age > 50) =$

```
SELECT AVG(age)
FROM people
WHERE age > 50
```



id	name	age	status
1001	Obama	63	Rested
1002	Swift	34	Paid
1003	Tupac	25	Dead
1004	Bieber	30	Crunk
1005	Andy	43	Illin
1006	TigerKing	61	Jailed

⋮

*1 billion tuples*

# SAMPLING

Modern DBMSs also collect samples from tables to estimate selectivities.


Update samples when the underlying tables changes significantly.

## *Table Sample*

1001	Obama	63	Rested
1003	Tupac	25	Dead
1005	Andy	43	Illin

$$\text{sel}(\text{age} > 50) = 1/3$$

```
SELECT AVG(age)
FROM people
WHERE age > 50
```



id	name	age	status
1001	Obama	63	Rested
1002	Swift	34	Paid
1003	Tupac	25	Dead
1004	Bieber	30	Crunk
1005	Andy	43	Illin
1006	TigerKing	61	Jailed

⋮

*1 billion tuples*

# CONCLUSION

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Query optimization is critical for a database system.

→ SQL → Logical Plan → Physical Plan

→ Flatten queries before going to the optimization part.

Expression handling is also important.

→ Estimate costs using models based on summarizations.

QO enumeration can be bottom-up or top-down.

# NEXT CLASS

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Transactions!

→ aka the second hardest part about database systems